# Computer Vision 2 WS 2018/19

#### Part 10 – Multi-Object Tracking 27.11.2018

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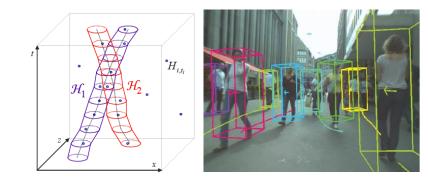
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# **Course Outline**

- Single-Object Tracking
- Bayesian Filtering
  - Kalman Filters, EKF
  - Particle Filters
- Multi-Object Tracking
  - Introduction
  - MHT, JPDAF

- Network Flow Optimization
- Visual Odometry
- Visual SLAM & 3D Reconstruction
- Deep Learning for Video Analysis

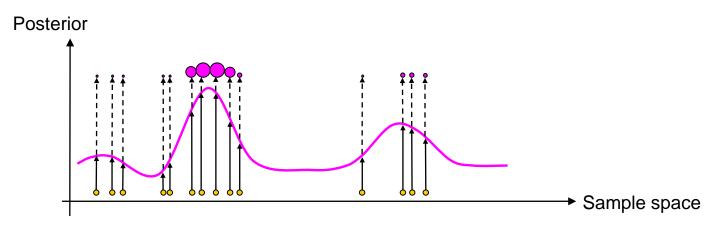






## **Recap: Particle Filtering**

- Many variations, one general concept:
  - Represent the posterior pdf by a set of randomly chosen weighted samples (particles)



- Randomly Chosen = Monte Carlo (MC)
- As the number of samples become very large the characterization becomes an equivalent representation of the true pdf.



Slide adapted from Michael Rubinstein





#### **Recap: Sequential Importance Sampling**

$$\begin{aligned} \mathbf{function} & \left[ \left\{ \mathbf{x}_{t}^{i}, w_{t}^{i} \right\}_{i=1}^{N} \right] = SIS \left[ \left\{ \mathbf{x}_{t-1}^{i}, w_{t-1}^{i} \right\}_{i=1}^{N}, \mathbf{y}_{t} \right] \\ \eta &= 0 \\ \text{Initialize} \\ \mathbf{for} \quad i = 1:N \end{aligned}$$

$$\begin{aligned} \mathbf{x}_{t}^{i} &\sim q(\mathbf{x}_{t} | \mathbf{x}_{t-1}^{i}, \mathbf{y}_{t}) \\ w_{t}^{i} &= w_{t-1}^{i} \frac{p(\mathbf{y}_{t} | \mathbf{x}_{t}^{i}) p(\mathbf{x}_{t}^{i} | \mathbf{x}_{t-1}^{i})}{q(\mathbf{x}_{t} | \mathbf{x}_{t-1}^{i}, \mathbf{y}_{t})} \\ \eta &= \eta + w_{t}^{i} \end{aligned}$$

end

for i = 1:N $w_t^i = w_t^i / \eta$ 

#### end

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Slide adapted from Michael Rubinstein

Sample from proposal pdf

Update weights

Update norm. factor

#### Normalize weights





#### Recap: Sequential Importance Sampling

$$\begin{aligned} & \text{function } \left[ \left\{ \mathbf{x}_{t}^{i}, w_{t}^{i} \right\}_{i=1}^{N} \right] = SIS \left[ \left\{ \mathbf{x}_{t-1}^{i}, w_{t-1}^{i} \right\}_{i=1}^{N}, \mathbf{y}_{t} \right] \\ & \eta = 0 & \text{Initialize} \\ & \text{for } i = 1:N & \\ & \mathbf{x}_{t}^{i} \sim q(\mathbf{x}_{t} | \mathbf{x}_{t-1}^{i}, \mathbf{y}_{t}) & \text{Sample from proposal pdf} \\ & w_{t}^{i} = w_{t-1}^{i} \frac{p(\mathbf{y}_{t} | \mathbf{x}_{t}^{i}) p(\mathbf{x}_{t}^{i} | \mathbf{x}_{t-1}^{i})}{q(\mathbf{x}_{t} | \mathbf{x}_{t-1}^{i}, \mathbf{y}_{t})} & \text{Update weights} \\ & \eta = \eta + w_{t}^{i} & \text{Update norm. factor} \\ & \text{end} & \\ & \text{for } i = 1:N & \\ & w_{t}^{i} = w_{t}^{i} / \eta & \text{For a concrete algorithm,} \\ & w_{t}^{i} = w_{t}^{i} / \eta & \text{Normalize weights} \end{aligned}$$

#### end

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#### Recap: SIS Algorithm with Transitional Prior

$$\begin{aligned} & \textbf{function} \left[ \left\{ \mathbf{x}_{t}^{i}, w_{t}^{i} \right\}_{i=1}^{N} \right] = SIS \left[ \left\{ \mathbf{x}_{t-1}^{i}, w_{t-1}^{i} \right\}_{i=1}^{N}, \mathbf{y}_{t} \right] \\ & \eta = 0 & \text{Initialize} \\ & \textbf{for } i = 1:N \\ & \mathbf{x}_{t}^{i} \sim p(\mathbf{x}_{t} | \mathbf{x}_{t-1}^{i}) & \text{Sample from proposal pdf} \\ & w_{t}^{i} = w_{t-1}^{i} p(\mathbf{y}_{t} | \mathbf{x}_{t}^{i}) & \text{Update weights} \\ & \eta = \eta + w_{t}^{i} & \text{Update norm. factor} \\ & \textbf{end} & \\ & \textbf{for } i = 1:N \\ & w_{t}^{i} = w_{t}^{i} / \eta & \text{Normalize weights} \end{aligned}$$

#### end

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Slide adapted from Michael Rubinstein





#### **Recap: Resampling**

- Degeneracy problem with SIS
  - After a few iterations, most particles have negligible weights.
  - Large computational effort for updating particles with very small contribution to  $p(\mathbf{x}_t | \mathbf{y}_{1:t})$ .
- Idea: Resampling
  - Eliminate particles with low importance weights and increase the number of particles with high importance weight.

$$\left\{\mathbf{x}_{t}^{i}, w_{t}^{i}\right\}_{i=1}^{N} \rightarrow \left\{\mathbf{x}_{t}^{i*}, \frac{1}{N}\right\}_{i=1}^{N}$$

– The new set is generated by sampling with replacement from the discrete representation of  $p(\mathbf{x}_t \mid \mathbf{y}_{1:t})$  such that

$$\Pr\left\{\mathbf{x}_t^{i*} = \mathbf{x}_t^j\right\} = w_t^j$$

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### Recap: Efficient Resampling Approach

#### • From Arulampalam paper:

Algorithm 2: Resampling Algorithm  $[\{\mathbf{x}_{k}^{j*}, w_{k}^{j}, i^{j}\}_{i=1}^{N_{s}}] = \text{RESAMPLE} [\{\mathbf{x}_{k}^{i}, w_{k}^{i}\}_{i=1}^{N_{s}}]$ • Initialize the CDF:  $c_1 = 0$ • FOR  $i = 2: N_*$ - Construct CDF:  $c_i = c_{i-1} + w_k^i$ END FOR Start at the bottom of the CDF: i = 1 • Draw a starting point:  $u_1 \sim \mathbb{U}[0, N_s^{-1}]$ • For  $j = 1: N_s$ - Move along the CDF:  $u_j = u_1 + N_s^{-1}(j-1)$ - WHILE  $u_i > c_i$ \* i = i + 1- END WHILE - Assign sample:  $\mathbf{x}_k^{j*} = \mathbf{x}_k^i$ - Assign weight:  $w_k^j = N_s^{-1}$ - Assign parent:  $i^{j} = i$ 

• END FOR

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Slide adapted from Robert Collins

Basic idea: choose one initial small random number; deterministically sample the rest by "crawling" up the cdf. This is  $\mathcal{O}(N)$ !





#### **Recap: Generic Particle Filter**

$$\begin{aligned} \mathbf{function} & \left[ \left\{ \mathbf{x}_{t}^{i}, w_{t}^{i} \right\}_{i=1}^{N} \right] = PF\left[ \left\{ \mathbf{x}_{t-1}^{i}, w_{t-1}^{i} \right\}_{i=1}^{N}, \mathbf{y}_{t} \right] \\ Apply SIS filtering & \left[ \left\{ \mathbf{x}_{t}^{i}, w_{t}^{i} \right\}_{i=1}^{N} \right] = SIS\left[ \left\{ \mathbf{x}_{t-1}^{i}, w_{t-1}^{i} \right\}_{i=1}^{N}, \mathbf{y}_{t} \right] \\ Calculate N_{eff} \end{aligned}$$

$$\begin{array}{ll} \mathbf{if} & N_{eff} < N_{thr} \\ & \left[ \left\{ \mathbf{x}_{t}^{i}, w_{t}^{i} \right\}_{i=1}^{N} \right] = RESAMPLE \left[ \left\{ \mathbf{x}_{t}^{i}, w_{t}^{i} \right\}_{i=1}^{N} \right] \\ \mathbf{end} \end{array}$$

- We can also apply resampling selectively
  - Only resample when it is needed, i.e.,  $N_{eff}$  is too low.
  - $\Rightarrow$  Avoids drift when the tracked state is stationary.

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## Recap: Sampling-Importance-Resampling (SIR)

function  $[\mathcal{X}_t] = SIR[\mathcal{X}_{t-1}, \mathbf{y}_t]$  $\bar{\mathcal{X}}_t = \mathcal{X}_t = \emptyset$ for i = 1:NSample  $\mathbf{x}_t^i \sim p(\mathbf{x}_t | \mathbf{x}_{t-1}^i)$  $w_t^i = p(\mathbf{y}_t | \mathbf{x}_t^i)$ end for i = 1:NDraw i with probability  $\propto w_t^i$ Add  $\mathbf{x}_{t}^{i}$  to  $\mathcal{X}_{t}$ 

#### end

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Slide adapted from Michael Rubinstein

#### Initialize

Generate new samples

Update weights

#### Resample





# Recap: Sampling-Importance-Resampling (SIR)

function 
$$[\mathcal{X}_t] = SIR [\mathcal{X}_{t-1}, \mathbf{y}_t]$$
  
 $\bar{\mathcal{X}}_t = \mathcal{X}_t = \emptyset$   
for  $i = 1:N$   
 $Sample \ \mathbf{x}_t^i \sim p(\mathbf{x}_t | \mathbf{x}_{t-1}^i)$   
 $w_t^i = p(\mathbf{y}_t | \mathbf{x}_t^i)$   
end  
for  $i = 1:N$ 

Draw i with probability  $\propto w_t^i$ Add  $\mathbf{x}_t^i$  to  $\mathcal{X}_t$ 

#### end

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Important property:

Particles are distributed according to pdf from previous time step.

Particles are distributed according to posterior from this time step.





#### Today: Multi-Object Tracking





# **Topics of This Lecture**

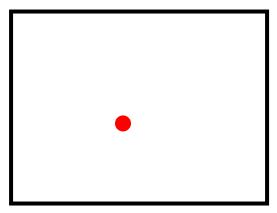
- Multi-Object Tracking
  - Motivation
  - Ambiguities
- Simple Approaches
  - Gating
  - Mahalanobis distance
  - Nearest-Neighbor Filter
- Track-Splitting Filter
  - Derivation
  - Properties
- Outlook

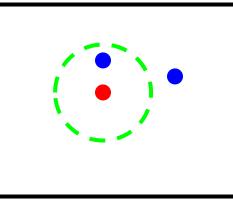


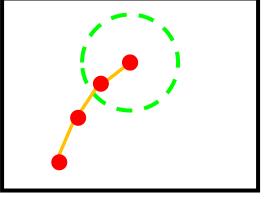




## **Elements of Tracking**







Detection

Data association

Prediction

- Detection
  - Where are candidate objects?
- Data association
  - Which detection corresponds to which object?
- Prediction

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- Where will the tracked object be in the next time step?

Lectures 7-9

Lectures 2-6

Today's topic



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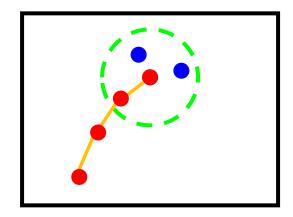
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# **Motion Correspondence**

- Motion correspondence problem
  - Do two measurements at different times originate from the same object?
- Why is it hard?

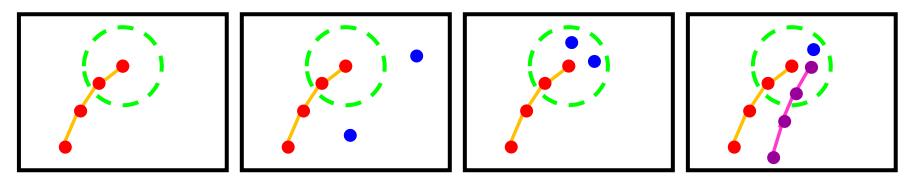
- First make predictions for the expected locations of the current set of objects
- Match predictions to actual measurements
- This is where ambiguities may arise...







# Motion Correspondence Ambiguities



- 1. Predictions may not be supported by measurements
  - Have the objects ceased to exist, or are they simply occluded?
- 2. There may be unexpected measurements
  - Newly visible objects, or just noise?
- 3. More than one measurement may match a prediction
  - Which measurement is the correct one (what about the others)?
- 4. A measurement may match to multiple predictions
  - Which object shall the measurement be assigned to?

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# **Topics of This Lecture**

- Multi-Object Tracking
  - Motivation
  - Ambiguities
- Simple Approaches
  - Gating
  - Mahalanobis distance
  - Nearest-Neighbor Filter
- Track-Splitting Filter
  - Derivation
  - Properties
- Outlook







#### Let's Formalize This

- Multi-Object Tracking problem
  - We represent a track by a state vector  $\mathbf{x}$ , e.g.,

$$\mathbf{x} = [x, y, v_x, v_y]^T$$

– As the track evolves, we denote its state by the time index k:

$$\mathbf{x}^{(k)} = \left[ x^{(k)}, y^{(k)}, v_x^{(k)}, v_y^{(k)} \right]$$

- At each time step, we get a set of observations (measurements)

$$\mathbf{Y}^{(k)} = \left\{ \mathbf{y}_1^{(k)}, \dots, \mathbf{y}_{M_k}^{(k)} 
ight\}$$

- We now need to make the data association between tracks

$$\begin{cases} \mathbf{x}_{1}^{(k)}, \dots, \mathbf{x}_{N_{k}}^{(k)} \end{cases} \text{ and observations } \begin{cases} \mathbf{y}_{1}^{(k)}, \dots, \mathbf{y}_{M_{k}}^{(k)} \end{cases} \text{:} \\ z_{l}^{(k)} = j \text{ iff } \mathbf{y}_{j}^{(k)} \text{ is associated with } \mathbf{x}_{l}^{(k)} \end{cases}$$

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# Reducing Ambiguities: Simple Approaches

- Gating
  - Only consider measurements within a certain area around the predicted location.
  - $\Rightarrow$  Large gain in efficiency, since only a small region needs to be searched
- Nearest-Neighbor Filter
  - Among the candidates in the gating region, only take the one closest to the prediction  $\mathbf{x}_p$

$$z_l^{(k)} = rgmin_j (\mathbf{x}_{p,l}^{(k)} - \mathbf{y}_j^{(k)})^T (\mathbf{x}_{p,l}^{(k)} - \mathbf{y}_j^{(k)})^T$$

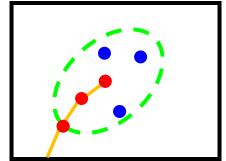
- Better: the one most likely under a Gaussian prediction model

$$z_l^{(k)} = \operatorname{arg\,max}_j \mathcal{N}(\mathbf{y}_j^{(k)}; \mathbf{x}_{p,l}^{(k)}, \mathbf{\Sigma}_{p,l}^{(k)})$$

which is equivalent to taking the Mahalanobis distance

$$z_l = \arg \min_j (\mathbf{x}_{p,l} - \mathbf{y}_j)^T \mathbf{\Sigma}_{p,l}^{-1} (\mathbf{x}_{p,l} - \mathbf{y}_j)$$

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### Gating with Mahalanobis Distance

- Recall: Kalman filter
  - Provides exactly the quantities necessary to perform this
  - Predicted mean location  $\mathbf{x}_p$
  - Prediction covariance  $\Sigma_p$
  - The Kalman filter prediction covariance also defines a useful gating area.
  - $\Rightarrow$  E.g., choose the gating area size such that 95% of the probability mass is covered.
- Side note

- The Mahalanobis distance is  $\chi^2$  distributed with the number of degrees of freedom  $n_z$  equal to the dimension of  $\mathbf{x}$ .
- For a given probability bound, the corresponding threshold on the Mahalanobis distance can be obtained from  $\chi^2$  distribution tables.



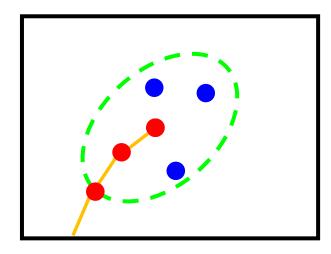


#### Mahalanobis Distance

- Additional notation
  - Our KF state of track  $\mathbf{x}_l$  is given by

the prediction  $\hat{\mathbf{x}}_{l}^{(k)}$  and covariance  $\boldsymbol{\Sigma}_{p,l}^{(k)}$ .

- We define the innovation that measurement  $\mathbf{y}_j$  brings to track  $\mathbf{x}_l$  at time k as  $\mathbf{v}_{j,l}^{(k)} = (\mathbf{y}_j^{(k)} - \mathbf{x}_{p,l}^{(k)})$ 



- With this, we can write the observation likelihood shortly as

$$p(\mathbf{y}_{j}^{(k)}|\mathbf{x}_{l}^{(k)}) \sim \exp\left\{-\frac{1}{2}\mathbf{v}_{j,l}^{(k)^{T}}\boldsymbol{\Sigma}_{p,l}^{(k)^{-1}}\mathbf{v}_{j,l}^{(k)}\right\}$$

- We define the ellipsoidal gating or validation volume as

$$V^{(k)}(\gamma) = \left\{ \mathbf{y} | (\mathbf{y} - \mathbf{x}_{p,l}^{(k)})^T \mathbf{\Sigma}_{p,l}^{(k)^{-1}} (\mathbf{y} - \mathbf{x}_{p,l}^{(k)}) \le \gamma \right\}$$

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## **Problems with NN Assignment**

- Limitations
  - For NN assignments, there is always a finite chance that the association is incorrect, which can lead to serious effects.
  - ⇒ If a Kalman filter is used, a misassigned measurement may lead the filter to lose track of its target.
  - The NN filter makes assignment decisions only based on the current frame.
  - More information is available by examining subsequent images.
  - $\Rightarrow$  Let's make use of this information by postponing the decision process until a future frame will resolve the ambiguity...





# **Topics of This Lecture**

- Multi-Object Tracking
  - Motivation
  - Ambiguities
- Simple Approaches
  - Gating
  - Mahalanobis distance
  - Nearest-Neighbor Filter
- Track-Splitting Filter
  - Derivation
  - Properties
- Outlook



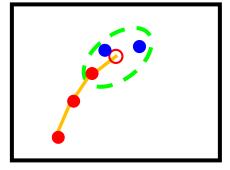


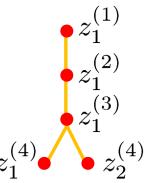


# **Track-Splitting Filter**

Idea

- Problem with NN filter was hard assignment.
- Rather than arbitrarily assigning the closest measurement, form a tree.
- Branches denote alternate assignments.
- No assignment decision is made at this stage!
- ⇒ Decisions are postponed until additional measurements have been gathered...
- Potential problems?
  - Track trees can quickly become very large due to combinatorial explosion.
  - $\Rightarrow$  We need some measure of the likelihood of a track, so that we can prune the tree!





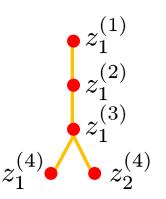




#### **Track Likelihoods**

- Expressing track likelihoods
  - Given a track l, denote by  $\theta_{k,l}$  the event that the sequence of assignments

$$Z_{k,l} = \left\{ z_{i_1,l}^{(1)}, \dots, z_{i_k,l}^{(k)} \right\}$$



from time 1 to k originate from the same object.

- The likelihood of  $\theta_{k,l}$  is the joint probability over all observations in the track k $L(\theta_{k,l}) = \prod p(z_{i_{j},l}^{(j)} | Z_{(j-1),l}, \theta_{k,l})$ j=1
- If we assume Gaussian observation likelihoods, this becomes

$$L(\theta_{k,l}) = \prod_{\substack{j=1\\j=1}}^{k} \frac{1}{(2\pi)^{\frac{d}{2}} |\mathbf{\Sigma}_{l}^{(j)}|^{\frac{1}{2}}} \exp \left[ -\frac{1}{2} \sum_{\substack{j=1\\j=1}}^{k} \mathbf{v}_{i_{j},l}^{(j)^{T}} \mathbf{\Sigma}_{l}^{(j)^{-1}} \mathbf{v}_{i_{j},l}^{(j)} \right]$$
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#### Track Likelihoods (2)

Starting from the likelihood

$$L(\theta_{k,l}) = \prod_{j=1}^{k} \frac{1}{(2\pi)^{\frac{d}{2}} |\mathbf{\Sigma}_{l}^{(j)}|^{\frac{1}{2}}} \exp\left[-\frac{1}{2} \sum_{j=1}^{k} \mathbf{v}_{i_{j},l}^{(j)^{T}} \mathbf{\Sigma}_{l}^{(j)^{-1}} \mathbf{v}_{i_{j},l}^{(j)}\right]$$

– Define the modified log-likelihood  $\lambda_l$  for track l as

$$\begin{aligned} \lambda_{l}(k) &= -2 \log \left[ \frac{L(\theta_{k,l})}{\prod_{j=1}^{k} (2\pi)^{-\frac{d}{2}} |\mathbf{\Sigma}_{l}^{(j)}|^{-\frac{1}{2}}} \right] \\ &= \sum_{j=1}^{k} \mathbf{v}_{i_{j},l}^{(j)^{T}} \mathbf{\Sigma}_{l}^{(j)^{-1}} \mathbf{v}_{i_{j},l}^{(j)} \\ &= \lambda_{l}(k-1) + \mathbf{v}_{i_{k},l}^{(k)^{T}} \mathbf{\Sigma}_{l}^{(k)^{-1}} \mathbf{v}_{i_{k},l}^{(k)} \end{aligned}$$

 $\Rightarrow$  Recursive calculation, sum of Mahalanobis distances of all the measurements assigned to track l.

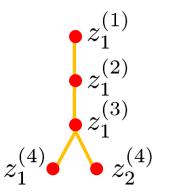
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# **Track-Splitting Filter**

- Effect
  - Instead of assigning the measurement that is currently closest, as in the NN algorithm, we can select the sequence of measurements that minimizes the total Mahalanobis distance over some interval!



- Modified log-likelihood provides the merit of a particular node in the track tree.
- Cost of calculating this is low, since most terms are needed anyway for the Kalman filter.

#### Problem

 The track tree grows exponentially, may generate a very large number of possible tracks that need to be maintained.







# **Pruning Strategies**

- In order to keep this feasible, need to apply pruning
  - Deleting unlikely tracks
    - May be accomplished by comparing the modified log-likelihood  $\lambda(k)$ , which has a  $\chi^2$  distribution with  $kn_z$  degrees of freedom, with a threshold  $\alpha$  (set according to  $\chi^2$  distribution tables).
    - Problem for long tracks: modified log-likelihood gets dominated by old terms and responds very slowly to new ones.
    - $\Rightarrow$  Use sliding window or exponential decay term.
  - Merging track nodes
    - If the state estimates of two track nodes are similar, merge them.
    - E.g., if both tracks validate identical subsequent measurements.
  - Only keeping the most likely  $N \, {\rm tracks}$ 
    - Rank tracks based on their modified log-likelihood.







# Summary: Track-Splitting Filter

- Properties
  - Very old algorithm
    - P. Smith, G. Buechler, A Branching Algorithm for Discriminating and Tracking Multiple Objects, IEEE Trans. Automatic Control, Vol. 20, pp. 101-104, 1975.
  - Improvement over NN assignment.
  - Assignment decisions are delayed until more information is available.
- Many problems remain
  - Exponential complexity, heuristic pruning needed.
  - Merging of track nodes is necessary, because tracks may share measurements, which is physically unrealistic.
- ⇒ Would need to add exclusion constraints such that each measurement may only belong to a single track.
- $\Rightarrow$  Impossible in this framework...







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# Outlook for the Next Lectures

- More powerful approaches
  - Multi-Hypothesis Tracking (MHT)
    - Well-suited for KF, EKF approaches

[Reid, 1979]

- Joint Probabilistic Data Association Filters (JPDAF)
  - Well-suited for Particle Filter based approaches

[Fortmann, 1983]

- Data association as convex optimization problem
  - Bipartite Graph Matching (Hungarian algorithm)
  - Network Flow Optimization
  - $\Rightarrow$  Efficient, globally optimal solutions for subclass of problems.





#### **References and Further Reading**

- A good tutorial on Data Association
  - I.J. Cox. <u>A Review of Statistical Data Association Techniques for</u> <u>Motion Correspondence</u>. In *International Journal of Computer Vision*, Vol. 10(1), pp. 53-66, 1993.



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