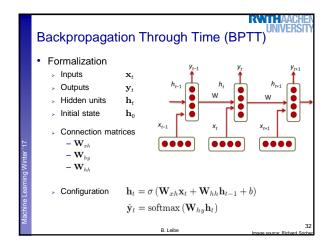
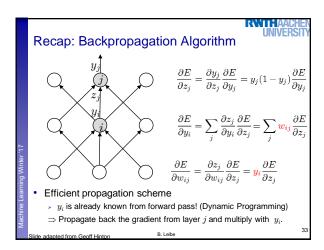
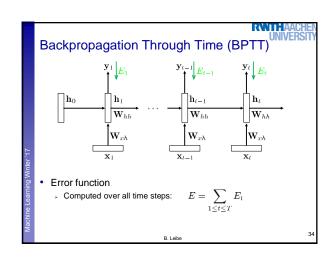
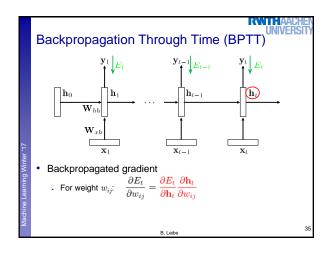


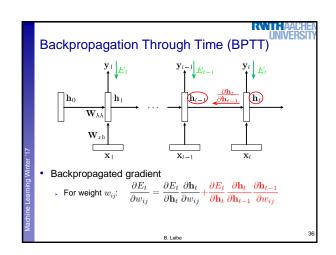
Backpropagation with Weight Constraints • It is easy to modify the backprop algorithm to incorporate linear weight constraints • To constrain $w_1 = w_2$, we start with the same initialization and then make sure that the gradients are the same: $\nabla w_1 = \nabla w_2$ • We compute the gradients as usual and then use $\frac{\partial E}{\partial w_1} + \frac{\partial E}{\partial w_2}$ for both w_1 and w_2 .

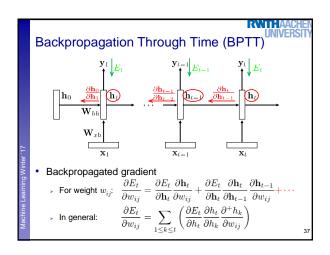


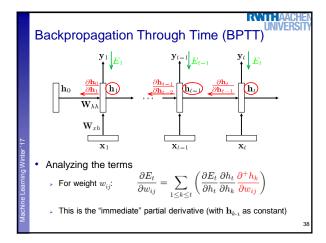


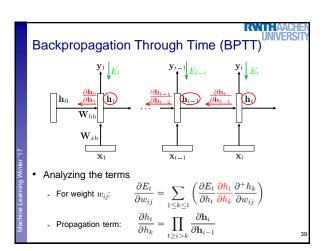


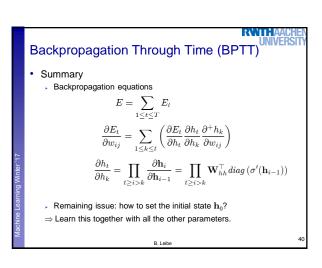


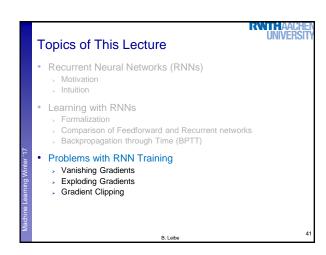


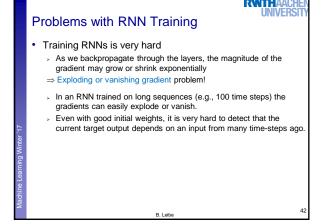












RWTHAACH UNIVERSI

Exploding / Vanishing Gradient Problem

· Consider the propagation equations:

$$\begin{split} \frac{\partial E_t}{\partial w_{ij}} &= \sum_{1 \leq k \leq t} \left(\frac{\partial E_t}{\partial h_t} \frac{\partial h_t}{\partial h_k} \frac{\partial^+ h_k}{\partial w_{ij}} \right) \\ \frac{\partial h_t}{\partial h_k} &= \prod_{t \geq i > k} \frac{\partial \mathbf{h}_i}{\partial \mathbf{h}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{hh}^\top diag\left(\sigma'(\mathbf{h}_{i-1})\right) \\ &= \left(\mathbf{W}_{hh}^\top\right)^l \end{split}$$

- \rightarrow if t goes to infinity and l=t-k.
- ⇒ We are effectively taking the weight matrix to a high power.
- \triangleright The result will depend on the eigenvalues of \mathbf{W}_{hh} .
 - Largest eigenvalue > 1 ⇒ Gradients may explode.
 - Largest eigenvalue < 1 ⇒ Gradients will vanish.
 - This is very bad...

R Leibe

Why Is This Bad?

- Vanishing gradients in language modeling
 - Words from time steps far away are not taken into consideration when training to predict the next word.
- · Example:
 - » "Jane walked into the room. John walked in too. It was late in the day. Jane said hi to _____"
 - ⇒ The RNN will have a hard time learning such long-range dependencies.

Slide adapted from Richard Socher

R Laiba

