

Machine Learning – Lecture 16

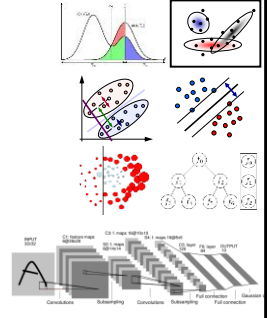
Convolutional Neural Networks II

18.12.2017

Bastian Leibe
 RWTH Aachen
<http://www.vision.rwth-aachen.de>
 leibe@vision.rwth-aachen.de

Course Outline

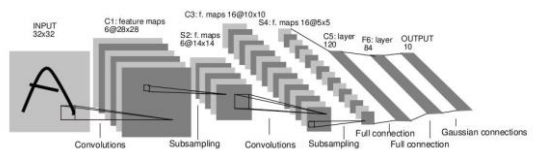
- Fundamentals
 - Bayes Decision Theory
 - Probability Density Estimation
- Classification Approaches
 - Linear Discriminants
 - Support Vector Machines
 - Ensemble Methods & Boosting
 - Random Forests
- Deep Learning
 - Foundations
 - Convolutional Neural Networks
 - Recurrent Neural Networks



Topics of This Lecture

- Recap: CNNs
- CNN Architectures
 - LeNet
 - AlexNet
 - VGGNet
 - GoogLeNet
 - ResNets
- Visualizing CNNs
 - Visualizing CNN features
 - Visualizing responses
 - Visualizing learned structures
- Applications

Recap: Convolutional Neural Networks

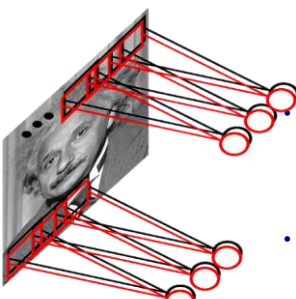


- Neural network with specialized connectivity structure
 - Stack multiple stages of feature extractors
 - Higher stages compute more global, more invariant features
 - Classification layer at the end

Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, [Gradient-based learning applied to document recognition](#), Proceedings of the IEEE 86(11): 2278–2324, 1998.

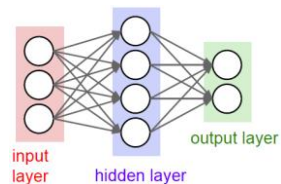
Recap: Intuition of CNNs

- Convolutional net
 - Share the same parameters across different locations
 - Convolutions with learned kernels
- Learn *multiple* filters
 - E.g. 1000x1000 image
 - 100 filters
 - 10x10 filter size
 - ⇒ only 10k parameters
- Result: Response map
 - size: 1000x1000x100
 - Only memory, not params!

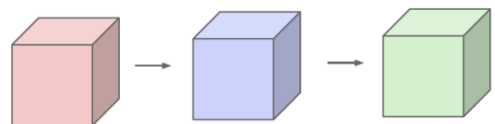


Important Conceptual Shift

- Before



- Now:



Machine Learning Winter '17

Convolution Layers

Example image: $32 \times 32 \times 3$ volume

Before: Full connectivity
 $32 \times 32 \times 3$ weights

Now: Local connectivity
One neuron connects to, e.g., $5 \times 5 \times 3$ region.
⇒ Only $5 \times 5 \times 3$ shared weights.

- Note: Connectivity is
 - Local in space (5×5 inside 32×32)
 - But full in depth (all 3 depth channels)

Slide adapted from FeiFei Li, Andrei Karpathy. B. Leibe

10

Machine Learning Winter '17

Convolution Layers

before: "hidden layer of 200 neurons"
now: "output volume of depth 200"

- All Neural Net activations arranged in 3 dimensions
 - Multiple neurons all looking at the same input region, stacked in depth

Slide adapted from FeiFei Li, Andrei Karpathy. B. Leibe

11

Machine Learning Winter '17

Convolution Layers

Naming convention:

- All Neural Net activations arranged in 3 dimensions
 - Multiple neurons all looking at the same input region, stacked in depth
 - Form a single $[1 \times 1 \times \text{depth}]$ depth column in output volume.

Slide credit: FeiFei Li, Andrei Karpathy. B. Leibe

12

Machine Learning Winter '17

Convolution Layers

Example:
 7×7 input
assume 3×3 connectivity
stride 1

- Replicate this column of hidden neurons across space, with some **stride**.

Slide credit: FeiFei Li, Andrei Karpathy. B. Leibe

14

Machine Learning Winter '17

Convolution Layers

Example:
 7×7 input
assume 3×3 connectivity
stride 1

- Replicate this column of hidden neurons across space, with some **stride**.

Slide credit: FeiFei Li, Andrei Karpathy. B. Leibe

15

Machine Learning Winter '17

Convolution Layers

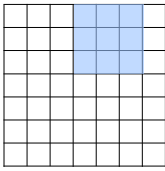
Example:
 7×7 input
assume 3×3 connectivity
stride 1

- Replicate this column of hidden neurons across space, with some **stride**.

Slide credit: FeiFei Li, Andrei Karpathy. B. Leibe

16

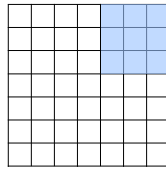
Convolution Layers



Example:
 7×7 input
 assume 3×3 connectivity
 stride 1

- Replicate this column of hidden neurons across space, with some **stride**.

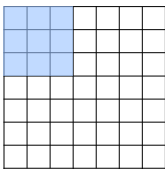
Convolution Layers



Example:
 7×7 input
 assume 3×3 connectivity
 stride 1
 $\Rightarrow 5 \times 5$ output

- Replicate this column of hidden neurons across space, with some **stride**.

Convolution Layers

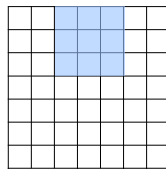


Example:
 7×7 input
 assume 3×3 connectivity
 stride 1
 $\Rightarrow 5 \times 5$ output

What about stride 2?

- Replicate this column of hidden neurons across space, with some **stride**.

Convolution Layers

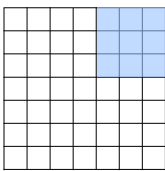


Example:
 7×7 input
 assume 3×3 connectivity
 stride 1
 $\Rightarrow 5 \times 5$ output

What about stride 2?

- Replicate this column of hidden neurons across space, with some **stride**.

Convolution Layers



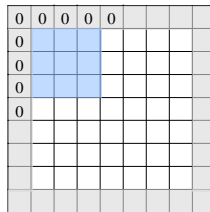
Example:
 7×7 input
 assume 3×3 connectivity
 stride 1
 $\Rightarrow 5 \times 5$ output

What about stride 2?

$\Rightarrow 3 \times 3$ output

- Replicate this column of hidden neurons across space, with some **stride**.

Convolution Layers



Example:
 7×7 input
 assume 3×3 connectivity
 stride 1
 $\Rightarrow 5 \times 5$ output

What about stride 2?

$\Rightarrow 3 \times 3$ output

- Replicate this column of hidden neurons across space, with some **stride**.
- In practice, common to zero-pad the border.
 - Preserves the size of the input spatially.

RWTH AACHEN UNIVERSITY

Activation Maps of Convolutional Filters

Activations: one filter = one depth slice (or activation map) 5x5 filters

Activations:

Each activation map is a depth slice through the output volume.

Activation maps

Machine Learning Winter '17 23

Slide adapted from FeiFei Li, Andrei Karpathy, B. Leibe

RWTH AACHEN UNIVERSITY

Effect of Multiple Convolution Layers

Low-Level Feature → Mid-Level Feature → High-Level Feature → Trainable Classifier

Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

Machine Learning Winter '17 24

Slide credit: Yann LeCun, B. Leibe

RWTH AACHEN UNIVERSITY

Convolutional Networks: Intuition

- Let's assume the filter is an eye detector
 - How can we make the detection robust to the exact location of the eye?

Machine Learning Winter '17 25

Slide adapted from Marc'Aurelio Ranzato, B. Leibe, Image source: Yann LeCun

RWTH AACHEN UNIVERSITY

Convolutional Networks: Intuition

- Let's assume the filter is an eye detector
 - How can we make the detection robust to the exact location of the eye?
- Solution:
 - By **pooling** (e.g., max or avg) filter responses at different spatial locations, we gain robustness to the exact spatial location of features.

Machine Learning Winter '17 26

Slide adapted from Marc'Aurelio Ranzato, B. Leibe, Image source: Yann LeCun

RWTH AACHEN UNIVERSITY

Max Pooling

Single depth slice

1	1	2	4
5	6	7	8
3	2	1	0
1	2	3	4

max pool with 2x2 filters and stride 2

6	8
3	4

Effect:

- Make the representation smaller without losing too much information
- Achieve robustness to translations

Machine Learning Winter '17 27

Slide adapted from FeiFei Li, Andrei Karpathy, B. Leibe

RWTH AACHEN UNIVERSITY

Max Pooling

Single depth slice

1	1	2	4
5	6	7	8
3	2	1	0
1	2	3	4

max pool with 2x2 filters and stride 2

6	8
3	4

Note

- Pooling happens independently across each slice, preserving the number of slices.

Machine Learning Winter '17 28

Slide adapted from FeiFei Li, Andrei Karpathy, B. Leibe

RWTH AACHEN UNIVERSITY

CNNs: Implication for Back-Propagation

- Convolutional layers
 - Filter weights are shared between locations
 - ⇒ Gradients are added for each filter location.

B. Leibe 29

RWTH AACHEN UNIVERSITY

Topics of This Lecture

- Recap: CNNs
- CNN Architectures
 - LeNet
 - AlexNet
 - VGGNet
 - GoogLeNet
- Visualizing CNNs
 - Visualizing CNN features
 - Visualizing responses
 - Visualizing learned structures
- Applications

B. Leibe 30

RWTH AACHEN UNIVERSITY

CNN Architectures: LeNet (1998)

- Early convolutional architecture
 - 2 Convolutional layers, 2 pooling layers
 - Fully-connected NN layers for classification
 - Successfully used for handwritten digit recognition (MNIST)

Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, [Gradient-based learning applied to document recognition](#), Proceedings of the IEEE 86(11): 2278–2324, 1998.

B. Leibe 31

RWTH AACHEN UNIVERSITY

ImageNet Challenge 2012

- ImageNet
 - ~14M labeled internet images
 - 20k classes
 - Human labels via Amazon Mechanical Turk
- Challenge (ILSVRC)
 - 1.2 million training images
 - 1000 classes
 - Goal: Predict ground-truth class within top-5 responses
 - Currently one of the top benchmarks in Computer Vision

[Deng et al., CVPR'09]

B. Leibe 32

RWTH AACHEN UNIVERSITY

CNN Architectures: AlexNet (2012)

- Similar framework as LeNet, but
 - Bigger model (7 hidden layers, 650k units, 60M parameters)
 - More data (10^6 images instead of 10^3)
 - GPU implementation
 - Better regularization and up-to-date tricks for training (Dropout)

A. Krizhevsky, I. Sutskever, and G. Hinton, [ImageNet Classification with Deep Convolutional Neural Networks](#), NIPS 2012.

B. Leibe 33

RWTH AACHEN UNIVERSITY

ILSVRC 2012 Results

Team	Top-5 error rate (%)
SuperVision	~16.4
ISI	~26.2
Oxford	~26.2
INRIA	~26.2
Amsterdam	~26.2

- AlexNet almost halved the error rate
 - 16.4% error (top-5) vs. 26.2% for the next best approach
 - ⇒ A revolution in Computer Vision
 - Acquired by Google in Jan '13, deployed in Google+ in May '13

B. Leibe 34

Machine Learning Winter '17

CNN Architectures: VGGNet (2014/15)

Input : Image input
 Conv : Convolutional layer
 Pool : Max-pooling layer
 FC : Fully-connected layer
 Softmax : Softmax layer

AlexNet
 Layer1
 Layer2
 Layer3
 Layer4
 Layer5
 Layer6
 Layer7

VGGNet
 Layer1
 Layer2
 Layer3
 Layer4
 Layer5
 Layer6
 Layer7

K. Simonyan, A. Zisserman, [Very Deep Convolutional Networks for Large-Scale Image Recognition](#), ICLR 2015

B. Leibe 36
 Image source: Hirakatsu Katoka

Machine Learning Winter '17

CNN Architectures: VGGNet (2014/15)

- Main ideas
 - Deeper network
 - Stacked convolutional layers with smaller filters (+ nonlinearity)
 - Detailed evaluation of all components
- Results
 - Improved ILSVRC top-5 error rate to 6.7%.

A	A-LRN	B	C	D	E
11 weight layers	11 weight layers	13 weight layers	16 weight layers	16 weight layers	19 weight layers
conv-3-64	conv-3-64 LRN	conv-3-64 input (224 x 224 RGB image)	conv-3-64 conv-3-64	conv-3-64 conv-3-64	conv-3-64 conv-3-64
conv-3-128	conv-3-128	conv-3-128 conv-3-128	conv-3-128 conv-3-128	conv-3-128 conv-3-128	conv-3-128 conv-3-128
conv-3-256 conv-3-256	conv-3-256 conv-3-256	conv-3-256 conv-3-256	conv-3-256 conv-3-256 conv-3-256	conv-3-256 conv-3-256 conv-3-256	conv-3-256 conv-3-256 conv-3-256
conv-3-512 conv-3-512	conv-3-512 conv-3-512	conv-3-512 conv-3-512	conv-3-512 conv-3-512 conv-1-512	conv-3-512 conv-3-512 conv-3-512	conv-3-512 conv-3-512 conv-3-512 conv-3-512
conv-3-512 conv-3-512	conv-3-512 conv-3-512	conv-3-512 conv-3-512	conv-3-512 conv-3-512 conv-1-512	conv-3-512 conv-3-512 conv-3-512	conv-3-512 conv-3-512 conv-3-512 conv-3-512
			maxpool		
			FC-4096		
			FC-4096		
			FC-1000		
			soft-max		

B. Leibe 37
 Image source: Simonyan & Zisserman

Machine Learning Winter '17

Comparison: AlexNet vs. VGGNet

- Receptive fields in the first layer
 - AlexNet: 11x11, stride 4
 - Zeiler & Fergus: 7x7, stride 2
 - VGGNet: 3x3, stride 1
- Why that?
 - If you stack a 3x3 on top of another 3x3 layer, you effectively get a 5x5 receptive field.
 - With three 3x3 layers, the receptive field is already 7x7.
 - But much fewer parameters: 3·3² = 27 instead of 7² = 49.
 - In addition, non-linearities in-between 3x3 layers for additional discriminativity.

B. Leibe 38

Machine Learning Winter '17

CNN Architectures: GoogLeNet (2014/2015)

(a) Inception module, naive version
 (b) Inception module with dimension reductions

- Main ideas
 - "Inception" module as modular component
 - Learns filters at several scales within each module

C. Szegedy, W. Liu, Y. Jia, et al, [Going Deeper with Convolutions](#), arXiv:1409.4842, 2014, CVPR'15, 2015.

B. Leibe 39

Machine Learning Winter '17

GoogLeNet Visualization

Inception module + copies

Auxiliary classification outputs for training the lower layers (deprecated)

Convolution
 Pooling
 Softmax
 Other

B. Leibe 40

Machine Learning Winter '17

Results on ILSVRC

Method	top-1 val. error (%)	top-5 val. error (%)	top-5 test error (%)
VGG (2 nets, multi-crop & dense eval.)	23.7	6.8	6.8
VGG (1 net, multi-crop & dense eval.)	24.4	7.1	7.0
VGG (ILSVRC submission, 7 nets, dense eval.)	24.7	7.5	7.3
GoogLeNet (Szegedy et al., 2014) (1 net)	-	-	7.9
GoogLeNet (Szegedy et al., 2014) (7 nets)	-	-	6.7
MSRA (He et al., 2014) (11 nets)	-	-	8.1
MSRA (He et al., 2014) (1 net)	27.9	9.1	9.1
Clarifai (Russakovsky et al., 2014) (multiple nets)	-	-	11.7
Clarifai (Russakovsky et al., 2014) (1 net)	-	-	12.5
Zeiler & Fergus (Zeiler & Fergus, 2013) (6 nets)	36.0	14.7	14.8
Zeiler & Fergus (Zeiler & Fergus, 2013) (1 net)	37.5	16.0	16.1
OverFeat (Sermanet et al., 2014) (7 nets)	34.0	13.2	13.6
OverFeat (Sermanet et al., 2014) (1 net)	35.7	14.2	-
Krizhevsky et al. (Krizhevsky et al., 2012) (5 nets)	38.1	16.4	16.4
Krizhevsky et al. (Krizhevsky et al., 2012) (1 net)	40.7	18.2	-

- VGGNet and GoogLeNet perform at similar level
 - Comparison: human performance ~5% [Karpathy]

<http://karpathy.github.io/2014/09/02/what-i-learned-from-competing-against-a-convnet-on-imagenet/>

B. Leibe 41
 Image source: Simonyan & Zisserman

Newer Developments: Residual Networks

AlexNet, 8 layers (ILSVRC 2012)

VGG, 19 layers (ILSVRC 2014)

GoogleNet, 22 layers (ILSVRC 2014)

B. Leibe

42

Newer Developments: Residual Networks

AlexNet, 8 layers (ILSVRC 2012)

VGG, 19 layers (ILSVRC 2014)

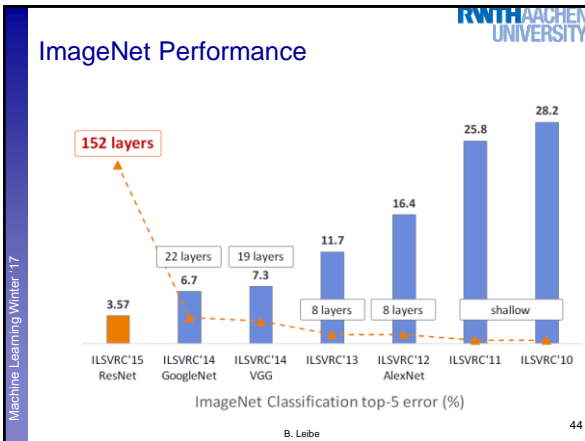
ResNet, 152 layers (ILSVRC 2015)

- Core component
 - Skip connections bypassing each layer
 - Better propagation of gradients to the deeper layers
 - We'll analyze this mechanism in more detail later...

$$H(x) = F(x) + x$$

B. Leibe

43



Understanding the ILSVRC Challenge

- Imagine the scope of the problem!
 - 1000 categories
 - 1.2M training images
 - 50k validation images
- This means...
 - Speaking out the list of category names at 1 word/s...
 - ...takes 15mins.
 - Watching a slideshow of the validation images at 2s/image...
 - ...takes a full day (24h+).
 - Watching a slideshow of the training images at 2s/image...
 - ...takes a full month.

B. Leibe

45

More Finegrained Classes

B. Leibe

46

More Finegrained Classes

B. Leibe

47

Quirks and Limitations of the Data Set

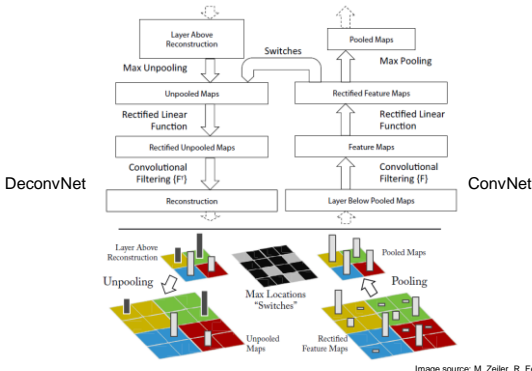


- Generated from WordNet ontology
 - Some animal categories are overrepresented
 - E.g., 120 subcategories of dog breeds
- ⇒ 6.7% top-5 error looks all the more impressive

Topics of This Lecture

- Recap: CNNs
- CNN Architectures
 - LeNet
 - AlexNet
 - VGGNet
 - GoogLeNet
- Visualizing CNNs
 - Visualizing CNN features
 - Visualizing responses
 - Visualizing learned structures
- Applications

Visualizing CNNs



Visualizing CNNs

reconstruction of image patches from that unit (indicates aspect of patches which unit is sensitive to)

top 9 image patches that cause maximal activation in layer 2 unit

M. Zeiler, R. Fergus, *Visualizing and Understanding Convolutional Neural Networks*, ECCV 2014.

Slide credit: Richard Turner


Visualizing CNNs

Visualizing CNNs

Machine Learning Winter '17

What Does the Network React To?

- Occlusion Experiment
 - Mask part of the image with an occluding square.
 - Monitor the output




B. Leibe

54

Machine Learning Winter '17

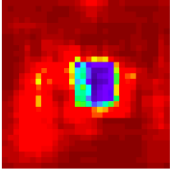
What Does the Network React To?

Input image

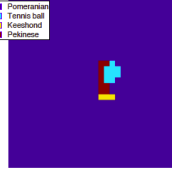


True Label: Pomeranian

p(True class)



Most probable class



Pomeranian
 Tennis ball
 Keeshond
 Pukinese

Slide credit: Svetlana Lazebnik, Rob Fergus


Image source: M. Zeiler, R. Fergus

55

Machine Learning Winter '17

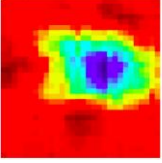
What Does the Network React To?

Input image

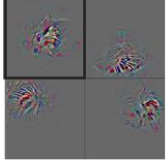


True Label: Pomeranian

Total activation in most active 5th layer feature map



Other activations from the same feature map.



Slide credit: Svetlana Lazebnik, Rob Fergus


Image source: M. Zeiler, R. Fergus

56

Machine Learning Winter '17

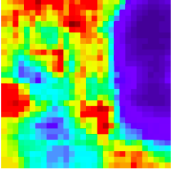
What Does the Network React To?

Input image




True Label: Car Wheel

p(True class)



Most probable class



Car wheel
 Racer
 Cab
 Police van

Slide credit: Svetlana Lazebnik, Rob Fergus


Image source: M. Zeiler, R. Fergus

57

Machine Learning Winter '17

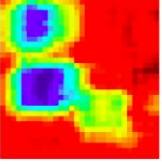
What Does the Network React To?

Input image




True Label: Car Wheel

Total activation in most active 5th layer feature map



Other activations from the same feature map.



Slide credit: Svetlana Lazebnik, Rob Fergus


Image source: M. Zeiler, R. Fergus

58

Machine Learning Winter '17

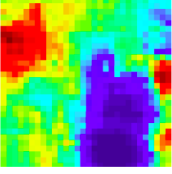
What Does the Network React To?

Input image

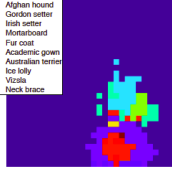


True Label: Afghan Hound

p(True class)



Most probable class



Afghan hound
 Gordon setter
 Irish setter
 Montbard
 Flat coat
 Academic gown
 Australian terrier
 Ice lolly
 Vizsla
 Neck trace

Slide credit: Svetlana Lazebnik, Rob Fergus


Image source: M. Zeiler, R. Fergus

59

Machine Learning Winter '17

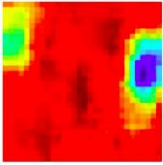
What Does the Network React To?

Input image




True Label: Afghan Hound

Total activation in most active 5th layer feature map



Other activations from the same feature map.

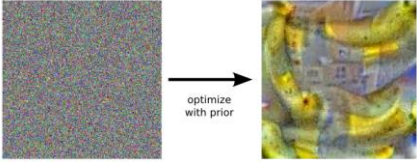


60

Slide credit: Svetlana Lazebnik, Rob Fergus. Image source: M. Zeiler, R. Fergus.

Machine Learning Winter '17

Inceptionism: Dreaming ConvNets



optimize with prior

- Idea
 - Start with a random noise image.
 - Enhance the input image such as to enforce a particular response (e.g., banana).
 - Combine with prior constraint that image should have similar statistics as natural images.

⇒ Network hallucinates characteristics of the learned class.

61

<http://googleresearch.blogspot.de/2015/06/inceptionism-going-deeper-into-neural.html>

Machine Learning Winter '17

Inceptionism: Dreaming ConvNets

- Results



62

<http://googleresearch.blogspot.de/2015/07/deepdream-code-example-for-visualizing.html>

Machine Learning Winter '17

Inceptionism: Dreaming ConvNets



63

<https://www.youtube.com/watch?v=IREsx-xWQ0g>

Machine Learning Winter '17

Topics of This Lecture

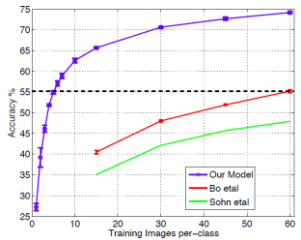
- Recap: CNNs
- CNN Architectures
 - LeNet
 - AlexNet
 - VGGNet
 - GoogLeNet
- Visualizing CNNs
 - Visualizing CNN features
 - Visualizing responses
 - Visualizing learned structures
- Applications

64

B. Leibe

Machine Learning Winter '17

The Learned Features are Generic



state of the art level (pre-CNN)

- Experiment: feature transfer
 - Train network on ImageNet
 - Chop off last layer and train classification layer on CalTech256

⇒ State of the art accuracy already with only 6 training images

65

B. Leibe. Image source: M. Zeiler, R. Fergus.

RWTH AACHEN UNIVERSITY

Other Tasks: Detection

R-CNN: Regions with CNN features

1. Input image
2. Extract region proposals (~2k)
3. Compute CNN features
4. Classify regions

- Results on PASCAL VOC Detection benchmark
 - Pre-CNN state of the art: 35.1% mAP [Uijlings et al., 2013]
 - 33.4% mAP DPM
 - R-CNN: 53.7% mAP

R. Girshick, J. Donahue, T. Darrell, and J. Malik, [Rich Feature Hierarchies for Accurate Object Detection and Semantic Segmentation](#), CVPR 2014

66

RWTH AACHEN UNIVERSITY

Most Recent Version: Faster R-CNN

- One network, four losses
 - Remove dependence on external region proposal algorithm.
 - Instead, infer region proposals from same CNN.
 - Feature sharing
 - Joint training

⇒ Object detection in a single pass becomes possible.
⇒ mAP improved to >70%

Slide credit: Ross Girshick

67

RWTH AACHEN UNIVERSITY

Faster R-CNN (based on ResNets)

K. He, X. Zhang, S. Ren, J. Sun, [Deep Residual Learning for Image Recognition](#), CVPR 2016.

B. Leibe

68

RWTH AACHEN UNIVERSITY

Faster R-CNN (based on ResNets)

K. He, X. Zhang, S. Ren, J. Sun, [Deep Residual Learning for Image Recognition](#), CVPR 2016.

B. Leibe

69

RWTH AACHEN UNIVERSITY

YOLO

J. Redmon, S. Divvala, R. Girshick, A. Farhadi, [You Only Look Once: Unified, Real-Time Object Detection](#), CVPR 2016.

70

RWTH AACHEN UNIVERSITY

Semantic Image Segmentation

- Perform pixel-wise prediction task
 - Usually done using Fully Convolutional Networks (FCNs)
 - All operations formulated as convolutions
 - Advantage: can process arbitrarily sized images

Image source: Long, Shelhamer, Darrell

71

Machine Learning Winter '17

Semantic Image Segmentation

- Encoder-Decoder Architecture
 - Problem: FCN output has low resolution
 - Solution: perform upsampling to get back to desired resolution
 - Use skip connections to preserve higher-resolution information

72
Image source: Newell et al

Machine Learning Winter '17

Semantic Segmentation

[Pohlen, Hermans, Mathias, Leibe, CVPR 2017]

- More recent results
 - Based on an extension of ResNets

Machine Learning Winter '17

Other Tasks: Face Verification

Method	Performance
Human cropped	97.9%
DeepFace-ensemble	97.35%
DeepFace-single	97.00%
TL Joint Bayesian	96.53%
High-dimensional LBP	95.17%
Tom-vs-Pete + Attribute	93.30%
combined Joint Bayesian	92.42%

Y. Taigman, M. Yang, M. Ranzato, L. Wolf, **DeepFace: Closing the Gap to Human-Level Performance in Face Verification**, CVPR 2014

Slide credit: Svetlana Lazebnik

74

Machine Learning Winter '17

Commercial Recognition Services

- E.g., **clarifai**

Try it out with your own media

Upload an image or video file under 100mb or give us a direct link to a file on the web.

Paste a url here... **ENGLISH**

USE THE URL **CHOOSE A FILE INSTEAD**

*By using the demo you agree to our terms of service

- Be careful when taking test images from Google Search
 - Chances are they may have been seen in the training set...

B. Leibe
Image source: clarifai.com

75

Machine Learning Winter '17

Commercial Recognition Services

clarifai

B. Leibe
Image source: clarifai.com

76

Machine Learning Winter '17

References and Further Reading

- LeNet
 - Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, [Gradient-based learning applied to document recognition](#), Proceedings of the IEEE 86(11): 2278–2324, 1998.
- AlexNet
 - A. Krizhevsky, I. Sutskever, and G. Hinton, [ImageNet Classification with Deep Convolutional Neural Networks](#), NIPS 2012.
- VGGNet
 - K. Simonyan, A. Zisserman, [Very Deep Convolutional Networks for Large-Scale Image Recognition](#), ICLR 2015
- GoogLeNet
 - C. Szegedy, W. Liu, Y. Jia, et al, [Going Deeper with Convolutions](#), arXiv:1409.4842, 2014.

B. Leibe

77

References and Further Reading

- ResNet
 - K. He, X. Zhang, S. Ren, J. Sun, [Deep Residual Learning for Image Recognition](#), CVPR 2016.

References

- ReLU
 - X. Glorot, A. Bordes, Y. Bengio, [Deep sparse rectifier neural networks](#), AISTATS 2011.
- Initialization
 - X. Glorot, Y. Bengio, [Understanding the difficulty of training deep feedforward neural networks](#), AISTATS 2010.
 - K. He, X.Y. Zhang, S.Q. Ren, J. Sun, [Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification](#), ArXiv 1502.01852v1, 2015.
 - A.M. Saxe, J.L. McClelland, S. Ganguli, [Exact solutions to the nonlinear dynamics of learning in deep linear neural networks](#), ArXiv 1312.6120v3, 2014.

References and Further Reading

- Batch Normalization
 - S. Ioffe, C. Szegedy, [Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift](#), ArXiv 1502.03167, 2015.
- Dropout
 - N. Srivastava, G. Hinton, A. Krizhevsky, I. Sutskever, R. Salakhutdinov, [Dropout: A Simple Way to Prevent Neural Networks from Overfitting](#), JMLR, Vol. 15:1929-1958, 2014.