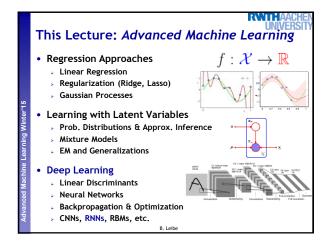
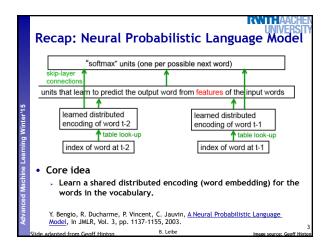
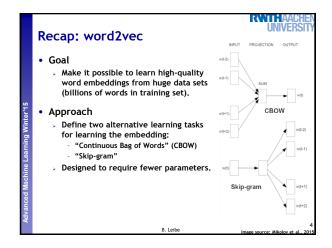
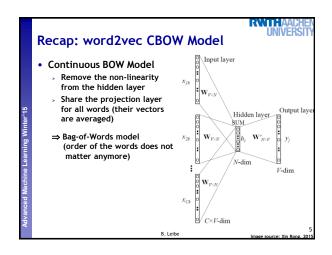
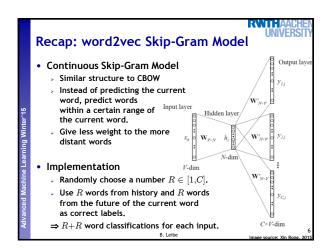
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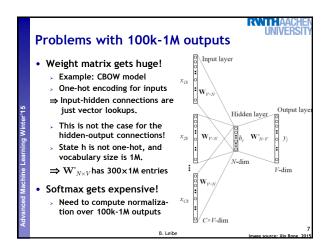


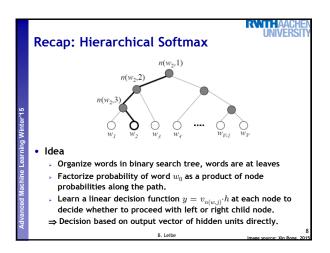


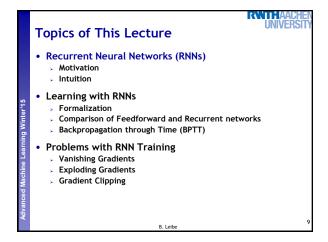


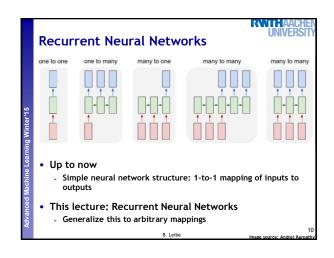


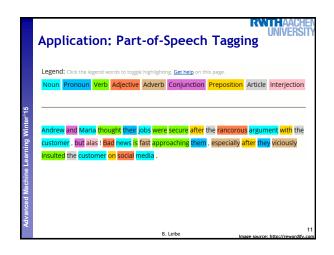


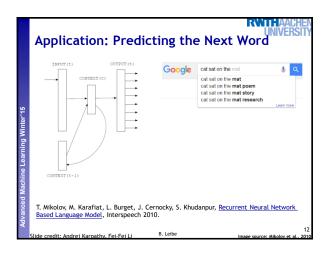


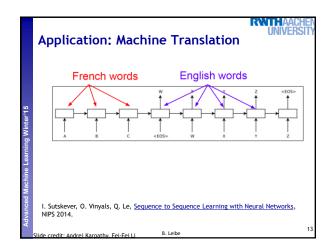


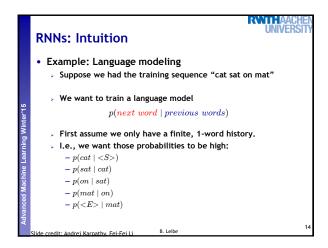


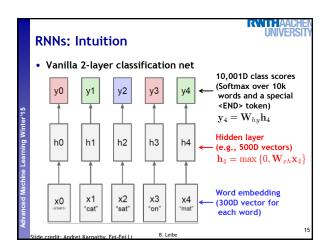


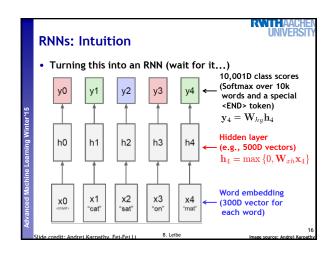


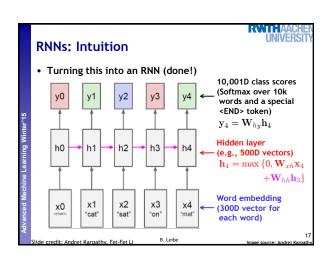


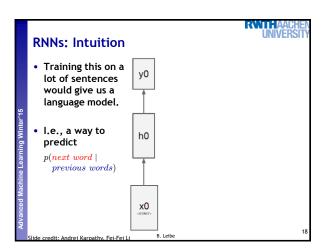


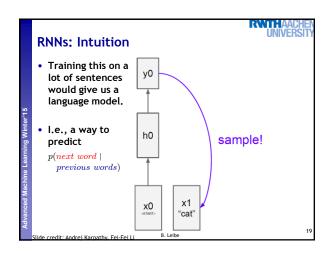


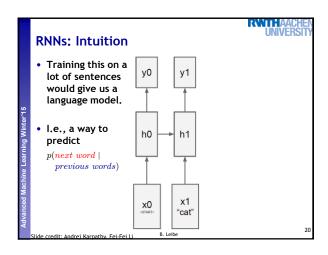


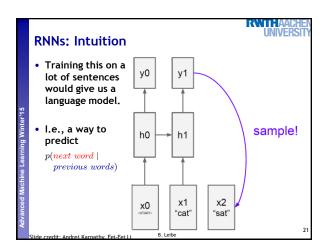


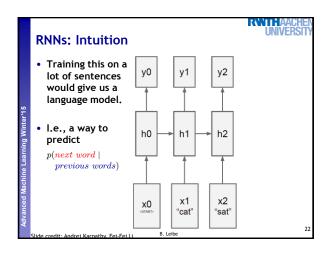


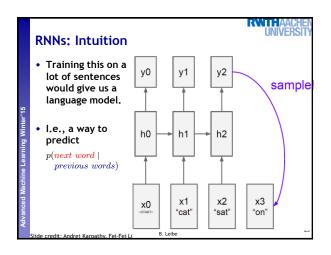


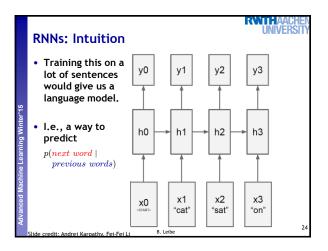


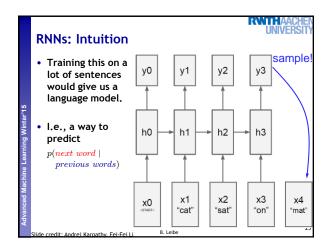


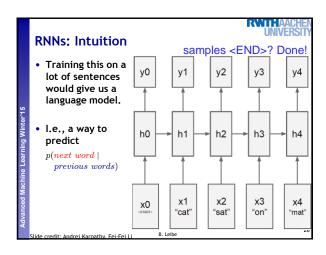


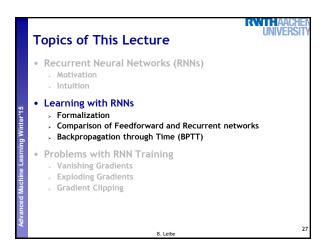


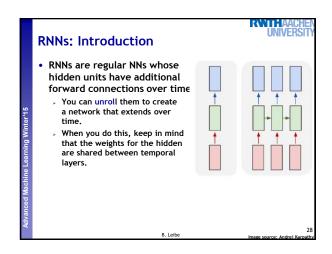


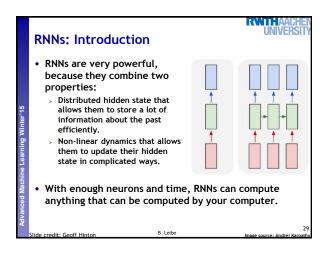


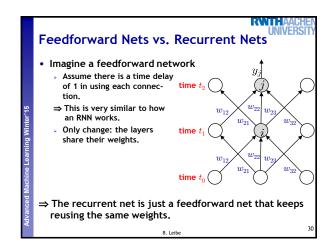












Backpropagation with Weight Constraints

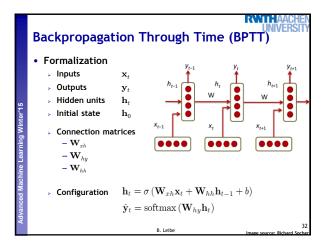
buckpropagation with weight constrain

- It is easy to modify the backprop algorithm to incorporate linear weight constraints
 - . To constrain $w_1=w_2$, we start with the same initialization and then make sure that the gradients are the same: $\nabla w_1=\nabla w_2$
 - > We compute the gradients as usual and then use

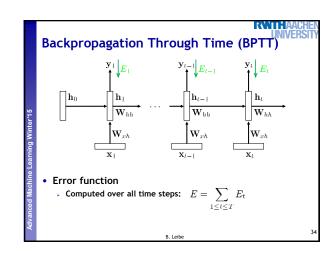
$$\frac{\partial E}{\partial w_1} + \frac{\partial E}{\partial w_2}$$

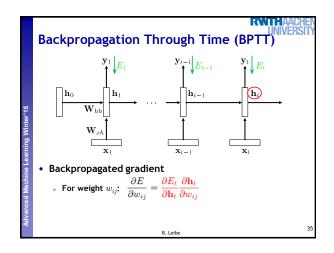
for both w_1 and w_2 .

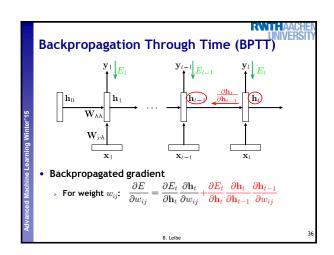
ide adapted from Geoff Hinton B. Leibe

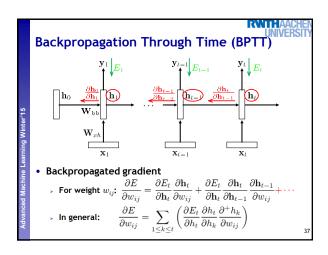


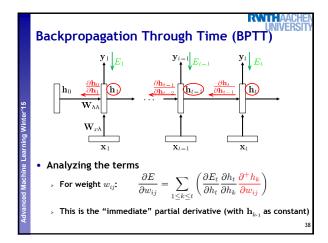
Recap: Backpropagation Algorithm $\frac{\partial E}{\partial z_j} = \frac{\partial y_j}{\partial z_j} \frac{\partial E}{\partial y_j} = y_j (1 - y_j) \frac{\partial E}{\partial y_j}$ $\frac{\partial E}{\partial y_i} = \sum_j \frac{\partial z_j}{\partial y_i} \frac{\partial E}{\partial z_j} = \sum_j w_{ij} \frac{\partial E}{\partial z_j}$ • Efficient propagation scheme $b_i = \sum_j y_i = \sum_j y_i \frac{\partial E}{\partial z_j} = y_i \frac{\partial E}{\partial z_j}$ • Efficient propagation scheme $b_i = \sum_j y_i = \sum_j y_i \frac{\partial E}{\partial z_j} = y_i \frac{\partial E}{\partial z_j}$ • Propagate back the gradient from layer j and multiply with j_i .

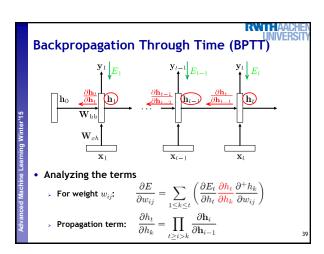


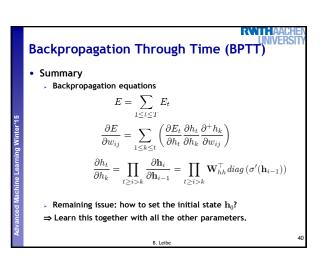




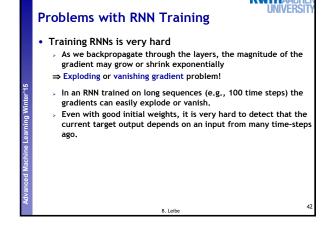








Topics of This Lecture Recurrent Neural Networks (RNNs) Motivation Intuition Learning with RNNs Formalization Comparison of Feedforward and Recurrent networks Backpropagation through Time (BPTT) Problems with RNN Training Vanishing Gradients Exploding Gradients Gradient Clipping



Exploding / Vanishing Gradient Problem

· Consider the propagation equations:

$$\begin{split} \frac{\partial E}{\partial w_{ij}} &= \sum_{1 \leq k \leq t} \left(\frac{\partial E_t}{\partial h_t} \frac{\partial h_t}{\partial h_k} \frac{\partial^+ h_k}{\partial w_{ij}} \right) \\ \frac{\partial h_t}{\partial h_k} &= \prod_{t \geq i > k} \frac{\partial \mathbf{h}_i}{\partial \mathbf{h}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{hh}^\top \operatorname{diag} \left(\sigma'(\mathbf{h}_{i-1}) \right) \\ &= \left. \left(\mathbf{W}_{hh}^\top \right)^l \end{split}$$

- ightarrow if t goes to infinity and l=t-k.
- ⇒ We are effectively taking the weight matrix to a high power.
- ightarrow The result will depend on the eigenvalues of \mathbf{W}_{hh} .
 - Largest eigenvalue > 1 ⇒ Gradients may explode.
 - Largest eigenvalue < 1 ⇒ Gradients will vanish.
 - This is very bad...

Why Is This Bad?

- · Vanishing gradients in language modeling
 - Words from time steps far away are not taken into consideration when training to predict the next word.
- · Example:
 - "Jane walked into the room. John walked in too. It was late in the day. Jane said hi to __
 - \Rightarrow The RNN will have a hard time learning such long-range dependencies.

Gradient Clipping

· Trick to handle exploding gradients

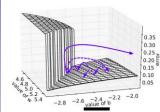
If the gradient is larger than a threshold, clip it to that threshold.

Algorithm 1 Pseudo-code for norm clipping the gradients whenever they explode

$$\begin{array}{c} \hat{\mathbf{g}} \leftarrow \frac{\partial \mathcal{E}}{\partial \theta} \\ \text{if } \quad \|\hat{\mathbf{g}}\| \geq threshold \text{ then} \\ \hat{\mathbf{g}} \leftarrow \frac{threshold}{\|\hat{\mathbf{g}}\|} \hat{\mathbf{g}} \\ \text{end if} \end{array}$$

> This makes a big difference in RNNs

Gradient Clipping Intuition



- Example
 - > Error surface of a single RNN neuron
 - > High curvature walls
 - Solid lines; standard gradient descent trajectories
 - Dashed lines: gradients rescaled to fixed size

References and Further Reading