

# Computer Vision – Lecture 15

## Epipolar Geometry & Stereo Basics

01.07.2019

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## Course Outline

- Image Processing Basics
- Segmentation & Grouping
- Object Recognition & Categorization
- Local Features & Matching
- Deep Learning
- 3D Reconstruction
  - Epipolar Geometry and Stereo Basics
  - Camera calibration & Uncalibrated Reconstruction
  - Multi-view Stereo

## Topics of This Lecture

- Geometric vision
  - Visual cues
  - Stereo vision
- Epipolar geometry
  - Depth with stereo
  - Geometry for a simple stereo system
  - Case example with parallel optical axes
  - General case with calibrated cameras
- Stereopsis & 3D Reconstruction
  - Correspondence search
  - Additional correspondence constraints
  - Possible sources of error
  - Applications

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## Geometric vision

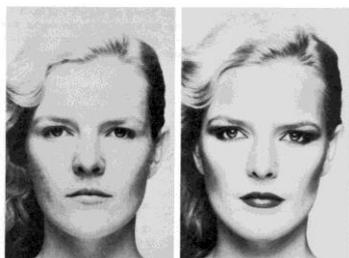
- Goal: Recovery of 3D structure
  - What cues in the image allow us to do this?



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## Visual Cues

- Shading

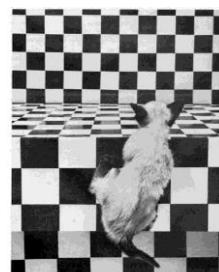


Merle Norman Cosmetics, Los Angeles

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## Visual Cues

- Shading
- Texture



The Visual Cliff, by William Vandivert, 1960

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## Visual Cues

- Shading
- Texture
- Focus



From *The Art of Photography*, Canon

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## Visual Cues

- Shading
- Texture
- Focus
- Perspective



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## Visual Cues

- Shading
- Texture
- Focus
- Perspective
- Motion



Figures from L. Zhang



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<http://www.brainconnection.com/essays/2manillusion/motionshare>

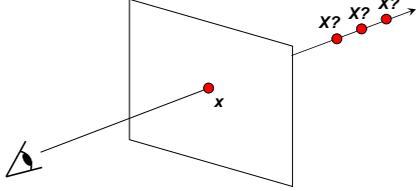
9

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## Our Goal: Recovery of 3D Structure

- We will focus on perspective and motion
- We need *multi-view geometry* because recovery of structure from one image is inherently ambiguous



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## To Illustrate This Point...

- Structure and depth are inherently ambiguous from single views.



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## Stereo Vision




[http://www.well.com/~jim/stereo/stereo\\_list.html](http://www.well.com/~jim/stereo/stereo_list.html)

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## What Is Stereo Vision?

- Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape



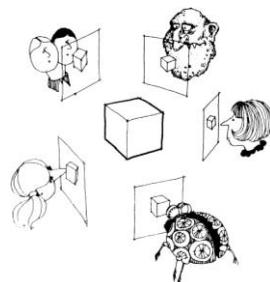
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13

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## What Is Stereo Vision?

- Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape



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14

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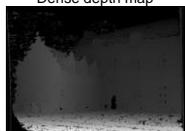
## What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image

Image 1  


Image 2  


Dense depth map



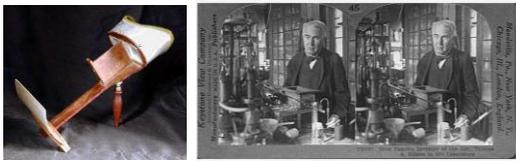
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## What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
  - Humans can do it



Stereograms: Invented by Sir Charles Wheatstone, 1838

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16

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## What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
  - Humans can do it



Autostereograms: <http://www.magiceye.com>

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17

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## What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
  - Humans can do it



Autostereograms: <http://www.magiceye.com>

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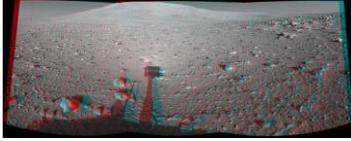
## Application of Stereo: Robotic Exploration



Nomad robot searches for meteorites in Antarctica



Real-time stereo on Mars



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## Topics of This Lecture

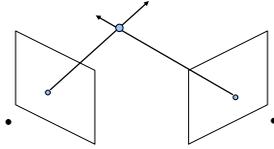
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## Depth with Stereo: Basic Idea



- Basic Principle: Triangulation
  - Gives reconstruction as intersection of two rays
  - Requires
    - Camera pose (calibration)
    - Point correspondence

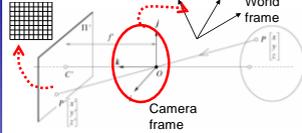
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## Camera Calibration



Extrinsic parameters:  
Camera frame ↔ Reference frame

Intrinsic parameters:  
Image coordinates relative to camera ↔ Pixel coordinates

- Parameters
  - *Extrinsic*: rotation matrix and translation vector
  - *Intrinsic*: focal length, pixel sizes (mm), image center point, radial distortion parameters

*We'll assume for now that these parameters are given and fixed.*

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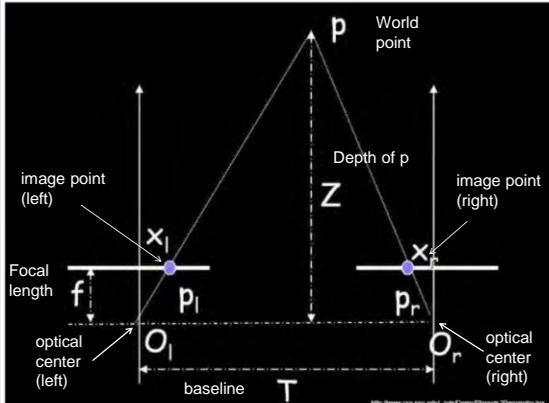
## Geometry for a Simple Stereo System

- First, assuming parallel optical axes, known camera parameters (i.e., calibrated cameras):

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## Geometry for a Simple Stereo System

- Assume parallel optical axes, known camera parameters (i.e., calibrated cameras). We can triangulate via:

Similar triangles ( $p_l, P, p_r$ ) and ( $O_l, P, O_r$ ):

$$\frac{T - (x_r - x_l)}{Z - f} = \frac{T}{Z}$$

$$Z = f \frac{T}{x_r - x_l}$$

“disparity”  $\rightarrow$   $x_r - x_l$

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## Depth From Disparity

Image  $I(x, y)$

Disparity map  $D(x, y)$

Image  $I'(x', y')$

$$(x', y') = (x + D(x, y), y)$$

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## General Case With Calibrated Cameras

- The two cameras need not have parallel optical axes.

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## Stereo Correspondence Constraints

p

p'?

- Given  $p$  in the left image, where can the corresponding point  $p'$  in the right image be?

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## Stereo Correspondence Constraints

p

p'?

- Given  $p$  in the left image, where can the corresponding point  $p'$  in the right image be?

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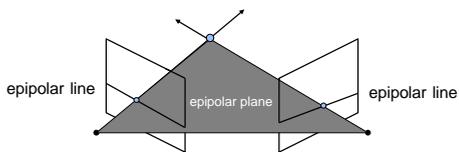
## Stereo Correspondence Constraints

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### Stereo Correspondence Constraints

- Geometry of two views allows us to constrain where the corresponding pixel for some image point in the first view must occur in the second view.



- Epipolar constraint: Why is this useful?
  - Reduces correspondence problem to 1D search along conjugate epipolar lines.

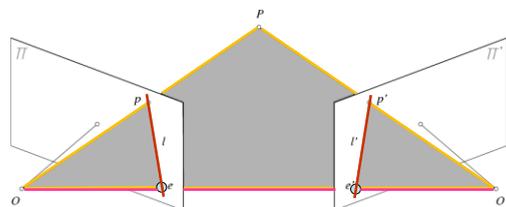
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Slide adapted from Steve Seitz

### Epipolar Geometry



- Epipolar Plane
- Baseline
- Epipoles
- Epipolar Lines

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### Epipolar Geometry: Terms

- **Baseline**
  - Line joining the camera centers
- **Epipole**
  - Point of intersection of baseline with the image plane
- **Epipolar plane**
  - Plane containing baseline and world point
- **Epipolar line**
  - Intersection of epipolar plane with the image plane
- **Properties**
  - All epipolar lines intersect at the epipole.
  - An epipolar plane intersects the left and right image planes in epipolar lines.

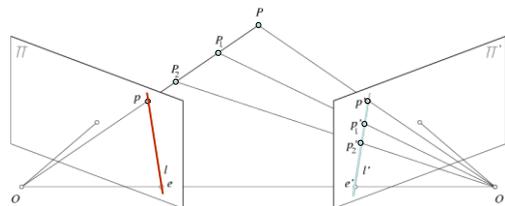
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### Epipolar Constraint



- Potential matches for  $p$  have to lie on the corresponding epipolar line  $l'$ .
- Potential matches for  $p'$  have to lie on the corresponding epipolar line  $l$ .

<http://www.ai.sri.com/~luong/research/Meta3DViewer/EpipolarGeo.html>

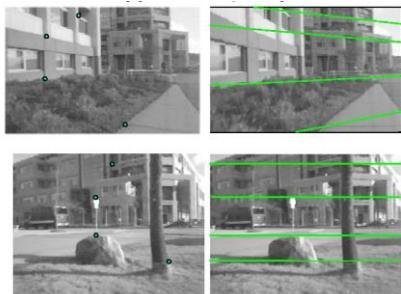
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### Example



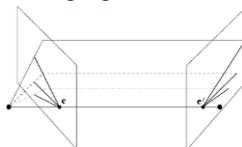
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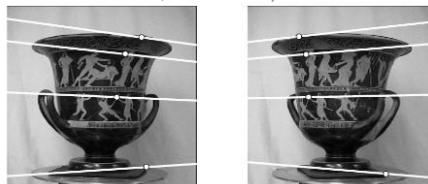
35

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### Example: Converging Cameras



As position of 3D point varies, epipolar lines "rotate" about the baseline



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Figure from Hartley & Zisserman

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### Example: Motion Parallel With Image Plane

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### Example: Forward Motion

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38

- Epipole has same coordinates in both images.
- Points move along lines radiating from  $e$ : "Focus of expansion"

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### Let's Formalize This!

- For a given stereo rig, how do we express the epipolar constraints algebraically?
- For this, we will need some linear algebra.
- But don't worry! We'll go through it step by step...

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### Stereo Geometry With Calibrated Cameras

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- If the rig is calibrated, we know:
  - How to rotate and translate camera reference frame 1 to get to camera reference frame 2.
    - Rotation: 3 x 3 matrix; translation: 3 vector.

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### Rotation Matrix

$$\mathbf{R}_x(\alpha) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{bmatrix}$$

Express 3D rotation as series of rotations around coordinate axes by angles  $\alpha, \beta, \gamma$

$$\mathbf{R}_y(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$$

Overall rotation is product of these elementary rotations:

$$\mathbf{R} = \mathbf{R}_x \mathbf{R}_y \mathbf{R}_z$$

$$\mathbf{R}_z(\gamma) = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

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### 3D Rigid Transformation

$$\begin{bmatrix} X' \\ Y' \\ Z' \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} + \begin{bmatrix} T_x \\ T_y \\ T_z \end{bmatrix}$$

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

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### Stereo Geometry With Calibrated Cameras

$\mathbf{p} = \begin{bmatrix} x \\ y \\ f \end{bmatrix}$

- Camera-centered coordinate systems are related by known rotation  $R$  and translation  $T$ :
 
$$\mathbf{X}' = R\mathbf{X} + \mathbf{T}$$

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### Excursion: Cross Product

$$\vec{a} \times \vec{b} = \vec{c} \quad \begin{aligned} \vec{a} \cdot \vec{c} &= 0 \\ \vec{b} \cdot \vec{c} &= 0 \end{aligned}$$

- Vector cross product takes two vectors and returns a third vector that's perpendicular to both inputs.
- So here,  $c$  is perpendicular to both  $a$  and  $b$ , which means the dot product is 0.

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### From Geometry to Algebra

$\mathbf{X}' = R\mathbf{X} + \mathbf{T}$

$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{X}') = \mathbf{X}' \cdot (\mathbf{T} \times R\mathbf{X})$

$\mathbf{T} \times \mathbf{X}' = \mathbf{T} \times R\mathbf{X} + \mathbf{T} \times \mathbf{T}$

Normal to the plane  $= \mathbf{T} \times R\mathbf{X}$

$0 = \mathbf{X}' \cdot (\mathbf{T} \times R\mathbf{X})$

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### Matrix Form of Cross Product

$$\vec{a} \times \vec{b} = \vec{c} \quad \begin{aligned} \vec{a} \cdot \vec{c} &= 0 \\ \vec{b} \cdot \vec{c} &= 0 \end{aligned}$$

"skew symmetric" matrix

$$[a_{\times}] = \begin{bmatrix} 0 & -a_z & a_y \\ a_z & 0 & -a_x \\ -a_y & a_x & 0 \end{bmatrix} \quad \vec{a} \times \vec{b} = [a_{\times}] \vec{b}$$

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### From Geometry to Algebra

$\mathbf{X}' = R\mathbf{X} + \mathbf{T}$

$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{X}') = \mathbf{X}' \cdot (\mathbf{T} \times R\mathbf{X})$

$\mathbf{T} \times \mathbf{X}' = \mathbf{T} \times R\mathbf{X} + \mathbf{T} \times \mathbf{T}$

Normal to the plane  $= \mathbf{T} \times R\mathbf{X}$

$0 = \mathbf{X}' \cdot (\mathbf{T} \times R\mathbf{X})$

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### Essential Matrix

$$\mathbf{X}' \cdot (\mathbf{T} \times R\mathbf{X}) = 0$$

$$\mathbf{X}' \cdot (\mathbf{T} \times R\mathbf{X}) = 0$$

Let  $\mathbf{E} = \mathbf{T} \times R$

$$\mathbf{X}'^T \mathbf{E} \mathbf{X} = 0$$

- This holds for the rays  $p$  and  $p'$  that are parallel to the camera-centered position vectors  $X$  and  $X'$ , so we have:  $\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$
- $E$  is called the **essential matrix**, which relates corresponding image points [Longuet-Higgins 1981]

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## Essential Matrix and Epipolar Lines

$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$  Epipolar constraint: if we observe point  $p$  in one image, then its position  $p'$  in second image must satisfy this equation.

$\mathbf{l}' = \mathbf{E} \mathbf{p}$  is the coordinate vector representing the epipolar line for point  $p$  (i.e., the line is given by:  $l'^T \mathbf{x} = 0$ )

$\mathbf{l} = \mathbf{E}^T \mathbf{p}'$  is the coordinate vector representing the epipolar line for point  $p'$

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## Essential Matrix: Properties

- Relates image of corresponding points in both cameras, given rotation and translation.
- Assuming intrinsic parameters are known

$\mathbf{E} = \mathbf{T} \cdot \mathbf{R}$

(i.e., the line is given by:  $l'^T \mathbf{x} = 0$ )

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## Essential Matrix Example: Parallel Cameras

$\mathbf{R} = \mathbf{I}$

$\mathbf{T} = [-d, 0, 0]^T$

$\mathbf{E} = [\mathbf{T}_x] \mathbf{R} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix}$

$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$

$$\begin{bmatrix} x' & y' & f \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ f \end{bmatrix} = 0$$

$$\Leftrightarrow \begin{bmatrix} x' & y' & f \end{bmatrix} \begin{bmatrix} 0 \\ df \\ -dy \end{bmatrix} = 0$$

$\Leftrightarrow y = y'$

For the parallel cameras, image of any point must lie on same horizontal line in each image plane.

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## More General Case

Image  $I(x, y)$       Disparity map  $D(x, y)$       Image  $I'(x', y')$

$(x', y') = (x + D(x, y), y)$

What about when cameras' optical axes are not parallel?

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## Stereo Image Rectification

- In practice, it is convenient if image scanlines are the epipolar lines.
- Algorithm
  - Reproject image planes onto a common plane parallel to the line between optical centers
  - Pixel motion is horizontal after this transformation
  - Two homographies ( $3 \times 3$  transforms), one for each input image reprojected

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Slide adapted from Li Zhang

C. Loop & Z. Zhang, Computing Rectifying Homographies for Stereo Vision, CVPR05

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## Stereo Image Rectification: Example

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54

Source: Aljosha Efros

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55

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## Stereo Reconstruction

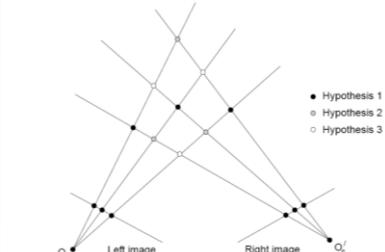
- Main Steps
  - Calibrate cameras
  - Rectify images
  - **Compute disparity**
  - Estimate depth



56

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## Correspondence Problem



Multiple match hypotheses satisfy epipolar constraint, but which is correct?

- Hypothesis 1
- Hypothesis 2
- Hypothesis 3




57

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## Dense Correspondence Search



- For each pixel in the first image
  - Find corresponding epipolar line in the right image
  - Examine all pixels on the epipolar line and pick the best match (e.g. SSD, correlation)
  - Triangulate the matches to get depth information
- This is easiest when epipolar lines are scanlines  
⇒ Rectify images first

59

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## Example: Window Search

- Data from University of Tsukuba




Scene

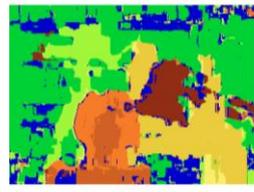
Ground truth

60

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## Example: Window Search

- Data from University of Tsukuba




Window-based matching  
(best window size)

Ground truth

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## Effect of Window Size

$W = 3$                        $W = 20$

Want window large enough to have sufficient intensity variation, yet small enough to contain only pixels with about the same disparity.

62

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## Alternative: Sparse Correspondence Search

HON. ABRAHAM LINCOLN, President of United States.

- Idea: Restrict search to sparse set of detected features
- Rather than pixel values (or lists of pixel values) use *feature descriptor* and an associated *feature distance*
- Still narrow search further by epipolar geometry

*What would make good features?*

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## Dense vs. Sparse

- Sparse
  - Efficiency
  - Can have more reliable feature matches, less sensitive to illumination than raw pixels
  - But...
    - Have to know enough to pick good features
    - Sparse information
- Dense
  - Simple process
  - More depth estimates, can be useful for surface reconstruction
  - But...
    - Breaks down in textureless regions anyway
    - Raw pixel distances can be brittle
    - Not good with very different viewpoints

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## Difficulties in Similarity Constraint

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Untextured surfaces

Occlusions

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## Possible Sources of Error?

- Low-contrast / textureless image regions
- Occlusions
- Camera calibration errors
- Violations of *brightness constancy* (e.g., specular reflections)
- Large motions

66

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## Application: View Interpolation

Right Image

67

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## Application: View Interpolation



Left Image

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## Application: View Interpolation



Disparity

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## Application: View Interpolation



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## Application: Free-Viewpoint Video



<http://www.liberovision.com>

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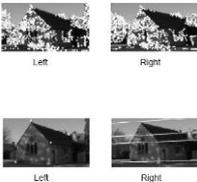
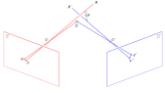
71

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## Summary: Stereo Reconstruction

- Main Steps
  - Calibrate cameras
  - Rectify images
  - Compute disparity
  - Estimate depth
- So far, we have only considered calibrated cameras...
- Next lecture
  - Uncalibrated cameras
  - Camera parameters
  - Revisiting epipolar geometry
  - Robust fitting

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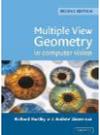
72

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## References and Further Reading

- Background information on epipolar geometry and stereopsis can be found in Chapters 10.1-10.2 and 11.1-11.3 of
  - D. Forsyth, J. Ponce. *Computer Vision – A Modern Approach*. Prentice Hall, 2003
- More detailed information (if you really want to implement 3D reconstruction algorithms) can be found in Chapters 9 and 10 of
  - R. Hartley, A. Zisserman. *Multiple View Geometry in Computer Vision* 2nd Ed., Cambridge Univ. Press, 2004

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73