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# Computer Vision – Lecture 8

## Local Features

14.05.2019

Computer Vision Summer'19

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## Course Outline

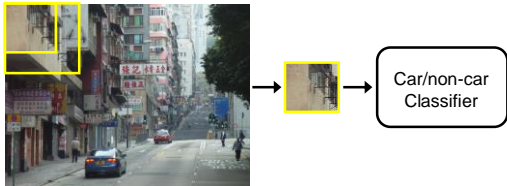
- Image Processing Basics
- Segmentation & Grouping
- Object Recognition & Categorization
  - Sliding Window based Object Detection
- Local Features & Matching
  - Local Features – Detection and Description
  - Recognition with Local Features
- Deep Learning
- 3D Reconstruction

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## Recap: Sliding-Window Object Detection

- If object may be in a cluttered scene, slide a window around looking for it.



- Essentially, this is a brute-force approach with many local decisions.

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Slide credit: Kristen Grauman

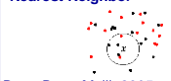
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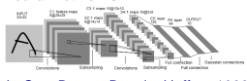
## Classifier Construction: Many Choices...

### Nearest Neighbor



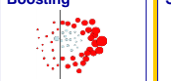
Berg, Berg, Malik 2005,  
Chum, Zisserman 2007,  
Boiman, Shechtman, Irani 2008, ...

### Neural networks



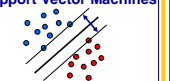
LeCun, Bottou, Bengio, Haffner 1998  
Rowley, Baluja, Kanade 1998  
...

### Boosting




Viola, Jones 2001,  
Torralba et al. 2004,  
Opelt et al. 2006,  
Benenson 2012, ...

### Support Vector Machines



Vapnik, Schölkopf 1995,  
Papageorgiou, Poggio '01,  
Dalal, Triggs 2005,  
Vedaldi, Zisserman 2012

### Randomized Forests



Amit, Geman 1997,  
Breiman 2001,  
Lepetit, Fua 2006,  
Gall, Lempitsky 2009, ...

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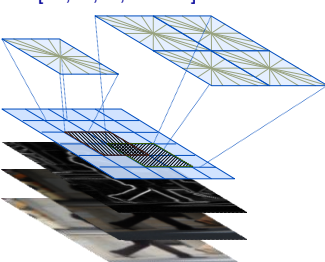
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## Recap: HOG Descriptor Processing Chain



Object/Non-object

Linear SVM

Collect HOGs over detection window

Contrast normalize over overlapping spatial cells

Weighted vote in spatial & orientation cells

Compute gradients

Gamma compression

Image Window

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Slide credit: Navneet Dalal

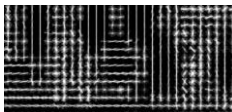
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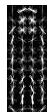
## Recap: Pedestrian Detection with HOG

- Train a pedestrian template using a linear SVM
- At test time, convolve feature map with learned template  $w$ 
  - Linear SVM classification function
 
$$y(x) = w^T x + b$$

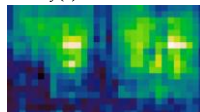
HOG feature map  
 $x$



Template  
 $w$



Detector response map  
 $y(x) = w^T x + b$



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N. Dalal and B. Triggs, [Histograms of Oriented Gradients for Human Detection](#), CVPR 2005

Slide credit: Svetlana Lazebnik

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## Classifier Construction: Many Choices...

### Nearest Neighbor

Shakhnarovich, Viola, Darrell 2003  
Berg, Berg, Malik 2005,  
Boiman, Shechtman, Irani 2008, ...

### Neural networks

LeCun, Bottou, Bengio, Haffner 1998  
Rowley, Baluja, Kanade 1998  
...

### Boosting

Viola, Jones 2001,  
Torralba et al. 2004,  
Opelt et al. 2006,  
Benenson 2012, ...

### Support Vector Machines

Vapnik, Schölkopf 1995,  
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Dalal, Triggs 2005,  
Vedaldi, Zisserman 2012

### Randomized Forests

Amit, Geman 1997,  
Breiman 2001,  
Lepetit, Fua 2006,  
Gall, Lempitsky 2009, ...

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## Recap: AdaBoost

Final classifier is combination of the weak classifiers

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## AdaBoost: Detailed Training Algorithm

see lecture Machine Learning!

- Initialization: Set  $w_n^{(1)} = \frac{1}{N}$  for  $n = 1, \dots, N$ .
- For  $m = 1, \dots, M$  iterations
  - Train a new weak classifier  $h_m(\mathbf{x})$  using the current weighting coefficients  $\mathbf{W}^{(m)}$  by minimizing the weighted error function
 
$$J_m = \sum_{n=1}^N w_n^{(m)} I(h_m(\mathbf{x}_n) \neq t_n) \quad I(A) = \begin{cases} 1, & \text{if } A \text{ is true} \\ 0, & \text{else} \end{cases}$$
  - Estimate the weighted error of this classifier on  $\mathbf{X}$ :
 
$$\epsilon_m = \frac{\sum_{n=1}^N w_n^{(m)} I(h_m(\mathbf{x}_n) \neq t_n)}{\sum_{n=1}^N w_n^{(m)}}$$
  - Calculate a weighting coefficient for  $h_m(\mathbf{x})$ :
 
$$\alpha_m = \ln \left\{ \frac{1 - \epsilon_m}{\epsilon_m} \right\}$$
  - Update the weighting coefficients:
 
$$w_n^{(m+1)} = w_n^{(m)} \exp \{ \alpha_m I(h_m(\mathbf{x}_n) \neq t_n) \}$$

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## Example: Face Detection

- Frontal faces are a good example of a class where global appearance models + a sliding window detection approach fit well:
  - Regular 2D structure
  - Center of face almost shaped like a "patch"/window

- Now we'll take AdaBoost and see how the Viola-Jones face detector works

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## Feature extraction

"Rectangular" filters

Feature output is difference between adjacent regions

Value at (x,y) is sum of pixels above and to the left of (x,y)

Efficiently computable with integral image: any sum can be computed in constant time

Avoid scaling images  $\rightarrow$  scale features directly for same cost

$$D = 1 + 4 - (2 + 3) = A + (A + B + C + D) - (A + C + A + B) = D$$

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Slide credit: Kristen Grauman B. Leibe [Viola & Jones, CVPR 2001]

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## Large Library of Features

Considering all possible filter parameters: position, scale, and type:

180,000+ possible features associated with each 24 x 24 window

Use AdaBoost both to select the informative features and to form the classifier

Weak classifier: feature output  $> \theta$

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Slide credit: Kristen Grauman B. Leibe [Viola & Jones, CVPR 2001]

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## AdaBoost for Feature+Classifier Selection

- Want to select the single rectangle feature and threshold that best separates **positive** (faces) and **negative** (non-faces) training examples, in terms of *weighted error*.

Resulting weak classifier:

$$h_t(x) = \begin{cases} +1 & \text{if } f_t(x) > \theta_t \\ -1 & \text{otherwise} \end{cases}$$

For next round, reweight the examples according to errors, choose another filter/threshold combo.

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[Viola & Jones, CVPR 2001]

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## Cascading Classifiers for Detection

- Even if the filters are fast to compute, each new image has a lot of possible windows to search.
- For efficiency, apply less accurate but faster classifiers first to immediately discard windows that clearly appear to be negative; e.g.,
  - Filter for promising regions with an initial inexpensive classifier
  - Build a chain of classifiers, choosing cheap ones with low false negative rates early in the chain

[Fleuret & Geman, IJCV 2001]  
 [Rowley et al., PAMI 1998]  
 [Viola & Jones, CVPR 2001]

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Figure from Viola & Jones CVPR

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## Recap: Viola-Jones Face Detector

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## Viola-Jones Face Detector: Results

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## Viola-Jones Face Detector: Results

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## You Can Try It At Home...

- The Viola & Jones detector was a huge success
  - First real-time face detector available
  - Many derivative works and improvements
- C++ implementation available in OpenCV [Lienhart, 2002]
  - <http://sourceforge.net/projects/opencvlibrary/>
- Matlab wrappers for OpenCV code available, e.g. here
  - <http://www.mathworks.com/matlabcentral/fileexchange/19912>

P. Viola, M. Jones, [Robust Real-Time Face Detection](#), IJCV, Vol. 57(2), 2004

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## Limitations: Changing Aspect Ratios

- Sliding window requires fixed window size
  - Basis for learning efficient cascade classifier
- How to deal with changing aspect ratios?
  - Fixed window size
    - Wastes training dimensions
  - Adapted window size
    - Difficult to share features
  - "Squashed" views [Dalal&Triggs]
    - Need to squash test image, too



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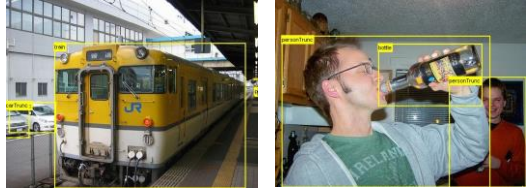
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## Limitations (continued)

- Not all objects are "box" shaped



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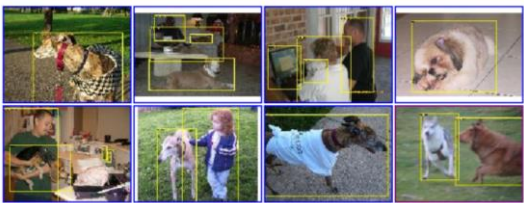
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## Limitations (continued)

- Non-rigid, deformable objects not captured well with representations assuming a fixed 2D structure; or must assume fixed viewpoint
- Objects with less-regular textures not captured well with holistic appearance-based descriptions



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## Limitations (continued)

- If considering windows in isolation, context is lost



Sliding window      Detector's view

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Figure credit: Derek Hoiem

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## Topics of This Lecture

- Local Invariant Features**
  - Motivation
  - Requirements, Invariances
- Keypoint Localization**
  - Harris detector
  - Hessian detector
- Scale Invariant Region Selection**
  - Automatic scale selection
  - Laplacian-of-Gaussian detector
  - Difference-of-Gaussian detector
  - Combinations
- Local Descriptors**
  - Orientation normalization
  - SIFT

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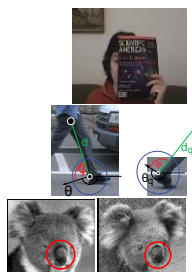
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## Motivation

- Global representations have major limitations
- Instead, describe and match only local regions
- Increased robustness to
  - Occlusions
  - Articulation
  - Intra-category variations



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## Application: Image Matching

by [Diva Sian](#)

by [swashford](#)

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## Harder Case

by [Diva Sian](#)

by [scqbt](#)

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## Harder Still?

NASA Mars Rover images

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## Answer Below (Look for Tiny Colored Squares)

NASA Mars Rover images with SIFT feature matches

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## Application: Image Stitching

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## Application: Image Stitching

- Procedure:
  - > Detect feature points in both images

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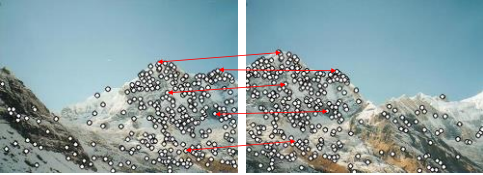
Slide credit: Darya Erolova, Denis Simakov

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## Application: Image Stitching




- Procedure:
  - Detect feature points in both images
  - Find corresponding pairs

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Slide credit: Darya Erolova, Denis Simakov, B. Leibe

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## Application: Image Stitching



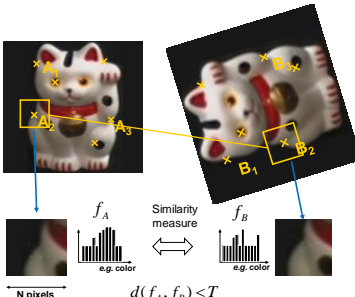
- Procedure:
  - Detect feature points in both images
  - Find corresponding pairs
  - Use these pairs to align the images

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## General Approach



1. Find a set of distinctive key-points
2. Define a region around each keypoint
3. Extract and normalize the region content
4. Compute a local descriptor from the normalized region
5. Match local descriptors


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## Common Requirements

- Problem 1:
  - Detect the same point *independently* in both images



No chance to match!

We need a repeatable detector!


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## Common Requirements

- Problem 1:
  - Detect the same point *independently* in both images
- Problem 2:
  - For each point correctly recognize the corresponding one




We need a reliable and distinctive descriptor!

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## Invariance: Geometric Transformations



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## Levels of Geometric Invariance

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## Requirements

- Region extraction needs to be **repeatable** and **accurate**
  - > **Invariant** to translation, rotation, scale changes
  - > **Robust or covariant** to out-of-plane ( $\approx$ affine) transformations
  - > **Robust** to lighting variations, noise, blur, quantization
- Locality**: Features are local, therefore robust to occlusion and clutter.
- Quantity**: We need a sufficient number of regions to cover the object.
- Distinctiveness**: The regions should contain "interesting" structure.
- Efficiency**: Close to real-time performance.

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## Many Existing Detectors Available

- Hessian & Harris** [Beaudet '78], [Harris '88]
- Laplacian, DoG** [Lindeberg '98], [Lowe '99]
- Harris-/Hessian-Laplace** [Mikolajczyk & Schmid '01]
- Harris-/Hessian-Affine** [Mikolajczyk & Schmid '04]
- EBR and IBR** [Tuytelaars & Van Gool '04]
- MSER** [Matas '02]
- Salient Regions** [Kadir & Brady '01]
- Others...

*Those detectors have become a basic building block for many applications in Computer Vision.*

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## Keypoint Localization

- Goals:
  - > Repeatable detection
  - > Precise localization
  - > Interesting content

$\Rightarrow$  Look for two-dimensional signal changes

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## Finding Corners

- Key property:
  - > In the region around a corner, image gradient has two or more dominant directions
- Corners are *repeatable* and *distinctive*

C.Harris and M.Stephens. "A Combined Corner and Edge Detector." *Proceedings of the 4th Alvey Vision Conference, 1988.*

Slide credit: Svetlana Lazebnik

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## Corners as Distinctive Interest Points

- Design criteria
  - > We should easily recognize the point by looking through a small window (*locality*)
  - > Shifting the window in *any direction* should give a *large change* in intensity (*good localization*)

"flat" region: no change in all directions

"edge": no change along the edge direction

"corner": significant change in all directions

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## Harris Detector Formulation




Image  $I$     $I_x$     $I_y$     $I_x I_y$

- Start from the second-moment matrix  $M$  :

$$M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

Sum over image region – the area we are checking for corner

Gradient with respect to  $x$ , times gradient with respect to  $y$

$$M = \begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_x I_y & \sum I_y I_y \end{bmatrix} = \sum \begin{bmatrix} I_x \\ I_y \end{bmatrix} \begin{bmatrix} I_x & I_y \end{bmatrix}$$

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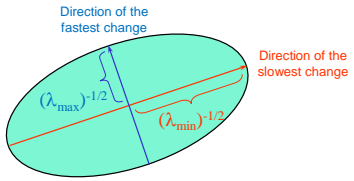
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Slide credit: Rick Szaliski

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## What Does This Matrix Reveal?

- Since  $M$  is symmetric, we have  $M = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$   
(Eigenvalue decomposition)
- We can visualize  $M$  as an ellipse with axis lengths determined by the eigenvalues and orientation determined by  $R$



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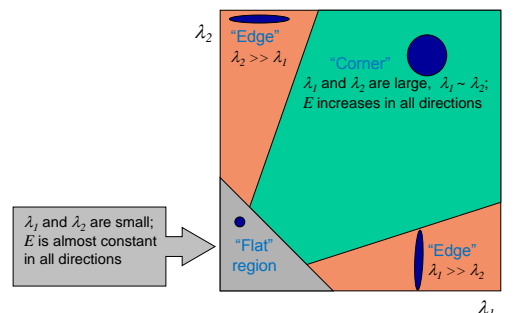
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Slide credit: Kristen Grauman   B. Leibe   adapted from Darya Frolova, Denis Simakov

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## Interpreting the Eigenvalues

- Classification of image points using eigenvalues of  $M$ :



$\lambda_2$  "Edge"  $\lambda_2 \gg \lambda_1$

"Corner"  $\lambda_1$  and  $\lambda_2$  are large,  $\lambda_1 \sim \lambda_2$ ;  $E$  increases in all directions

"Flat" region  $\lambda_1$  and  $\lambda_2$  are small;  $E$  is almost constant in all directions

"Edge"  $\lambda_1 \gg \lambda_2$

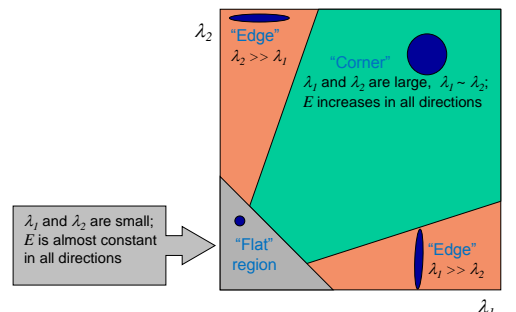
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## Corner Response Function

$$R = \det(M) - \alpha \text{trace}(M)^2 = \lambda_1 \lambda_2 - \alpha (\lambda_1 + \lambda_2)^2$$


$\lambda_2$  "Edge"  $R < 0$

"Corner"  $R > 0$

"Flat" region  $R < 0$

"Edge"  $R < 0$

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- Fast approximation
  - Avoid computing the eigenvalues
  - $\alpha$ : constant (0.04 to 0.06)

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## Window Function $w(x,y)$

$$M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

- Option 1: uniform window
  - Sum over square window
$$M = \sum_{x,y} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

1 in window, 0 outside

Problem: not rotation invariant
- Option 2: Smooth with Gaussian
  - Gaussian already performs weighted sum
$$M = g(\sigma) * \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

Gaussian

Result is rotation invariant

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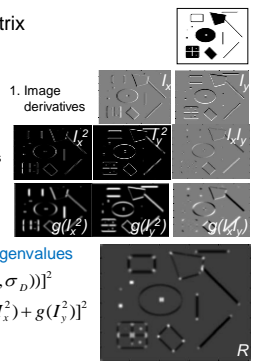
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## Summary: Harris Detector [Harris88]

- Compute second moment matrix (autocorrelation matrix)
 
$$M(\sigma_x, \sigma_y) = g(\sigma_x) * \begin{bmatrix} I_x^2(\sigma_y) & I_x I_y(\sigma_y) \\ I_x I_y(\sigma_y) & I_y^2(\sigma_y) \end{bmatrix}$$
  - Image derivatives
  - Square of derivatives
  - Gaussian filter  $g(\sigma)$
- Corneriness function – two strong eigenvalues
 
$$R = \det[M(\sigma_x, \sigma_y)] - \alpha [\text{trace}(M(\sigma_x, \sigma_y))]^2$$

$$= g(I_x^2)g(I_y^2) - [g(I_x I_y)]^2 - \alpha [g(I_x^2) + g(I_y^2)]^2$$
- Perform non-maximum suppression



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Slide credit: Krystian Mikolajczyk



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### Harris Detector: Workflow

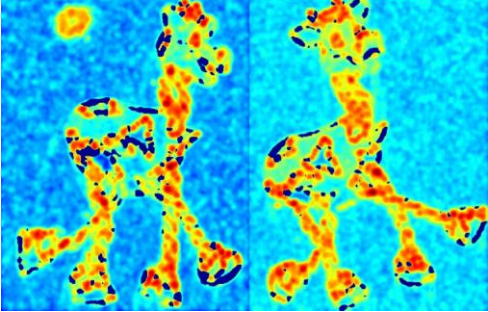


Slide adapted from Darya Erolova, Denis Simakov, B. Leibe

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### Harris Detector: Workflow




- Compute corner responses  $R$

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### Harris Detector: Workflow



- Take only the local maxima of  $R$ , where  $R >$  threshold.

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### Harris Detector: Workflow



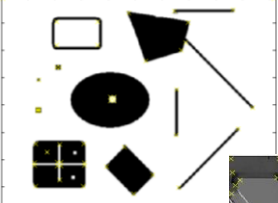
- Resulting Harris points

Slide adapted from Darya Erolova, Denis Simakov, B. Leibe


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### Harris Detector – Responses [Harris88]



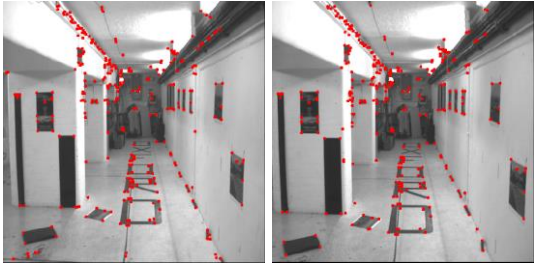
Effect: A very precise corner detector.




Slide credit: Kostas Mikolajczyk

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### Harris Detector – Responses [Harris88]



- Results are well suited for finding stereo correspondences



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## Harris Detector: Properties

- Rotation invariance?

Ellipse rotates but its shape (i.e. eigenvalues) remains the same

Corner response  $R$  is invariant to image rotation

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## Harris Detector: Properties

- Rotation invariance
- Scale invariance?

Corner All points will be classified as edges!

Not invariant to image scale!

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## Hessian Detector [Beaudet78]

- Hessian determinant

$$\text{Hessian}(I) = \begin{bmatrix} I_{xx} & I_{xy} \\ I_{xy} & I_{yy} \end{bmatrix}$$

Note: these are 2<sup>nd</sup> derivatives!

*Intuition:* Search for strong derivatives in two orthogonal directions

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## Hessian Detector [Beaudet78]

- Hessian determinant

$$\text{Hessian}(I) = \begin{bmatrix} I_{xx} & I_{xy} \\ I_{xy} & I_{yy} \end{bmatrix}$$

$$\det(\text{Hessian}(I)) = I_{xx}I_{yy} - I_{xy}^2$$

In Matlab:

$$I_{xx} * I_{yy} - (I_{xy})^2$$

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## Hessian Detector – Responses [Beaudet78]

*Effect:* Responses mainly on corners and strongly textured areas.

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## Topics of This Lecture

- Local Invariant Features
  - Motivation
  - Requirements, Invariances
- Keypoint Localization
  - Harris detector
  - Hessian detector
- Scale Invariant Region Selection
  - Automatic scale selection
  - Laplacian-of-Gaussian detector
  - Difference-of-Gaussian detector
  - Combinations
- Local Descriptors
  - Orientation normalization
  - SIFT


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## From Points to Regions...

- The Harris and Hessian operators define interest points.
  - Precise localization
  - High repeatability



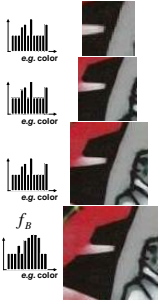
- In order to compare those points, we need to compute a descriptor over a region.
  - How can we define such a region in a scale invariant manner?
- I.e. how can we detect scale invariant interest regions?*

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## Naïve Approach: Exhaustive Search

- Comparing descriptors while varying the patch size
  - Computationally inefficient
  - Inefficient but possible for matching
  - Prohibitive for retrieval in large databases
  - Prohibitive for recognition



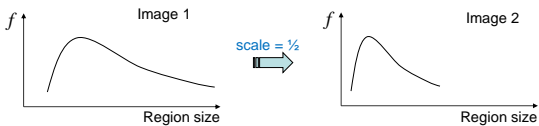
Similarity measure =  $d(f_A, f_B)$

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## Automatic Scale Selection

- Solution:
  - Design a signature function on the region that is "scale invariant" (the same for corresponding regions, even if they are at different scales)
  - For a point in one image, we can consider it as a function of region size (patch width)



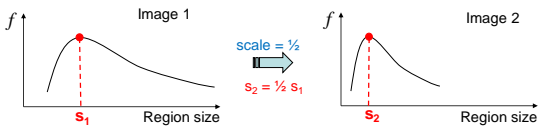
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## Automatic Scale Selection

- Common approach:
  - Take a local maximum of this function.
  - Observation: region size for which the maximum is achieved should be *invariant* to image scale.

Important: this scale invariant region size is found in each image *independently!*

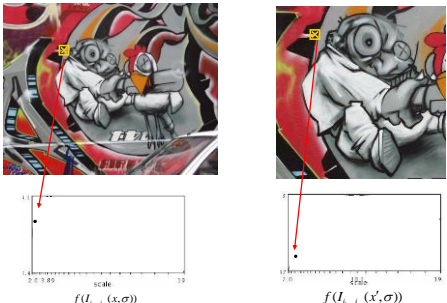


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## Automatic Scale Selection

- Function responses for increasing scale (scale signature)

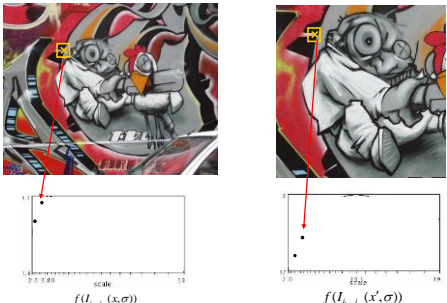


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## Automatic Scale Selection

- Function responses for increasing scale (scale signature)



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## Automatic Scale Selection

- Function responses for increasing scale (scale signature)

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## Automatic Scale Selection

- Function responses for increasing scale (scale signature)

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## Automatic Scale Selection

- Function responses for increasing scale (scale signature)

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## Automatic Scale Selection

- Function responses for increasing scale (scale signature)

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## Automatic Scale Selection

- Normalize: Rescale to fixed size

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## What Is A Useful Signature Function?

- Laplacian-of-Gaussian = "blob" detector

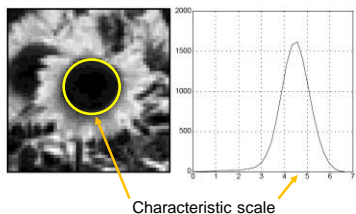
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### Characteristic Scale

- We define the *characteristic scale* as the scale that produces peak of Laplacian response



T. Lindeberg (1998). "Feature detection with automatic scale selection." *International Journal of Computer Vision* 30 (2): pp 77--116.

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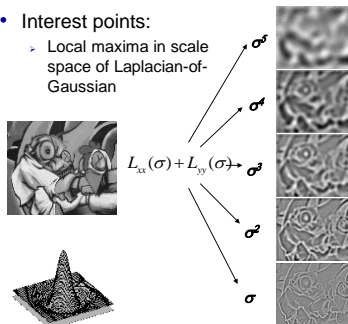
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### Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



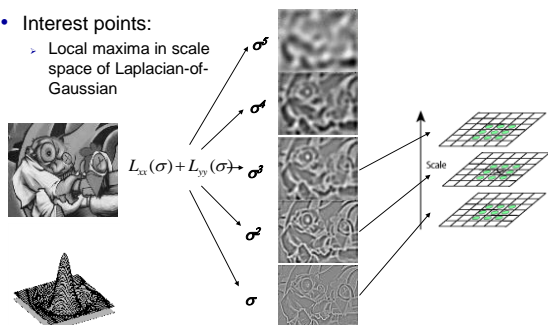
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### Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



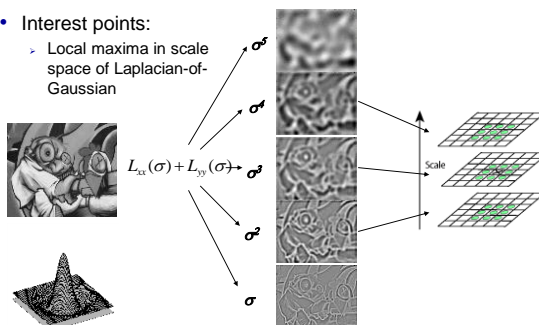
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### Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



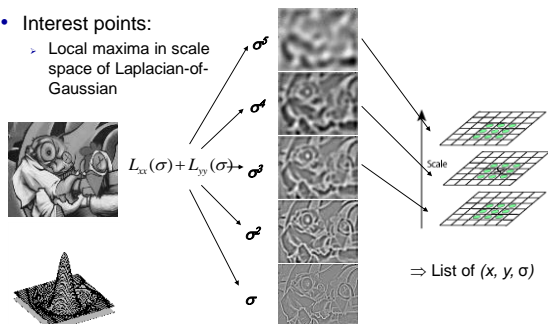
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### Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



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### LoG Detector: Workflow



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## LoG Detector: Workflow



sigma = 11.9912

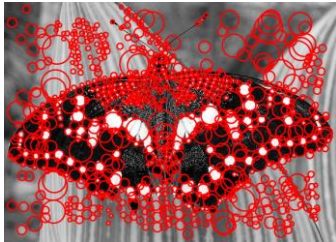
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## LoG Detector: Workflow



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## Technical Detail

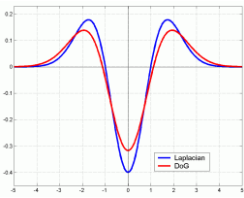
- We can efficiently approximate the Laplacian with a difference of Gaussians:

$$L = \sigma^2 (G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

(Difference of Gaussians)



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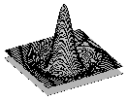

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## Difference-of-Gaussian (DoG)

- Difference of Gaussians as approximation of the LoG
  - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
  - No need to compute 2<sup>nd</sup> derivatives
  - Gaussians are computed anyway, e.g. in a Gaussian pyramid.

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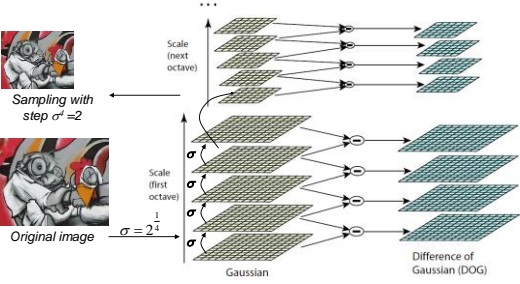
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## DoG – Efficient Computation

- Computation in Gaussian scale pyramid




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## Results: Lowe's DoG



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## Harris-Laplace [Mikolajczyk '01]

1. Initialization: Multiscale Harris corner detection
2. Scale selection based on Laplacian (same procedure with Hessian  $\Rightarrow$  Hessian-Laplace)

Harris points

Harris-Laplace points

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## Summary: Scale Invariant Detection

- **Given:** Two images of the same scene with a large *scale difference* between them.
- **Goal:** Find *the same* interest points *independently* in each image.
- **Solution:** Search for *maxima* of suitable functions in *scale* and in *space* (over the image).
- Two strategies
  - Laplacian-of-Gaussian (LoG)
  - Difference-of-Gaussian (DoG) as a fast approximation
  - *These can be used either on their own, or in combinations with single-scale keypoint detectors (Harris, Hessian).*

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## Local Descriptors

- We know how to detect points
- Next question: **How to describe them for matching?**

$\Rightarrow$  Next lecture...

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## You Can Try It At Home...

- For most local feature detectors, executables are available online:
  - <http://robots.ox.ac.uk/~vgg/research/affine>
  - <http://www.cs.ubc.ca/~lowe/keypoints/>
  - <http://www.vision.ee.ethz.ch/~surf>
  - <http://homes.esat.kuleuven.be/~ncorneli/gpusurf/>

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## Affine Covariant Features

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### Affine Covariant Region Detectors

Detector output

**Parameters defining an affine region**

```

x0, y0, x1, y1  m  s1  s2  r1  r2  r3  r4  r5  r6  r7  r8  r9  r10  r11  r12  r13  r14  r15  r16  r17  r18  r19  r20  r21  r22  r23  r24  r25  r26  r27  r28  r29  r30  r31  r32  r33  r34  r35  r36  r37  r38  r39  r40  r41  r42  r43  r44  r45  r46  r47  r48  r49  r50  r51  r52  r53  r54  r55  r56  r57  r58  r59  r60  r61  r62  r63  r64  r65  r66  r67  r68  r69  r70  r71  r72  r73  r74  r75  r76  r77  r78  r79  r80  r81  r82  r83  r84  r85  r86  r87  r88  r89  r90  r91  r92  r93  r94  r95  r96  r97  r98  r99  r100
  
```

**Code**

```

// provided by the authors, see README for details and links to authors web sites
// Lines: features  Example of use  Displaying
// -----
// 1. Main: Main program
// 2. Detector: Main program
// 3. Detector: Main program
// 4. Detector: Main program
// 5. Detector: Main program
// 6. Detector: Main program
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```

<http://www.robots.ox.ac.uk/~vgg/research/affine/detectors.html#binaries>

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## References and Further Reading

- Read David Lowe's SIFT paper
  - D. Lowe, *Distinctive image features from scale-invariant keypoints*, IJCV 60(2), pp. 91-110, 2004
- Good survey paper on Int. Pt. detectors and descriptors
  - T. Tuytelaars, K. Mikolajczyk, *Local Invariant Feature Detectors: A Survey*, Foundations and Trends in Computer Graphics and Vision, Vol. 3, No. 3, pp 177-280, 2008.
- Try the example code, binaries, and Matlab wrappers
  - Good starting point: Oxford interest point page <http://www.robots.ox.ac.uk/~vgg/research/affine/detectors.html#binaries>

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