Computer Vision 2 – Lecture 10

Multi-Object Tracking III (06.06.2016)

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Content of the Lecture

- Single-Object Tracking
- Bayesian Filtering
- Kalman Filters, EKF
- Particle Filters
- Multi-Object Tracking
- Introduction
- MHT, (JPDAF)
- Network Flow Optimization



Visual SLAM & 3D Reconstruction







Topics of This Lecture

- · Recap: MHT
- · Data Association as Linear Assignment Problem
 - LAP formulation
 - Greedy algorithm
 - Hungarian algorithm
- · Tracking as Network Flow Optimization
- Min-cost network flow
- Generalizing to multiple frames
- Complications
- Formulation



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Recap: Multi-Hypothesis Tracking (MHT)

- Ideas
 - Instead of forming a track tree, keep a set of hypotheses that generate child hypotheses based on the associations.
- Enforce exclusion constraints between tracks and measurements in the assignment.
- Integrate track generation into the assignment process.
- After hypothesis generation, merge and prune the current hypothesis set.
 - D. Reid, An Algorithm for Tracking Multiple Targets, IEEE Trans. Automatic
 - Control, Vol. 24(6), pp. 843-854, 1979.
- 4

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Recap: Hypothesis Generation

· Create hypothesis matrix of the feasible associations

$$\Theta = \begin{bmatrix} \mathbf{X}_1 & \mathbf{X}_2 \mathbf{X}_{fa} \mathbf{X}_{nt} \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix} \begin{array}{c} \mathbf{y}_1 \\ \mathbf{y}_2 \\ \mathbf{y}_3 \\ \mathbf{y}_4 \end{bmatrix}$$



- Interpretation
- Columns represent tracked objects, rows encode measurements
- A non-zero element at matrix position (i,j) denotes that measurement \mathbf{y}_i is contained in the validation region of track \mathbf{x}_j .
- Extra column \mathbf{x}_{fa} for association as false alarm.
- Extra column \mathbf{x}_{nt} for association as new track.

Enumerate all assignments that are consistent with this matrix.

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Recap: Assignments

Z_{j}	\mathbf{x}_1	\mathbf{x}_2	\mathbf{x}_{fa}	\mathbf{x}_{nt}
\mathbf{y}_1	0	0	1	0
\mathbf{y}_2	1	0	0	0
\mathbf{y}_3	0	1	0	0
\mathbf{y}_4	0	0	0	1

- Impose constraints
 - A measurement can originate from only one object.
- ⇒ Any row has only a single non-zero value.
- An object can have at most one associated measurement per time step.
- \Rightarrow Any column has only a single non-zero value, except for $\mathbf{x}_{fa}, \mathbf{x}_{nt}$



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Recap: Calculating Hypothesis Probabilities

- · Probabilistic formulation
- It is straightforward to enumerate all possible assignments.
- However, we also need to calculate the probability of each child
- This is done recursively:

$$\begin{split} p(\Omega_j^{(k)}|\mathbf{Y}^{(k)}) &= p(Z_j^{(k)}, \Omega_{p(j)}^{(k-1)}|\mathbf{Y}^{(k)}) \\ &\stackrel{Bayes}{=} \eta p(\mathbf{Y}^{(k)}|Z_j^{(k)}, \Omega_{p(j)}^{(k-1)}) p(Z_j^{(k)}, \Omega_{p(j)}^{(k-1)}) \\ &= \eta p(\mathbf{Y}^{(k)}|Z_j^{(k)}, \Omega_{p(j)}^{(k-1)}) p(Z_j^{(k)}|\Omega_{p(j)}^{(k-1)}) p(\Omega_{p(j)}^{(k-1)}) \\ &\text{Normalization} \quad \text{Measurement} \quad \underset{\text{factor}}{\text{Prob. of}} \quad \underset{\text{assignment set}}{\text{Prob. of}} \quad \underset{\text{parent}}{\text{Prob. of}} \quad \end{split}$$

Recap: Measurement Likelihood

- Use KF prediction
- Assume that a measurement $\mathbf{y}_i^{(k)}$ associated to a track \mathbf{x}_j has a Gaussian pdf centered around the measurement prediction $\hat{\mathbf{x}}_j^{(k)}$ with innovation covariance $\widehat{\boldsymbol{\Sigma}}_j^{(k)}$.
- Further assume that the pdf of a measurement belonging to a new track or false alarm is uniform in the observation volume \tilde{W} (the sensor's field-of-view) with probability $W^{\text{--}1}$.
- Thus, the measurement likelihood can be expressed as

$$\begin{split} p\left(\mathbf{Y}^{(k)}|Z_{j}^{(k)},\Omega_{p(j)}^{(k-1)}\right) &= \prod_{i=1}^{M_{k}} \mathcal{N}\left(\mathbf{y}_{i}^{(k)};\hat{\mathbf{x}}_{j},\widehat{\boldsymbol{\Sigma}}_{j}^{(k)}\right)^{\delta_{i}} W^{-(1-\delta_{i})} \\ &= W^{-(N_{fal}+N_{new})} \prod_{i=1}^{M_{k}} \mathcal{N}\left(\mathbf{y}_{i}^{(k)};\hat{\mathbf{x}}_{j},\widehat{\boldsymbol{\Sigma}}_{j}^{(k)}\right)^{\delta_{i}} \end{split}$$

Recap: Probability of an Assignment Set

$$p(Z_j^{(k)}|\Omega_{p(j)}^{(k-1)})$$

Composed of three terms

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- 1. Probability of the number of tracks N_{det} , N_{fal} , N_{new}

- Assumption 1:
$$N_{det}$$
 follows a binomial distribution
$$p(N_{det}|\Omega_{p(j)}^{(k-1)}) \ = \ \binom{N}{N_{det}} \ p_{det}^{N_{det}} (1-p_{det})^{(N-N_{det})}$$

where N is the number of tracks in the parent hypothesis

- Assumption 2: N_{fal} and N_{new} both follow a Poisson distribution with expected number of events $\lambda_{fal}W$ and $\lambda_{new}W$

$$\begin{split} p(N_{det}, N_{fal}, N_{new} | \Omega_{p(j)}^{(k-1)}) &= \binom{N}{N_{det}} p_{det}^{N_{det}} (1 - p_{det})^{(N - N_{det})} \\ &\cdot \mu(N_{fal}; \lambda_{fal} W) \cdot \mu(N_{new}; \lambda_{new} W) \end{split}$$





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Recap: Probability of an Assignment Set

- 2. Probability of a specific assignment of measurements
- Such that $M_k = N_{det} + N_{fal} + N_{new}$ holds.
- . This is determined as 1 over the number of combinations

$$\begin{pmatrix} M_k \\ N_{det} \end{pmatrix} \begin{pmatrix} M_k - N_{det} \\ N_{fal} \end{pmatrix} \begin{pmatrix} M_k - N_{det} - N_{fal} \\ N_{new} \end{pmatrix}$$

- 3. Probability of a specific assignment of tracks
 - Given that a track can be either detected or not detected.
- This is determined as 1 over the number of assignments

$$\frac{N!}{(N-N_{det})!} \left(\begin{array}{c} N-N_{det} \\ N_{det} \end{array} \right)$$

⇒ When combining the different parts, many terms cancel out!







Topics of This Lecture

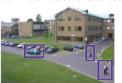
- · Recap: MHT
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Back to Data Association...

· Goal: Match detections across frames





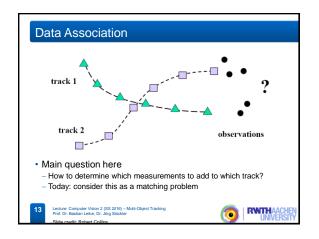


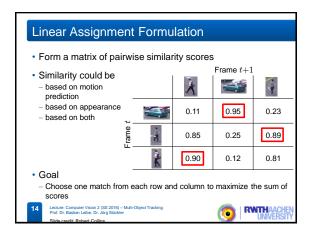


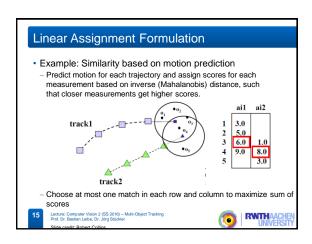


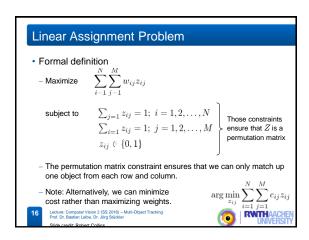


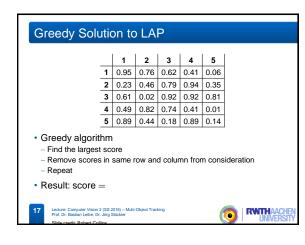


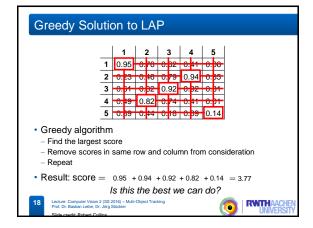


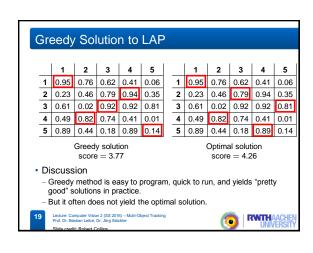


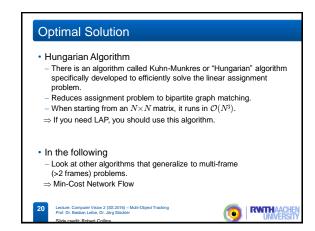


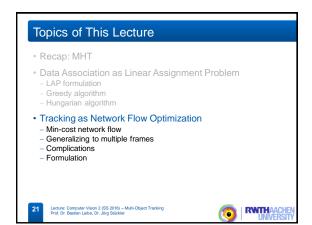


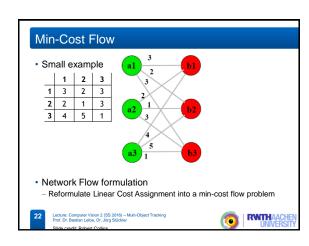


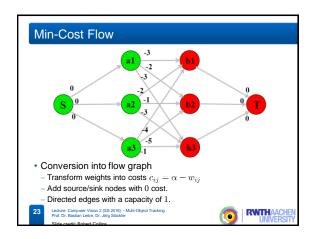


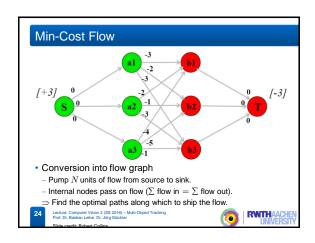


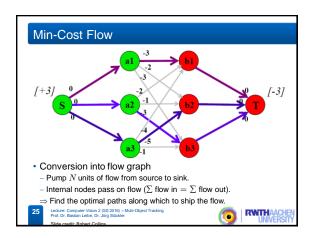


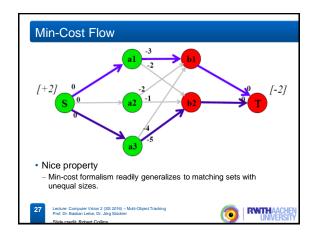


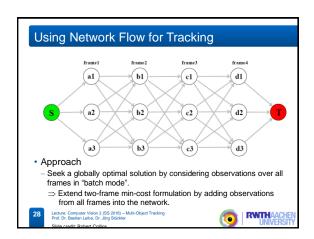


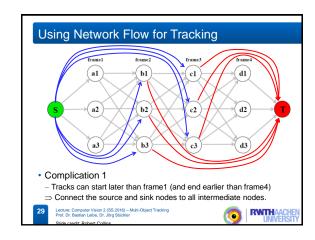


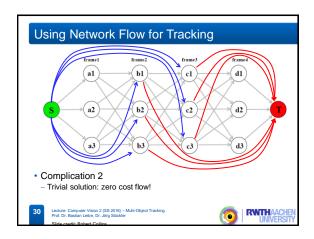


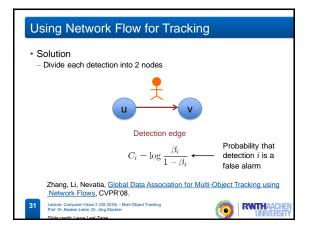


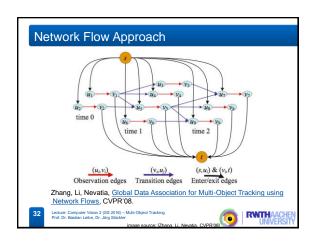


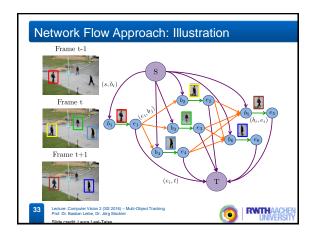


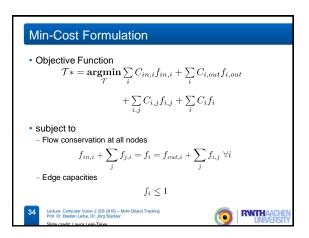


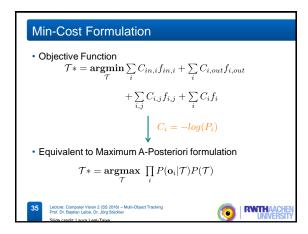


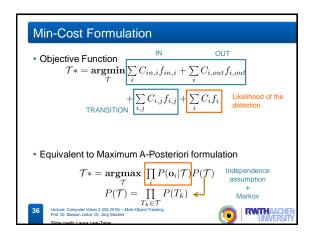


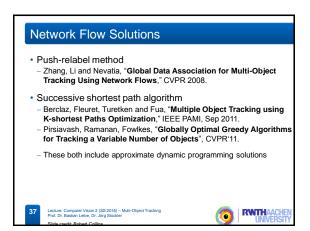












Summary

- · Tracking as network flow optimization
- Dros
- Clear algorithmic framework, equivalence to probabilistic formulation
- Well-understood LP optimization problem, efficient algorithms available
- Globally optimal solution
- Cons / Limitations
- Only applicable to restricted problem setting due to LP formulation
- Not possible to encode exclusion constraints between detections (e.g., to penalize physical overlap)
- Motion model can only draw upon information from pairs of detections (i.e., only zero-velocity model possible, no constant velocity models)
- C_{in} and C_{out} cost terms are quite fiddly to set in practice
- Too low ⇒ fragmentations, too high ⇒ ID switches



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References and Further Reading

- The original network flow tracking paper
- Zhang, Li, Nevatia, Global Data Association for Multi-Object Tracking using Network Flows, CVPR'08.
- Extensions and improvements
- Berclaz, Fleuret, Turetken, Fua, Multiple Object Tracking using K-shortest Paths Optimization, IEEE PAMI, Sep 2011. (code)
- Pirsiavash, Ramanan, Fowlkes, Globally Optimal Greedy Algorithms for Tracking a Variable Number of Objects, CVPR'11.
- A recent extension to incorporate social walking models
 - L. Leal-Taixe, G. Pons-Moll, B. Rosenhahn, <u>Everybody Needs</u> <u>Somebody: Modeling Social and Grouping Behavior on a Linear</u> <u>Programming Multiple People Tracker</u>, ICCV Workshops 2011.



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