Computer Vision 2 – Lecture 9

Multi-Object Tracking II (02.06.2016)

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Content of the Lecture

- Single-Object Tracking
- Bayesian Filtering
 - Kalman Filters, EKF
 - Particle Filters
- Multi-Object Tracking
 - Introduction
 - MHT, (JPDAF)
 - Network Flow Optimization
- Visual Odometry
- Visual SLAM & 3D Reconstruction





Image sources: Andreas Ess

Topics of This Lecture

Recap: Track-Splitting Filter

- Motivation
- Ambiguities
- Multi-Hypothesis Tracking (MHT)
 - Basic idea
 - Hypothesis Generation
 - Assignment

- Measurement Likelihood
- Practical considerations



Recap: Motion Correspondence Ambiguities



- 1. Predictions may not be supported by measurements
 - Have the objects ceased to exist, or are they simply occluded?
- 2. There may be unexpected measurements
 - Newly visible objects, or just noise?
- 3. More than one measurement may match a prediction
 - Which measurement is the correct one (what about the others)?
- 4. A measurement may match to multiple predictions
 - Which object shall the measurement be assigned to?

Δ



Let's Formalize This

- Multi-Object Tracking problem
 - We represent a track by a state vector \mathbf{x} , e.g.,

$$\mathbf{x} = [x, y, v_x, v_y]^T$$

– As the track evolves, we denote its state by the time index k:

$$\mathbf{x}^{(k)} = \left[x^{(k)}, y^{(k)}, v_x^{(k)}, v_y^{(k)} \right]$$

- At each time step, we get a set of observations (measurements)

$$\mathbf{Y}^{(k)} = \left\{ \mathbf{y}_1^{(k)}, \dots, \mathbf{y}_{M_k}^{(k)}
ight\}$$

- We now need to make the data association between tracks

$$\begin{cases} \mathbf{x}_1^{(k)}, \dots, \mathbf{x}_{N_k}^{(k)} \end{cases} \text{and observations} \begin{cases} \mathbf{y}_1^{(k)}, \dots, \mathbf{y}_{M_k}^{(k)} \end{cases} \text{:} \\ z_l^{(k)} = j \text{ iff } \mathbf{y}_j^{(k)} \text{ is associated with } \mathbf{x}_l^{(k)} \end{cases}$$

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Mahalanobis Distance

- Additional notation
 - Our KF state of track \mathbf{x}_l is given by

the prediction $\hat{\mathbf{x}}_{l}^{(k)}$ and covariance $\boldsymbol{\Sigma}_{p,l}^{(k)}$.

– We define the innovation that measurement \mathbf{y}_j brings to track \mathbf{x}_l at time k as $\mathbf{v}_{j,l}^{(k)} = (\mathbf{y}_j^{(k)} - \mathbf{x}_{p,l}^{(k)})$



- With this, we can write the observation likelihood shortly as

$$p(\mathbf{y}_{j}^{(k)}|\mathbf{x}_{l}^{(k)}) \sim \exp\left\{-\frac{1}{2}\mathbf{v}_{j,l}^{(k)^{T}}\boldsymbol{\Sigma}_{p,l}^{(k)^{-1}}\mathbf{v}_{j,l}^{(k)}\right\}$$

- We define the ellipsoidal gating or validation volume as

$$V^{(k)}(\gamma) = \left\{ \mathbf{y} | (\mathbf{y} - \mathbf{x}_{p,l}^{(k)})^T \mathbf{\Sigma}_{p,l}^{(k)^{-1}} (\mathbf{y} - \mathbf{x}_{p,l}^{(k)}) \le \gamma \right\}$$

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Recap: Track-Splitting Filter

Idea

- Instead of assigning the measurement that is currently closest, as in the NN algorithm, select the sequence of measurements that minimizes the *total* Mahalanobis distance over some interval!
- Form a track tree for the different association decisions
- Modified log-likelihood provides the merit of a particular node in the track tree.
- Cost of calculating this is low, since most terms are needed anyway for the Kalman filter.
- Problem
 - The track tree grows exponentially, may generate a very large number of possible tracks that need to be maintained.





Recap: Pruning Strategies

- In order to keep this feasible, need to apply pruning
 - Deleting unlikely tracks
 - May be accomplished by comparing the modified log-likelihood $\lambda(k)$, which has a χ^2 distribution with kn_z degrees of freedom, with a threshold α (set according to χ^2 distribution tables).
 - Problem for long tracks: modified log-likelihood gets dominated by old terms and responds very slowly to new ones.
 - \Rightarrow Use sliding window or exponential decay term.
 - Merging track nodes

- If the state estimates of two track nodes are similar, merge them.
- E.g., if both tracks validate identical subsequent measurements.
- Only keeping the most likely $N \, {\rm tracks}$
 - Rank tracks based on their modified log-likelihood.



Topics of This Lecture

- Recap: Track-Splitting Filter
 - Motivation
 - Ambiguities

• Multi-Hypothesis Tracking (MHT)

- Basic idea
- Hypothesis Generation
- Assignment

- Measurement Likelihood
- Practical considerations



Multi-Hypothesis Tracking (MHT)

- Ideas
 - Again associate sequences of measurements.
 - Evaluate the probabilities of all association hypotheses.
 - For each sequence of measurements (a hypothesized track), a standard KF yields the state estimate and covariance
- Differences to Track-Splitting Filter
 - Instead of forming a track tree, keep a set of hypotheses that generate child hypotheses based on the associations.
 - After each hypothesis generation step, merge and prune the current hypothesis set to keep the approach feasible.
 - Integrate track generation into the assignment process.

D. Reid, <u>An Algorithm for Tracking Multiple Targets</u>, IEEE Trans. Automatic Control, Vol. 24(6), pp. 843-854, 1979.



Target vs. Measurement Orientation

- Target-oriented approaches
 - Evaluate the probability that a measurement belongs to an established target.
- Measurement-oriented approaches
 - Evaluate the probability that an established target or a new target gave rise to a certain measurement sequence.
 - This makes it possible to include track initiation of new targets within the algorithmic framework.
- MHT
 - Measurement-oriented
 - Handles track initialization and termination





Challenge: Exponential Complexity

Strategy

- Generate all possible hypotheses and then depend on pruning these hypotheses to avoid the combinatorial explosion.
 - \Rightarrow Exhaustive search
- Tree data structures are used to keep this search efficient
- Commonly used pruning techniques
 - Clustering to reduce the combinatorial complexity
 - Pruning of low-probability hypotheses
 - N-scan pruning
 - Select a single best hypothesis at frame K and prune all tracks that do not share the predecessor track at the (K-N)th frame.
 - Merging of similar hypotheses



Multi-Hypothesis Tracking (MHT)

Ideas

- Instead of forming a track tree, keep a set of hypotheses that generate child hypotheses based on the associations.
- Enforce exclusion constraints between tracks and measurements in the assignment.
- Integrate track generation into the assignment process.
- After hypothesis generation, merge and prune the current hypothesis set.



Raw Sensor Data

D. Reid, <u>An Algorithm for Tracking Multiple Targets</u>, IEEE Trans. Automatic Control, Vol. 24(6), pp. 843-854, 1979.

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Hypothesis Generation

- Formalization
 - Set of hypotheses at time k: $\mathbf{\Omega}^{(\mathbf{k})} = \left\{ \Omega_{j}^{(k)} \right\}$
 - This set is obtained from $\Omega^{(k-1)}$ and the latest set of measurements

$$\mathbf{Y}^{(k)} = \left\{ \mathbf{y}_1^{(k)}, \dots, \mathbf{y}_{M_k}^{(k)}
ight\}$$

- The set $\Omega^{(k)}$ is generated from $\Omega^{(k-1)}$ by performing all feasible associations between the old hypotheses and the new measurements $\mathbf{Y}^{(k)}$.
- Feasible associations can be
 - A continuation of a previous track
 - A false alarm
 - A new target





Hypothesis Matrix

Visualize feasible associations by a hypothesis matrix

 $\Theta = \begin{bmatrix} \mathbf{x}_1 & \mathbf{x}_2 \mathbf{x}_{fa} \mathbf{x}_{nt} \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{y}_1 \\ \mathbf{y}_2 \\ \mathbf{y}_3 \\ \mathbf{y}_4 \end{bmatrix}$

Interpretation

- Columns represent tracked objects
- Rows represent measurements
- A non-zero element at matrix position (i,j) denotes that measurement
 - \mathbf{y}_i is contained in the validation region of track \mathbf{x}_j .
- Extra column \mathbf{x}_{fa} for association as false alarm.
- Extra column \mathbf{x}_{nt} for association as *new track*.





Assignments

- Turning feasible associations into assignments
 - For each feasible association, we generate a new hypothesis.
 - Let $\Omega_j^{(k)}$ be the *j*-th hypothesis at time *k* and $\Omega_{p(j)}^{(k-1)}$ be the parent hypothesis from which $\Omega_j^{(k)}$ was derived.
 - Let $Z_j^{(k)}$ denote the set of assignments that gives rise to $\Omega_j^{(k)}$.
 - Assignments are again best visualized in matrix form

Z_{j}	\mathbf{x}_1	\mathbf{x}_2	\mathbf{x}_{fa}	\mathbf{x}_{nt}
\mathbf{y}_1	0	0	1	0
\mathbf{y}_2	1	0	0	0
\mathbf{y}_3	0	1	0	0
\mathbf{y}_4	0	0	0	1



Assignments



- Impose constraints
 - A measurement can originate from only one object.
 - \Rightarrow Any row has only a single non-zero value.

- An object can have at most one associated measurement per time step.

 \Rightarrow Any column has only a single non-zero value, except for \mathbf{x}_{fa} , \mathbf{x}_{nt}



Calculating Hypothesis Probabilities

- Probabilistic formulation
 - It is straightforward to enumerate all possible assignments.
 - However, we also need to calculate the probability of each child hypothesis.
 - This is done recursively:



Measurement Likelihood

Use KF prediction

- Assume that a measurement $\mathbf{y}_i^{(k)}$ associated to a track \mathbf{x}_j has a Gaussian pdf centered around the measurement prediction $\hat{\mathbf{x}}_j^{(k)}$ with innovation covariance $\widehat{\boldsymbol{\Sigma}}_j^{(k)}$.
- Further assume that the pdf of a measurement belonging to a new track or false alarm is uniform in the observation volume W (the sensor's field-of-view) with probability W^{-1} .
- Thus, the measurement likelihood can be expressed as

$$p\left(\mathbf{Y}^{(k)}|Z_{j}^{(k)},\Omega_{p(j)}^{(k-1)}\right) = \prod_{i=1}^{M_{k}} \mathcal{N}\left(\mathbf{y}_{i}^{(k)};\hat{\mathbf{x}}_{j},\widehat{\boldsymbol{\Sigma}}_{j}^{(k)}\right)^{\delta_{i}} W^{-(1-\delta_{i})}$$
$$= W^{-(N_{fal}+N_{new})} \prod_{i=1}^{M_{k}} \mathcal{N}\left(\mathbf{y}_{i}^{(k)};\hat{\mathbf{x}}_{j},\widehat{\boldsymbol{\Sigma}}_{j}^{(k)}\right)^{\delta_{i}}$$
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Probability of an Assignment Set

$$p(Z_j^{(k)}|\Omega_{p(j)}^{(k-1)})$$

- Composed of three terms
 - 1. Probability of the number of tracks $N_{det},\,N_{fal},\,N_{new}$
 - Assumption 1: N_{det} follows a binomial distribution

$$p(N_{det}|\Omega_{p(j)}^{(k-1)}) = \binom{N}{N_{det}} p_{det}^{N_{det}} (1 - p_{det})^{(N-N_{det})}$$

where N is the number of tracks in the parent hypothesis

- Assumption 2: N_{fal} and N_{new} both follow a Poisson distribution with expected number of events $\lambda_{fal}W$ and $\lambda_{new}W$

$$p(N_{det}, N_{fal}, N_{new} | \Omega_{p(j)}^{(k-1)}) = \binom{N}{N_{det}} p_{det}^{N_{det}} (1 - p_{det})^{(N-N_{det})}$$

 $\cdot \mu(N_{fal}; \lambda_{fal}W) \cdot \mu(N_{new}; \lambda_{new}W)$

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Probability of an Assignment Set

- 2. Probability of a specific assignment of measurements
 - Such that $M_k = N_{det} + N_{fal} + N_{new}$ holds.
 - This is determined as $1 \ {\rm over}$ the number of combinations

$$\begin{pmatrix} M_k \\ N_{det} \end{pmatrix} \begin{pmatrix} M_k - N_{det} \\ N_{fal} \end{pmatrix} \begin{pmatrix} M_k - N_{det} - N_{fal} \\ N_{new} \end{pmatrix}$$

- 3. Probability of a specific assignment of tracks
 - Given that a track can be either detected or not detected.
 - This is determined as 1 over the number of assignments

$$\frac{N!}{(N-N_{det})!} \left(\begin{array}{c} N-N_{det} \\ N_{det} \end{array} \right)$$

 \Rightarrow When combining the different parts, many terms cancel out!



Measurement Likelihood

- Combining all the different parts
 - Nice property: many terms cancel out!
 - (Derivation left as exercise)
 - \Rightarrow The final probability $p\left(\Omega_{j}^{(k)}|\mathbf{Y}^{(k)}\right)$ can be computed in a very simple form.
 - This was the main contribution by Reid and it is one of the reasons why the approach is still popular.
- Practical issues

- Exponential complexity remains
- Heuristic pruning strategies must be applied to contain the growth of the hypothesis set.
- E.g., dividing hypotheses into spatially disjoint clusters.



Laser-based Leg Tracking using MHT



K. Arras, S. Grzonka, M. Luber, W. Burgard, <u>Efficient People Tracking in Laser Range</u> <u>Data using a Multi-Hypothesis Leg-Tracker with Adaptive Occlusion Probabilities</u>, ICRA'08.







video source: Social Robotics Lab, Univ. Freiburg

Laser-based People Tracking using MHT

Multi Hypothesis Tracking of People

Matthias Luber, Gian Diego Tipaldi and Kai O. Arras

Laser-baser People Tracking using MHT (Inner city of Freiburg, Germany) Results projected onto video data.





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video source: Social Robotics Lab, Univ. Freiburg

References and Further Reading

- A good tutorial on Data Association
 - I.J. Cox. <u>A Review of Statistical Data Association Techniques for Motion</u> <u>Correspondence</u>. In *International Journal of Computer Vision*, Vol. 10(1), pp. 53-66, 1993.
- Reid's original MHT paper
 - D. Reid, <u>An Algorithm for Tracking Multiple Targets</u>, IEEE Trans. Automatic Control, Vol. 24(6), pp. 843-854, 1979.

