

Computer Vision 2 – Lecture 8

Multi-Object Tracking (30.05.2016)

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Content of the Lecture

- Single-Object Tracking
- Bayesian Filtering
 - Kalman Filters, EKF
 - Particle Filters
- Multi-Object Tracking
 - Introduction
 - MHT, JPDAF
 - Network Flow Optimization
- Visual Odometry
- Visual SLAM & 3D Reconstruction

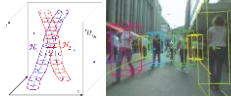

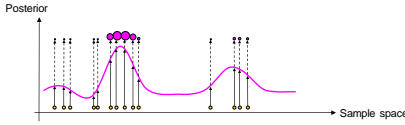


Image sources: Andreas Ess


2
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Recap: Particle Filtering

- Many variations, one general concept:
 - Represent the posterior pdf by a set of randomly chosen weighted samples (particles)



- Randomly Chosen = Monte Carlo (MC)
- As the number of samples become very large – the characterization becomes an equivalent representation of the true pdf.

3
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Recap: Sequential Importance Sampling

function $[\{\mathbf{x}_t^i, w_t^i\}_{i=1}^N] = SIS [\{\mathbf{x}_{t-1}^i, w_{t-1}^i\}_{i=1}^N, \mathbf{y}_t]$

$\eta = 0$ Initialize

for $i = 1:N$

$\mathbf{x}_t^i \sim q(\mathbf{x}_t | \mathbf{x}_{t-1}^i, \mathbf{y}_t)$ Sample from proposal pdf

$w_t^i = w_{t-1}^i \frac{p(\mathbf{y}_t | \mathbf{x}_t^i) p(\mathbf{x}_t^i | \mathbf{x}_{t-1}^i)}{q(\mathbf{x}_t | \mathbf{x}_{t-1}^i, \mathbf{y}_t)}$ Update weights


$\eta = \eta + w_t^i$ Update norm. factor

end

for $i = 1:N$

$w_t^i = w_t^i / \eta$ Normalize weights

end

4
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end

for $i = 1:N$

$w_t^i = w_t^i / \eta$ Normalize weights

end

For a concrete algorithm, we need to define the importance density $q(\cdot, \cdot)$!

5
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Recap: SIS Algorithm with Transitional Prior

function $[\{\mathbf{x}_t^i, w_t^i\}_{i=1}^N] = SIS [\{\mathbf{x}_{t-1}^i, w_{t-1}^i\}_{i=1}^N, \mathbf{y}_t]$

$\eta = 0$ Initialize

for $i = 1:N$

$\mathbf{x}_t^i \sim p(\mathbf{x}_t | \mathbf{x}_{t-1}^i)$ Sample from proposal pdf

$w_t^i = w_{t-1}^i p(\mathbf{y}_t | \mathbf{x}_t^i)$ Update weights

$\eta = \eta + w_t^i$ Update norm. factor


end

for $i = 1:N$

$w_t^i = w_t^i / \eta$ Normalize weights

end

Transitional prior
 $q(\mathbf{x}_t | \mathbf{x}_{t-1}^i, \mathbf{y}_t) = p(\mathbf{x}_t | \mathbf{x}_{t-1}^i)$

6
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Recap: Resampling

- Degeneracy problem with SIS
 - After a few iterations, most particles have negligible weights.
 - Large computational effort for updating particles with very small contribution to $p(\mathbf{x}_t | \mathbf{y}_{1:t})$.
- Idea: Resampling
 - Eliminate particles with low importance weights and increase the number of particles with high importance weight.
$$\{\mathbf{x}_t^i, w_t^i\}_{i=1}^N \rightarrow \left\{ \mathbf{x}_t^{i*}, \frac{1}{N} \right\}_{i=1}^N$$
 - The new set is generated by sampling with replacement from the discrete representation of $p(\mathbf{x}_t | \mathbf{y}_{1:t})$ such that

$$Pr \left\{ \mathbf{x}_t^{i*} = \mathbf{x}_t^j \right\} = w_t^j$$

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Recap: Efficient Resampling Approach

- From Arulampalam paper:

Algorithm 2: Resampling Algorithm
 $[\{\mathbf{x}_t^i, w_t^i, \varphi^i\}_{i=1}^{N_s}] = \text{RESAMPLE} [\{\mathbf{x}_{t-1}^i, w_{t-1}^i\}_{i=1}^{N_s}]$

 - Initialize the CDF: $c_1 = 0$
 - FOR $i = 2: N_s$
 - Construct CDF: $c_i = c_{i-1} + w_{t-1}^i$
 - END FOR
 - Start at the bottom of the CDF: $i = 1$
 - Draw a starting point: $u_1 \sim \mathcal{U}[0, N_s^{-1}]$
 - FOR $j = 1: N_s$
 - Move along the CDF: $w_j = u_1 + N_s^{-1}(j-1)$
 - WHILE $w_j > c_i$
 - * $i = i + 1$
 - END WHILE
 - Assign sample: $\mathbf{x}_t^{j*} = \mathbf{x}_{t-1}^i$
 - Assign weight: $w_t^{j*} = N_s^{-1}$
 - Assign parent: $\varphi^j = i$
 - END FOR

Basic idea: choose one initial small random number; deterministically sample the rest by "crawling" up the cdf. This is $\mathcal{O}(N)$!

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 Slide adapted from Robert Collins

Recap: Generic Particle Filter

```

function  $[\{\mathbf{x}_t^i, w_t^i\}_{i=1}^N] = PF [\{\mathbf{x}_{t-1}^i, w_{t-1}^i\}_{i=1}^N, \mathbf{y}_t]$ 
    Apply SIS filtering  $[\{\mathbf{x}_t^i, w_t^i\}_{i=1}^N] = SIS [\{\mathbf{x}_{t-1}^i, w_{t-1}^i\}_{i=1}^N, \mathbf{y}_t]$ 
    Calculate  $N_{eff}$ 
    if  $N_{eff} < N_{thr}$ 
         $[\{\mathbf{x}_t^i, w_t^i\}_{i=1}^N] = \text{RESAMPLE} [\{\mathbf{x}_t^i, w_t^i\}_{i=1}^N]$ 
    end
    
```

- We can also apply resampling selectively
 - Only resample when it is needed, i.e., N_{eff} is too low.
 - > Avoids drift when the tracked state is stationary.

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Sampling-Importance-Resampling (SIR)

```

function  $[\mathcal{X}_t] = SIR [\mathcal{X}_{t-1}, \mathbf{y}_t]$ 
     $\bar{\mathcal{X}}_t = \mathcal{X}_t = \emptyset$  Initialize
    for  $i = 1:N$ 
        Sample  $\mathbf{x}_t^i \sim p(\mathbf{x}_t | \mathbf{x}_{t-1}^i)$  Generate new samples
         $w_t^i = p(\mathbf{y}_t | \mathbf{x}_t^i)$  Update weights
    end
    for  $i = 1:N$ 
        Draw  $i$  with probability  $\propto w_t^i$  Resample
        Add  $\mathbf{x}_t^i$  to  $\mathcal{X}_t$ 
    end
    
```

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Sampling-Importance-Resampling (SIR)

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function  $[\mathcal{X}_t] = SIR [\mathcal{X}_{t-1}, \mathbf{y}_t]$ 
     $\bar{\mathcal{X}}_t = \mathcal{X}_t = \emptyset$ 
    for  $i = 1:N$ 
        Sample  $\mathbf{x}_t^i \sim p(\mathbf{x}_t | \mathbf{x}_{t-1}^i)$ 
         $w_t^i = p(\mathbf{y}_t | \mathbf{x}_t^i)$ 
    end
    for  $i = 1:N$ 
        Draw  $i$  with probability  $\propto w_t^i$ 
        Add  $\mathbf{x}_t^i$  to  $\mathcal{X}_t$ 
    end
    
```

Important property:

Particles are distributed according to pdf from previous time step.

Particles are distributed according to posterior from this time step.

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Today: Multi-Object Tracking




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 (Ess, Leibe, Schindler, Van Gool, CVPR08; ICRA09; PAMI09)

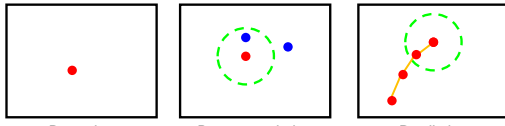
Topics of This Lecture

- Multi-Object Tracking
 - Motivation
 - Ambiguities
- Simple Approaches
 - Gating
 - Mahalanobis distance
 - Nearest-Neighbor Filter
- Track-Splitting Filter
 - Derivation
 - Properties
- Outlook

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Elements of Tracking



Detection Data association Prediction

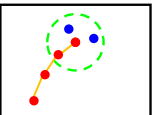
- Detection
 - Where are candidate objects? Lecture 4
- Data association
 - Which detection corresponds to which object? Today's topic
- Prediction
 - Where will the tracked object be in the next time step? Lectures 5-7

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Motion Correspondence

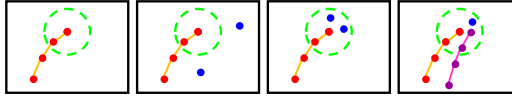
- Motion correspondence problem
 - Do two measurements at different times originate from the same object?
- Why is it hard?
 - First make predictions for the expected locations of the current set of objects
 - Match predictions to actual measurements
 - This is where ambiguities may arise...



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Motion Correspondence Ambiguities



1. Predictions may not be supported by measurements
 - Have the objects ceased to exist, or are they simply occluded?
2. There may be unexpected measurements
 - Newly visible objects, or just noise?
3. More than one measurement may match a prediction
 - Which measurement is the correct one (what about the others)?
4. A measurement may match to multiple predictions
 - Which object shall the measurement be assigned to?


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Let's Formalize This

- Multi-Object Tracking problem
 - We represent a track by a state vector \mathbf{x} , e.g.,

$$\mathbf{x} = [x, y, v_x, v_y]^T$$
 - As the track evolves, we denote its state by the time index k :


$$\mathbf{x}^{(k)} = [x^{(k)}, y^{(k)}, v_x^{(k)}, v_y^{(k)}]^T$$
 - At each time step, we get a set of observations (measurements)

$$\mathbf{Y}^{(k)} = \{\mathbf{y}_1^{(k)}, \dots, \mathbf{y}_{M_k}^{(k)}\}$$
 - We now need to make the data association between tracks

$$\{\mathbf{x}_1^{(k)}, \dots, \mathbf{x}_{N_k}^{(k)}\}$$
 and observations $\{\mathbf{y}_1^{(k)}, \dots, \mathbf{y}_{M_k}^{(k)}\}$:

$$z_j^{(k)} = j \text{ iff } \mathbf{y}_j^{(k)} \text{ is associated with } \mathbf{x}_i^{(k)}$$

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Reducing Ambiguities: Simple Approaches

- Gating
 - Only consider measurements within a certain area around the predicted location.
 - ⇒ Large gain in efficiency, since only a small region needs to be searched
- Nearest-Neighbor Filter
 - Among the candidates in the gating region, only take the one closest to the prediction \mathbf{x}_p
 - $$z_l^{(k)} = \arg \min_j (\mathbf{x}_{p,l}^{(k)} - \mathbf{y}_j^{(k)})^T (\mathbf{x}_{p,l}^{(k)} - \mathbf{y}_j^{(k)})$$
 - Better: the one most likely under a Gaussian prediction model
 - $$z_l^{(k)} = \arg \max_j \mathcal{N}(\mathbf{y}_j^{(k)}; \mathbf{x}_{p,l}^{(k)}, \Sigma_{p,l}^{(k)})$$
 - which is equivalent to taking the Mahalanobis distance
 - $$z_l = \arg \min_j (\mathbf{x}_{p,l} - \mathbf{y}_j)^T \Sigma_{p,l}^{-1} (\mathbf{x}_{p,l} - \mathbf{y}_j)$$

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Gating with Mahalanobis Distance

- Recall: Kalman filter
 - Provides exactly the quantities necessary to perform this
 - Predicted mean location \mathbf{x}_p
 - Prediction covariance Σ_p
 - The Kalman filter prediction covariance also defines a useful gating area.
 - ⇒ E.g., choose the gating area size such that 95% of the probability mass is covered.
- Side note
 - The Mahalanobis distance is χ^2 distributed with the number of degrees of freedom n_x equal to the dimension of \mathbf{x} .
 - For a given probability bound, the corresponding threshold on the Mahalanobis distance can be got from χ^2 distribution tables.

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Mahalanobis Distance

- Additional notation
 - Our KF state of track \mathbf{x}_i is given by the prediction $\hat{\mathbf{x}}_i^{(k)}$ and covariance $\Sigma_{p,i}^{(k)}$
 - We define the innovation that measurement \mathbf{y}_j brings to track \mathbf{x}_i at time k as
 - $$\mathbf{v}_{j,i}^{(k)} = (\mathbf{y}_j^{(k)} - \mathbf{x}_{p,i}^{(k)})$$
 - With this, we can write the observation likelihood shortly as
 - $$p(\mathbf{y}_j^{(k)} | \mathbf{x}_i^{(k)}) \sim \exp \left\{ -\frac{1}{2} \mathbf{v}_{j,i}^{(k)T} \Sigma_{p,i}^{(k)-1} \mathbf{v}_{j,i}^{(k)} \right\}$$
 - We define the ellipsoidal gating or validation volume as
 - $$V^{(k)}(\gamma) = \left\{ \mathbf{y} | (\mathbf{y} - \mathbf{x}_{p,i}^{(k)})^T \Sigma_{p,i}^{(k)-1} (\mathbf{y} - \mathbf{x}_{p,i}^{(k)}) \leq \gamma \right\}$$

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Problems with NN Assignment

- Limitations
 - For NN assignments, there is always a finite chance that the association is incorrect, which can lead to serious effects.
 - ⇒ If a Kalman filter is used, a misassigned measurement may lead the filter to lose track of its target.
 - The NN filter makes assignment decisions only based on the current frame.
 - More information is available by examining subsequent images.
 - ⇒ Let's make use of this information by postponing the decision process until a future frame will resolve the ambiguity...

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Track-Splitting Filter

- Idea
 - Problem with NN filter was hard assignment.
 - Rather than arbitrarily assigning the closest measurement, form a tree.
 - Branches denote alternate assignments.
 - No assignment decision is made at this stage!
 - ⇒ Decisions are postponed until additional measurements have been gathered...
- Potential problems?
 - Track trees can quickly become very large due to combinatorial explosion.
 - ⇒ We need some measure of the likelihood of a track, so that we can prune the tree!

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Track Likelihoods

Expressing track likelihoods

- Given a track l , denote by $\theta_{k,l}$ the event that the sequence of assignments

$$Z_{k,l} = \{z_{i_1,l}^{(1)}, \dots, z_{i_k,l}^{(k)}\}$$

from time 1 to k originate from the same object.

- The likelihood of $\theta_{k,l}$ is the joint probability over all observations in the track

$$L(\theta_{k,l}) = \prod_{j=1}^k p(z_{i_j,l}^{(j)} | Z_{(j-1),l}, \theta_{k,l})$$

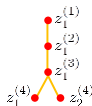
- If we assume Gaussian observation likelihoods, this becomes

$$L(\theta_{k,l}) = \prod_{j=1}^k \frac{1}{(2\pi)^{\frac{d}{2}} |\Sigma_l^{(j)}|^{\frac{1}{2}}} \exp \left[-\frac{1}{2} \sum_{j=1}^k \mathbf{v}_{i_j,l}^{(j)T} \Sigma_l^{(j)-1} \mathbf{v}_{i_j,l}^{(j)} \right]$$

25

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Track Likelihoods (2)

Starting from the likelihood

$$L(\theta_{k,l}) = \prod_{j=1}^k \frac{1}{(2\pi)^{\frac{d}{2}} |\Sigma_l^{(j)}|^{\frac{1}{2}}} \exp \left[-\frac{1}{2} \sum_{j=1}^k \mathbf{v}_{i_j,l}^{(j)T} \Sigma_l^{(j)-1} \mathbf{v}_{i_j,l}^{(j)} \right]$$

- Define the **modified log-likelihood** λ_l for track l as

$$\begin{aligned} \lambda_l(k) &= -2 \log \left[\frac{L(\theta_{k,l})}{\prod_{j=1}^k (2\pi)^{-\frac{d}{2}} |\Sigma_l^{(j)}|^{-\frac{1}{2}}} \right] \\ &= \sum_{j=1}^k \mathbf{v}_{i_j,l}^{(j)T} \Sigma_l^{(j)-1} \mathbf{v}_{i_j,l}^{(j)} \\ &= \lambda_l(k-1) + \mathbf{v}_{i_k,l}^{(k)T} \Sigma_l^{(k)-1} \mathbf{v}_{i_k,l}^{(k)} \end{aligned}$$

- Recursive calculation, sum of Mahalanobis distances of all the measurements assigned to track l .

26

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Track-Splitting Filter

Effect

- Instead of assigning the measurement that is currently closest, as in the NN algorithm, we can select the *sequence* of measurements that minimizes the *total* Mahalanobis distance over some interval!

- Modified log-likelihood provides the merit of a particular node in the track tree.
- Cost of calculating this is low, since most terms are needed anyway for the Kalman filter.

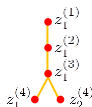
Problem

- The track tree grows exponentially, may generate a very large number of possible tracks that need to be maintained.

27

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Pruning Strategies

- In order to keep this feasible, need to apply pruning

- Deleting unlikely tracks
 - May be accomplished by comparing the modified log-likelihood $\lambda(k)$, which has a χ^2 distribution with km_z degrees of freedom, with a threshold α (set according to χ^2 distribution tables).
 - Problem for long tracks: modified log-likelihood gets dominated by old terms and responds very slowly to new ones.
 - Use sliding window or exponential decay term.
- Merging track nodes
 - If the state estimates of two track nodes are similar, merge them.
 - E.g., if both tracks validate identical subsequent measurements.
- Only keeping the most likely N tracks
 - Rank tracks based on their modified log-likelihood.

28

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Summary: Track-Splitting Filter

Properties

- Very old algorithm
 - P. Smith, G. Buechler, A Branching Algorithm for Discriminating and Tracking Multiple Objects, IEEE Trans. Automatic Control, Vol. 20, pp. 101-104, 1975.
- Improvement over NN assignment.
- Assignment decisions are delayed until more information is available.

Many problems remain

- Exponential complexity, heuristic pruning needed.
 - Merging of track nodes is necessary, because tracks may share measurements, which is physically unrealistic.
- ⇒ Would need to add exclusion constraints such that each measurement may only belong to a single track.
- ⇒ Impossible in this framework...

29

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30

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Outlook for the Next Lectures

- More powerful approaches
 - Multi-Hypothesis Tracking (MHT)
 - Well-suited for KF, EKF approaches [Reid, 1979]
 - Joint Probabilistic Data Association Filters (JPDAF)
 - Well-suited for PF approaches [Fortmann, 1983]
- Data association as convex optimization problem
 - Bipartite Graph Matching (Hungarian algorithm)
 - Network Flow Optimization
 ⇒ Efficient, globally optimal solutions for subclass of problems.

31

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References and Further Reading

- A good tutorial on Data Association
 - I.J. Cox. [A Review of Statistical Data Association Techniques for Motion Correspondence](#). In *International Journal of Computer Vision*, Vol. 10(1), pp. 53-66, 1993.

32

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