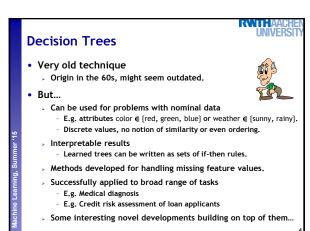
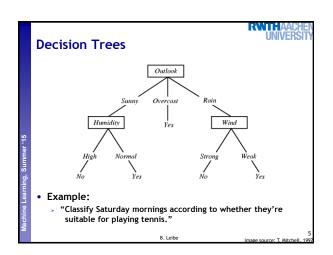
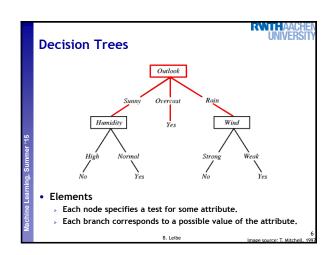


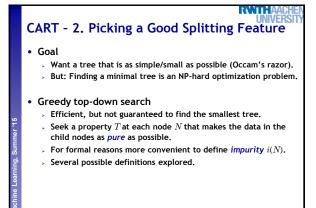
Topics of This Lecture • Decision Trees • Main concepts • Randomized Decision Trees • Randomized attribute selection • Random Forests • Bootstrap sampling • Ensemble of randomized trees • Posterior sum combination • Analysis • Extremely randomized trees • Random attribute selection

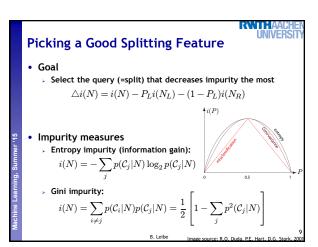


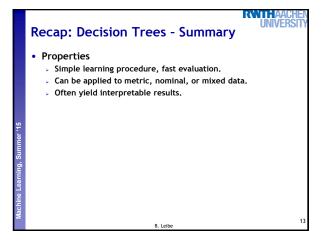


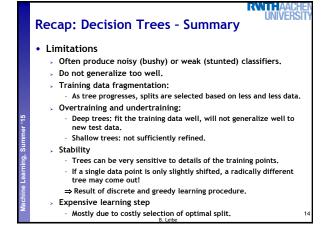


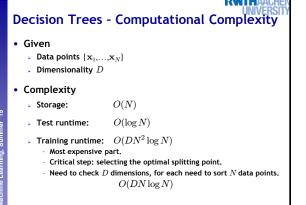
CART Framework • Six general questions 1. Binary or multi-valued problem? - I.e. how many splits should there be at each node? 2. Which property should be tested at a node? - I.e. how to select the query attribute? 3. When should a node be declared a leaf? - I.e. when to stop growing the tree? 4. How can a grown tree be simplified or pruned? - Goal: reduce overfitting. 5. How to deal with impure nodes? - I.e. when the data itself is ambiguous. 6. How should missing attributes be handled?



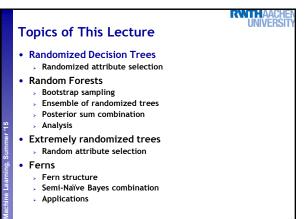


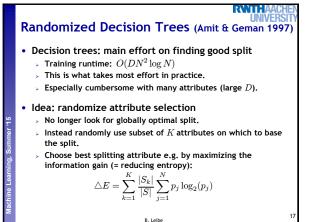


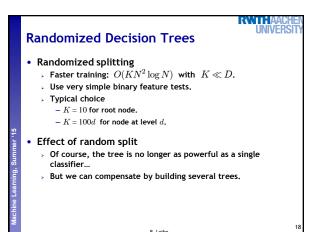


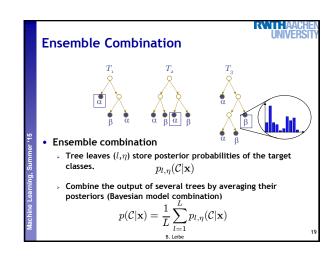


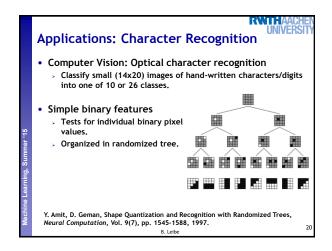
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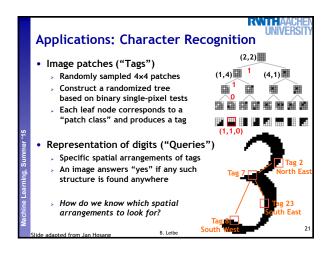


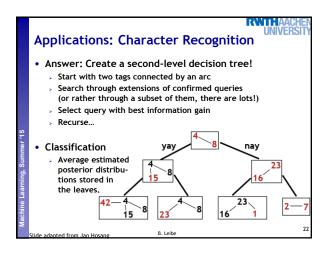


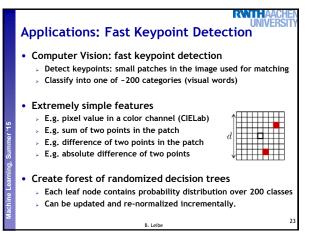


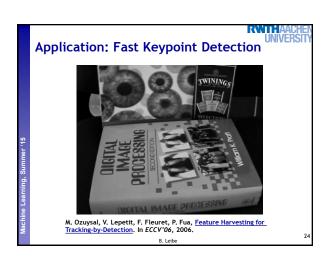


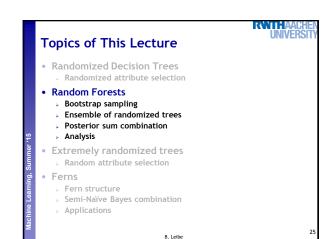


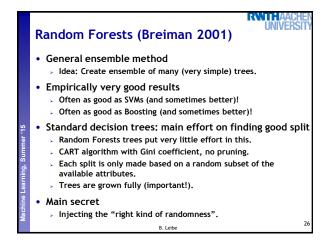


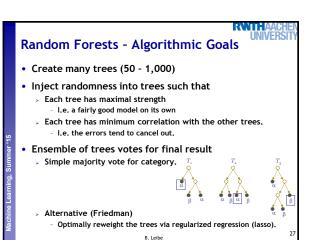








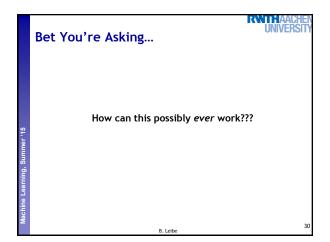


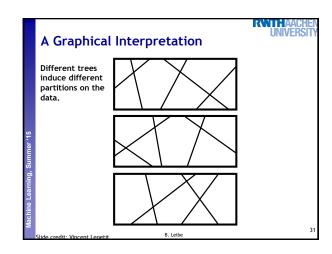


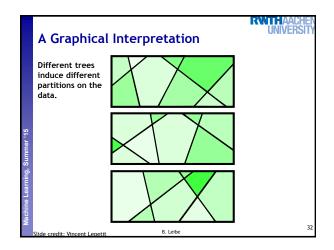
Random Forests - Injecting Randomness (1) • Bootstrap sampling process • Select a training set by choosing N times with replacement from all N available training examples. ⇒ On average, each tree is grown on only -63% of the original training data. • Remaining 37% "out-of-bag" (OOB) data used for validation. • Provides ongoing assessment of model performance in the current tree. • Allows fitting to small data sets without explicitly holding back any data for testing. • Error estimate is unbiased and behaves as if we had an independent test sample of the same size as the training sample.

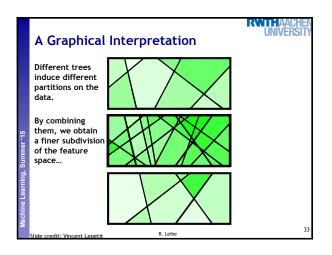
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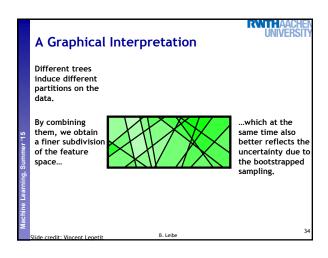
Random Forests - Injecting Randomness (2) • Random attribute selection • For each node, randomly choose subset of K attributes on which the split is based (typically K = √N_f). ⇒ Faster training procedure • Need to test only few attributes. • Minimizes inter-tree dependence • Reduce correlation between different trees. • Each tree is grown to maximal size and is left unpruned • Trees are deliberately overfit ⇒ Become some form of nearest-neighbor predictor.

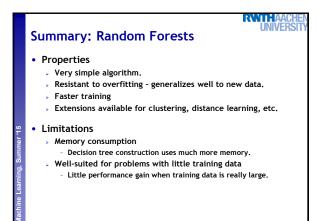


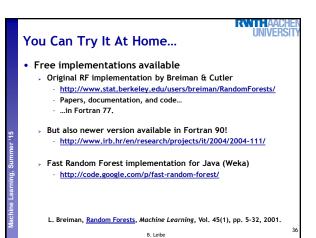


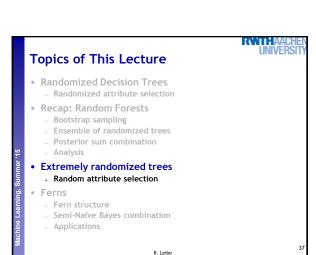


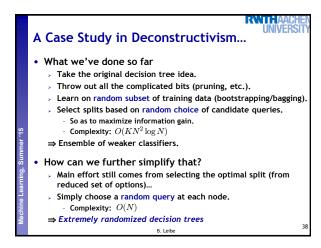


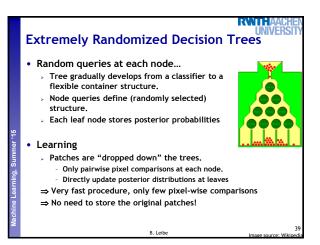


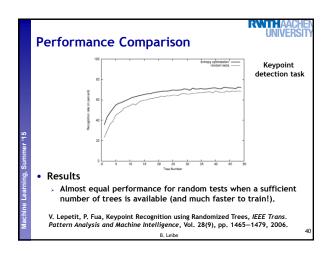


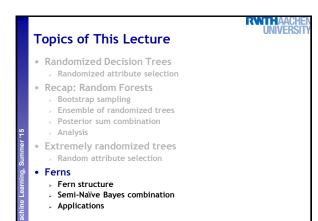


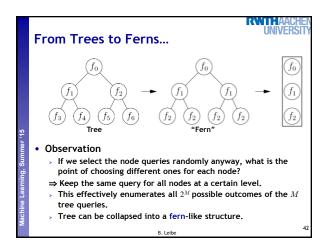


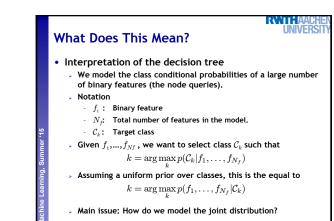




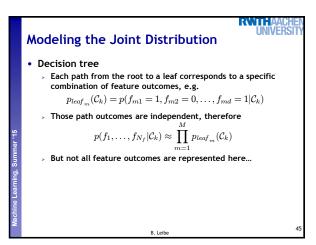


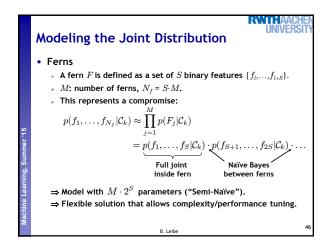


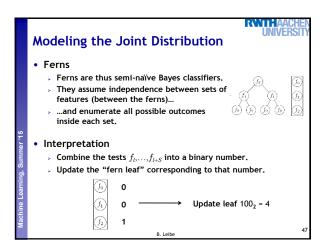


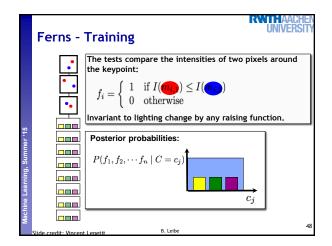


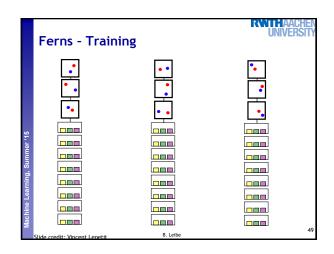
Modeling the Joint Distribution • Full Joint • Model all correlations between features $p(f_1,\ldots,f_{N_f}|\mathcal{C}_k)$ \Rightarrow Model with 2^{N_f} parameters, not feasible to learn. • Naïve Bayes classifier • Assumption: all features are independent. $p(f_1,\ldots,f_{N_f}|\mathcal{C}_k) = \prod_{i=1}^{N_f} p(f_i|\mathcal{C}_k)$ \Rightarrow Too simplistic, assumption does not really hold! \Rightarrow Naïve Bayes model ignores correlation between features.

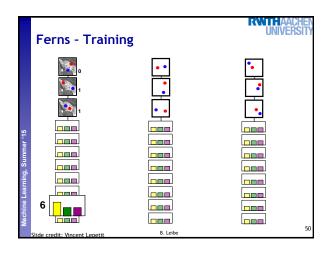


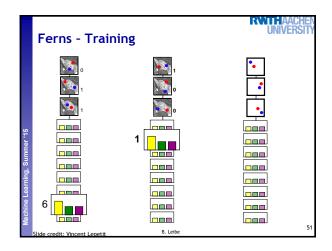


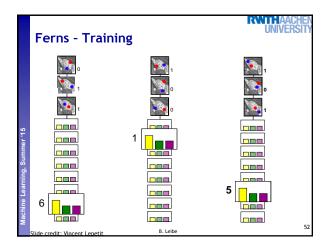


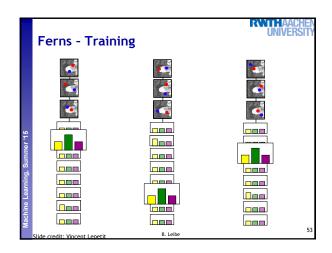


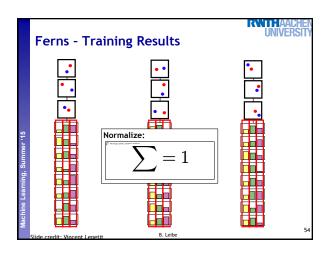


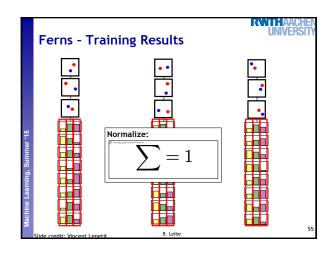


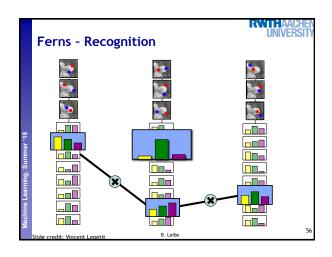


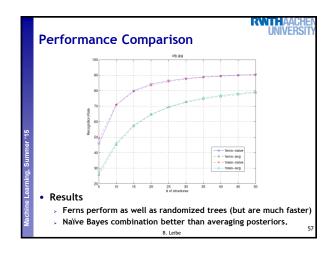


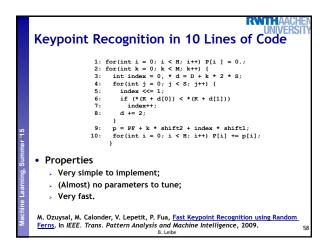


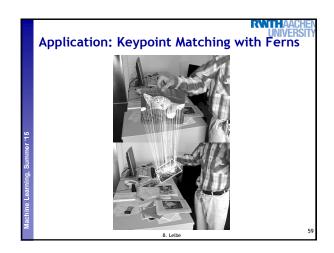




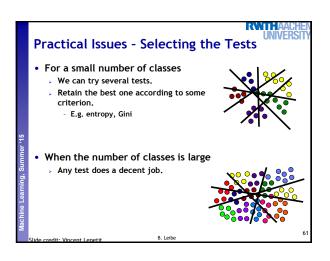


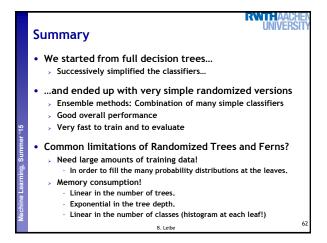












References and Further Reading • Very recent topics, not covered sufficiently well in books yet... • The original papers for Randomized Trees • Y. Amit, D. Geman, Shape Quantization and Recognition with Randomized Trees, Neural Computation, Vol. 9(7), pp. 1545-1588, 1997. • V. Lepetit, P. Fua, Keypoint Recognition using Randomized Trees, IEEE Trans. Pattern Analysis and Machine Intelligence, Vol. 28(9), pp. 1465-1479, 2006. • The original paper for Random Forests: • L. Breiman, Random Forests, Machine Learning, Vol. 45(1), pp. 5-32, 2001. • The papers for Ferns: • M. Ozuysal, M. Calonder, V. Lepetit, P. Fua, East Keypoint Recognition using Random Ferns. In IEEE. Trans. Pattern Analysis and Machine Intelligence, 2009. • D. Wagner, G. Reitmayr, A. Mulloni, T. Drummond, D. Schmalstieg, Pose Tracking from Natural Features on Mobile Phones. In ISMAR 2008.