RWTHAACHEN UNIVERSITY

Computer Vision II - Lecture 10

Particle Filters (The Gritty Details)

27.05.2014

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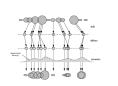
Announcement

- Problems with exam registration fixed...
 - ...for Master CS and Master SSE
 - You should now be able to register
 - > I extended the registration deadline until this Friday (30.05.)
- Exchange students can register directly with us
 - If registration is not possible via ZPA
- · Please let us know if problems persist.

R Leibe

Course Outline

- Single-Object Tracking
 - > Background modeling
 - Template based tracking
 - Color based tracking
 - > Contour based tracking
 - > Tracking by online classification
 - > Tracking-by-detection
- Bayesian Filtering
 - Kalman filters
 - Particle filters
 - > Case studies
- Multi-Object Tracking
- Articulated Tracking



Today: Beyond Gaussian Error Models

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Topics of This Lecture

- · Recap: Extended Kalman Filter
 - > Detailed algorithm
- Particle Filters: Detailed Derivation
 - Recap: Basic idea
 - Importance Sampling
 - > Sequential Importance Sampling (SIS)
 - Transitional prior
 - Resampling
 - Generic Particle Filter
 - Sampling Importance Resampling (SIR)

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Recap: Kalman Filter

- recup, raman ince
- Algorithm summary
 Assumption: linear model

$$\mathbf{x}_t = \mathbf{D}_t \mathbf{x}_{t-1} + \varepsilon_t$$

 $y_t = M_t x_t + \delta_t$

Prediction step

$$\mathbf{x}_{t}^{-} = \mathbf{D}_{t}\mathbf{x}_{t-1}^{+}$$

$$\boldsymbol{\Sigma}_t^- \ = \ \mathbf{D}_t \boldsymbol{\Sigma}_{t-1}^+ \mathbf{D}_t^T + \boldsymbol{\Sigma}_{d_t}$$

Correction step

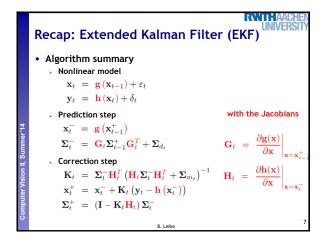
$$\mathbf{K}_t \; = \; \mathbf{\Sigma}_t^- \mathbf{M}_t^T \left(\mathbf{M}_t \mathbf{\Sigma}_t^- \mathbf{M}_t^T + \mathbf{\Sigma}_{m_t}
ight)^{-1}$$

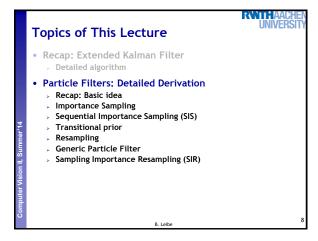
$$\mathbf{x}_{t}^{+} = \mathbf{x}_{t}^{-} + \mathbf{K}_{t} \left(\mathbf{y}_{t} - \mathbf{M}_{t} \mathbf{x}_{t}^{-} \right)$$

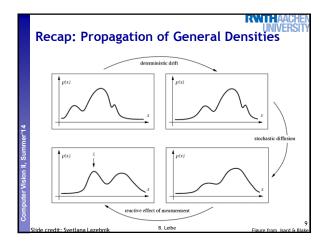
$$\Sigma_t^+ = (\mathbf{I} - \mathbf{K}_t \mathbf{M}_t) \Sigma_t^-$$

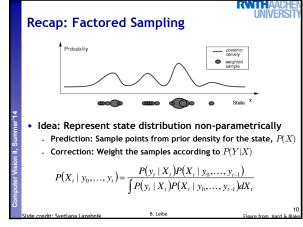
B. Leibe

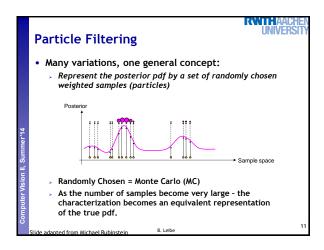
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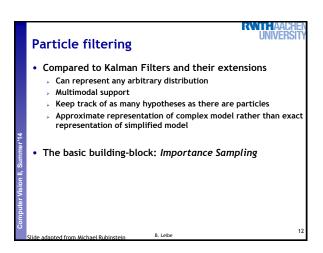


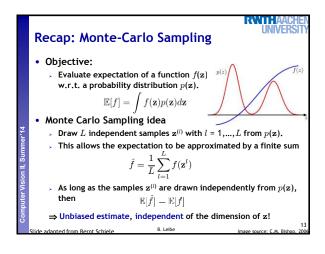


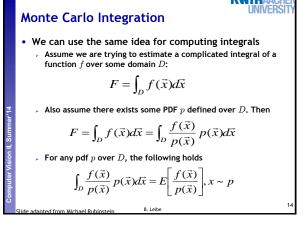


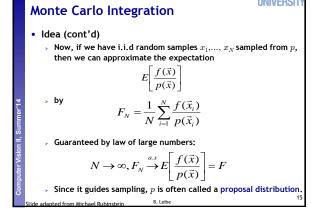


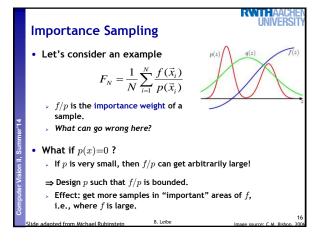


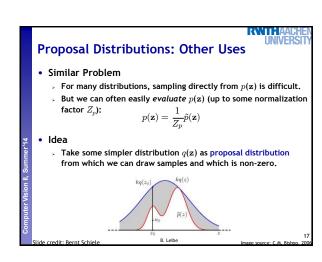


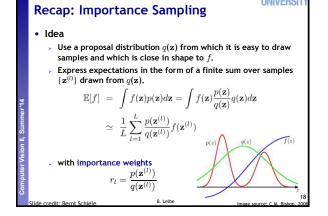


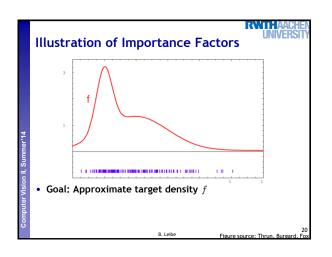


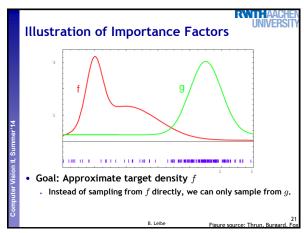


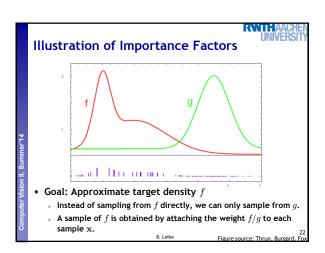


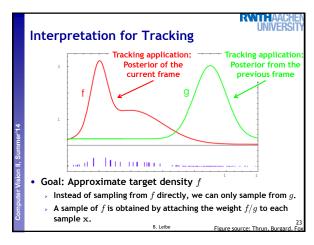




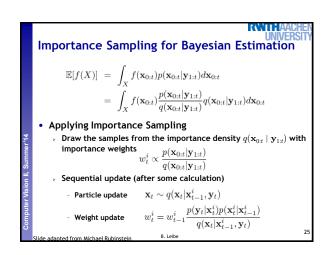


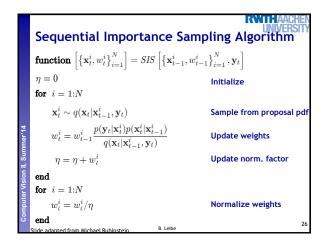


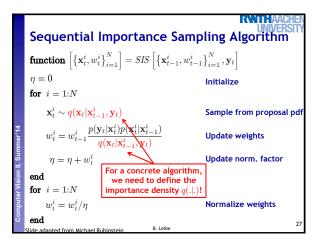


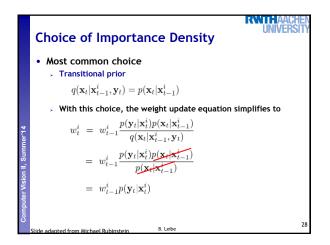


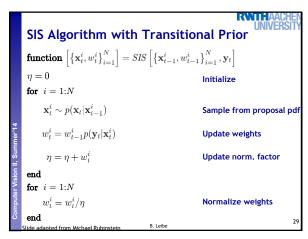
Importance Sampling for Bayesian Estimation $\mathbb{E}[f(X)] = \int_X f(\mathbf{x}_{0:t}) p(\mathbf{x}_{0:t}|\mathbf{y}_{1:t}) d\mathbf{x}_{0:t} \\ = \int_X f(\mathbf{x}_{0:t}) \frac{p(\mathbf{x}_{0:t}|\mathbf{y}_{1:t})}{q(\mathbf{x}_{0:t}|\mathbf{y}_{1:t})} q(\mathbf{x}_{0:t}|\mathbf{y}_{1:t}) d\mathbf{x}_{0:t}$ • Applying Importance Sampling . Characterize the posterior pdf using a set of samples (particles) and their weights $\left\{\mathbf{x}_{0:t}^i, w_t^i\right\}_{i=1}^N$ • Then the joint posterior is approximated by $p(\mathbf{x}_{0:t}|\mathbf{y}_{1:t}) \approx \sum_{i=1}^N w_t^i \delta(\mathbf{x}_{0:t} - \mathbf{x}_{0:t}^i)$ Slide adapted from Michael Rubinstein

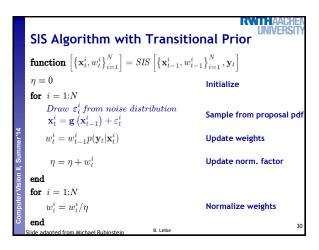


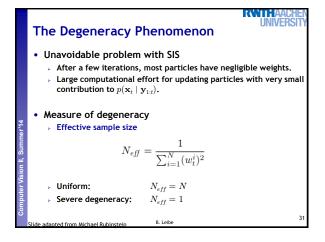




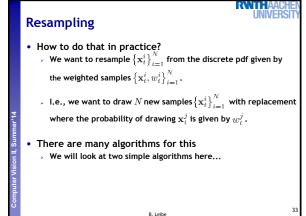


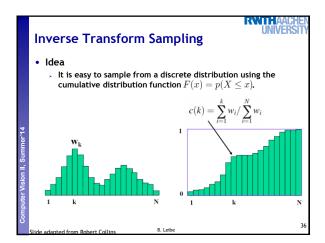


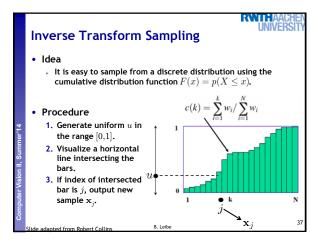


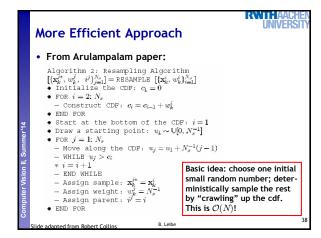


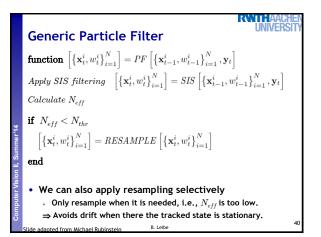
Resampling • Idea • Eliminate particles with low importance weights and increase the number of particles with high importance weight. $\left\{\mathbf{x}_t^i, w_t^i\right\}_{i=1}^N \to \left\{\mathbf{x}_t^{i*}, \frac{1}{N}\right\}_{i=1}^N$ • The new set is generated by sampling with replacement from the discrete representation of $p(\mathbf{x}_t \mid \mathbf{y}_{1:t})$ such that $Pr\left\{\mathbf{x}_t^{i*} = \mathbf{x}_t^j\right\} = w_t^j$

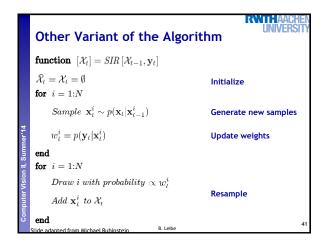


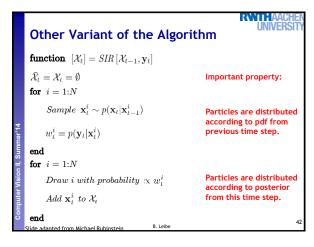


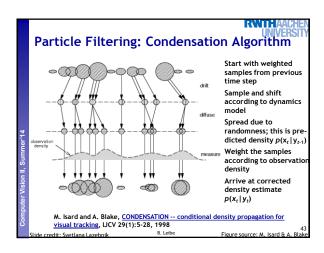


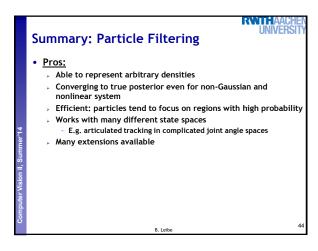




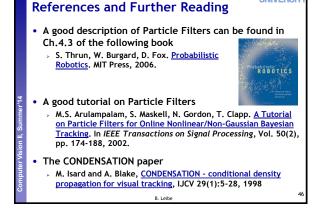








Summary: Particle Filtering • Cons / Caveats: • #Particles is important performance factor • Want as few particles as possible for efficiency. • But need to cover state space sufficiently well. • Worst-case complexity grows exponentially in the dimensions • Multimodal densities possible, but still single object • Interactions between multiple objects require special treatment. • Not handled well in the particle filtering framework (state space explosion).



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