

# **Computer Vision II - Lecture 5**

### **Contour based Tracking**

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**Bastian Leibe** 

**RWTH Aachen** 

http://www.vision.rwth-aachen.de

leibe@vision.rwth-aachen.de

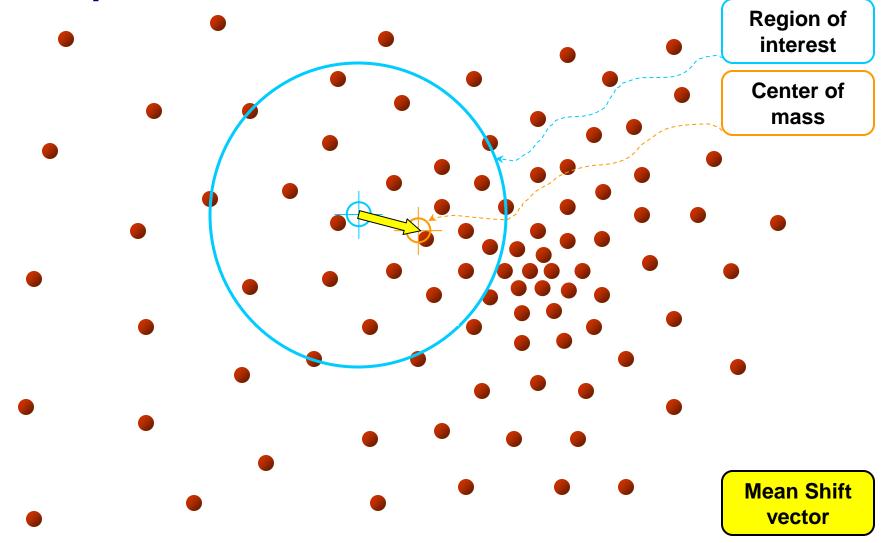
### **Course Outline**

- Single-Object Tracking
  - Background modeling
  - Template based tracking
  - Color based tracking
  - Contour based tracking
  - > Tracking by online classification
  - Tracking-by-detection
- Bayesian Filtering
- Multi-Object Tracking
- Articulated Tracking





Recap: Mean-Shift



Objective: Find the densest region

## Recap: Using Mean-Shift on Color Models

### Two main approaches

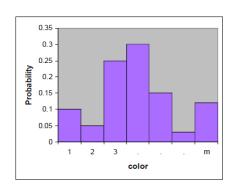
#### 1. Explicit weight images

- Create a color likelihood image, with pixels weighted by the similarity to the desired color (best for unicolored objects).
- Use mean-shift to find spatial modes of the likelihood.



#### 2. Implicit weight images

- Represent color distribution by a histogram.
- Use mean-shift to find the region that has the most similar color distribution.



4



## Mean-Shift on Weight Images

#### Ideal case

Want an indicator function that returns 1 for pixels on the tracked object and 0 for all other pixels.

#### Instead

- Compute likelihood maps
- Value at a pixel is proportional to the likelihood that the pixel comes from the tracked object.



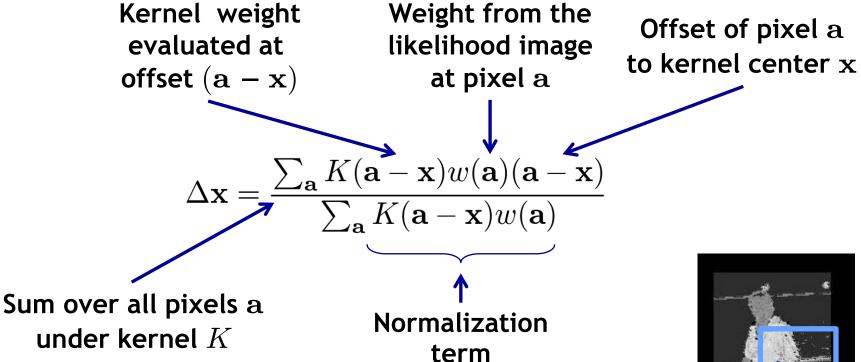
- Color
- Texture
- Shape (boundary)
- Predicted location



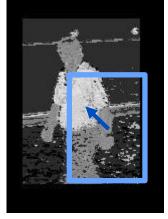


# Recap: Mean-Shift Tracking

• Mean-Shift finds the mode of an explicit likelihood image

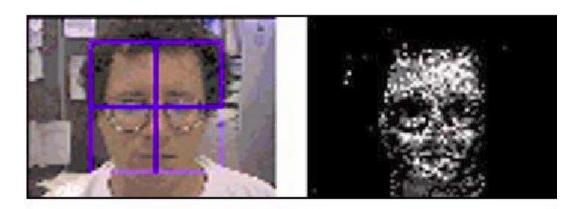


⇒ Mean-shift computes the weighted mean of all shifts (offsets), weighted by the point likelihood and the kernel function centered at x.





### Recap: Explicit Weight Images



- Histogram backprojection
  - ightharpoonup Histogram is an empirical estimate of  $p(color \mid object) = p(c \mid o)$

> Bayes' rule says: 
$$p(o|c) = \frac{p(c|o)p(o)}{p(c)}$$

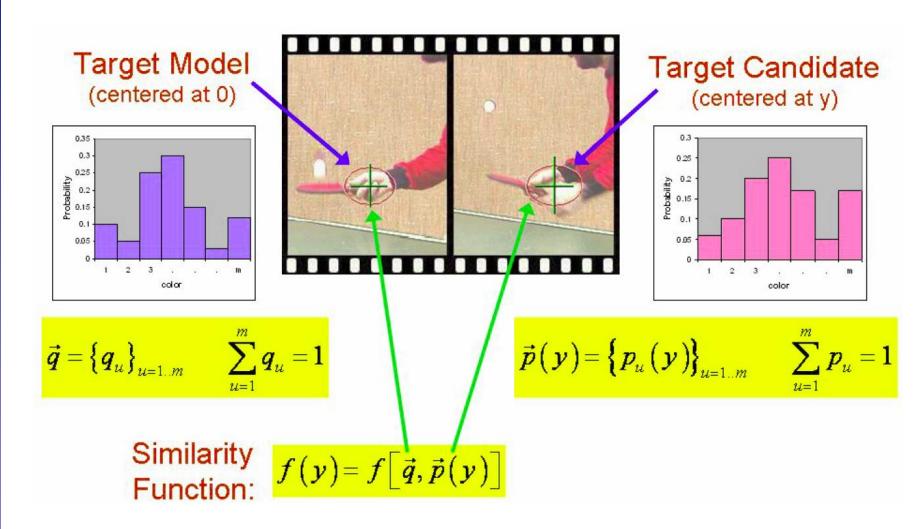
- > Simplistic approximation: assume p(o)/p(c) is constant.
- $\Rightarrow$  Use histogram h as a lookup table to set pixel values in the weight image.
- ightharpoonup If pixel maps to histogram bucket i, set weight for pixel to h(i).

### Recap: Scale Adaptation in CAMshift



Mean shift window initialization

# Recap: Tracking with Implicit Weight Images







# Recap: Comaniciu's Mean-Shift

Color histogram representation

target model:

$$\hat{\mathbf{q}} = {\{\hat{q}_u\}}_{u=1\dots m}$$

$$\sum_{u=1}^{m} \hat{q}_u = 1$$

target candidate:

$$\hat{\mathbf{p}}(\mathbf{y}) = \{\hat{p}_u(\mathbf{y})\}_{u=1...m}$$

$$\sum_{u=1}^{m} \hat{p}_u = 1 .$$

- Measuring distances between histograms
  - > Distance as a function of window location y

$$d(\mathbf{y}) = \sqrt{1 - \rho \left[\hat{\mathbf{p}}(\mathbf{y}), \hat{\mathbf{q}}\right]}$$

ightarrow where  $\hat{
ho}(\mathbf{y})$  is the Bhattacharyya coefficient

$$\hat{\rho}(\mathbf{y}) \equiv \rho \left[\hat{\mathbf{p}}(\mathbf{y}), \hat{\mathbf{q}}\right] = \sum_{u=1}^{m} \sqrt{\hat{p}_u(\mathbf{y})\hat{q}_u},$$



## Recap: Comaniciu's Mean-Shift

Compute histograms via Parzen estimation

$$\hat{q}_u = C \sum_{i=1}^n k(\|\mathbf{x}_i^{\star}\|^2) \delta \left[ b(\mathbf{x}_i^{\star}) - u \right] ,$$

$$\hat{p}_u(\mathbf{y}) = C_h \sum_{i=1}^{n_h} k \left( \left\| \frac{\mathbf{y} - \mathbf{x}_i}{h} \right\|^2 \right) \delta \left[ b(\mathbf{x}_i) - u \right] ,$$

- where  $k(\cdot)$  is some radially symmetric smoothing kernel profile,  $\mathbf{x}_i$  is the pixel at location i, and  $b(\mathbf{x}_i)$  is the index of its bin in the quantized feature space.
- Consequence of this formulation
  - Gathers a histogram over a neighborhood
  - Also allows interpolation of histograms centered around an off-lattice location.



12

# Recap: Result of Taylor Expansion

Simple update procedure: At each iteration, perform

$$\hat{\mathbf{y}}_{1} = \frac{\sum_{i=1}^{n_{h}} \mathbf{x}_{i} w_{i} g\left(\left\|\frac{\hat{\mathbf{y}}_{0} - \mathbf{x}_{i}}{h}\right\|^{2}\right)}{\sum_{i=1}^{n_{h}} w_{i} g\left(\left\|\frac{\hat{\mathbf{y}}_{0} - \mathbf{x}_{i}}{h}\right\|^{2}\right)} \quad \text{where } g(x) = -k'(x),$$

- which is just standard mean-shift on (implicit) weight image  $w_i$ .
- $\triangleright$  Let's look at the weight image more closely. For each pixel  $\mathbf{x}_i$

$$w_i = \sum_{u=1}^m \sqrt{\frac{\hat{q}_u}{\hat{p}_u(\hat{\mathbf{y}}_0)}} \delta\left[b(\mathbf{x}_i) - u\right].$$
 This is only 1 once in the summation

 $\Rightarrow$  If pixel  $\mathbf{x}_i$ 's value maps to histogram bucket B, then

$$w_i = \sqrt{q_B/p_B(\mathbf{y}_0)}$$



# **Today: Contour based Tracking**





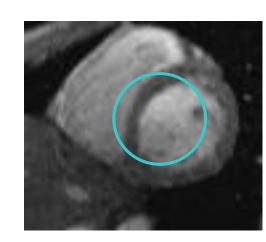
### **Topics of This Lecture**

- Deformable contours
  - Motivation
  - Contour representation
- Defining the energy function
  - External energy
  - Internal energy
- Energy minimization
  - Greedy approach
  - Dynamic Programming approach
- Extensions
  - Tracking
  - Level Sets



### **Deformable Contours**

- Given
  - Initial contour (model) near desired object



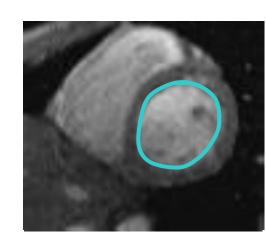
M. Kass, A. Witkin, D. Terzopoulos. <u>Snakes: Active Contour Models</u>, IJCV1988.



### **Deformable Contours**

#### Given

- Initial contour (model) near desired object
- Goal
  - Evolve the contour to fit the exact object boundary



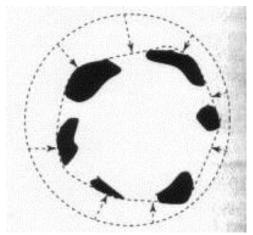
#### Main ideas

- Iteratively adjust the elastic band so as to be near image positions with high gradients, and
- Satisfy shape "preferences" or contour priors
- > Formulation as energy minimization problem.

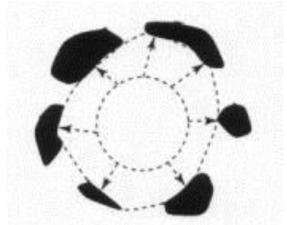
M. Kass, A. Witkin, D. Terzopoulos. <u>Snakes: Active Contour Models</u>, IJCV1988.

### **Deformable Contours: Intuition**

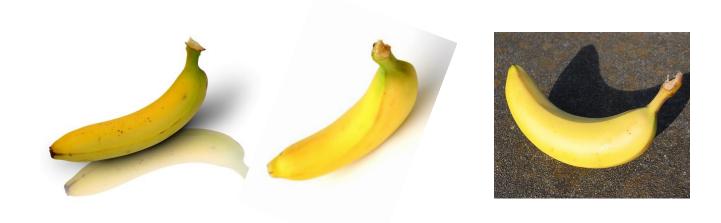








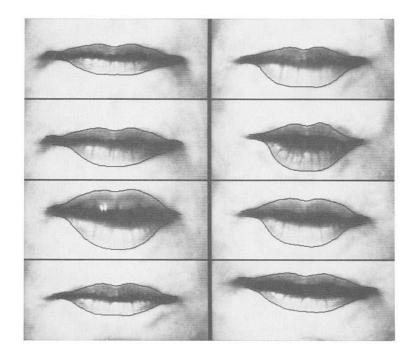
# Why Do We Want Deformable Shapes?



#### Motivations

Some objects have similar basic form, but some variety in contour shape.

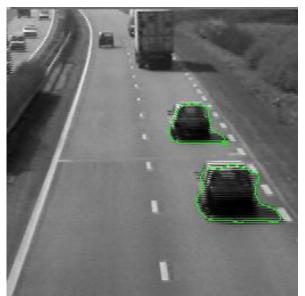
### Why Do We Want Deformable Shapes?

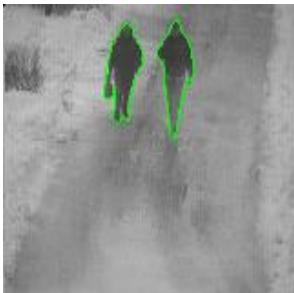


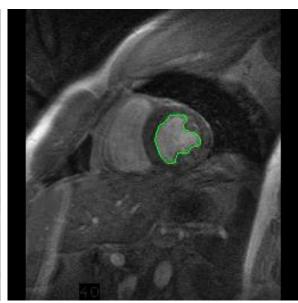
#### Motivations

- Some objects have similar basic form, but some variety in contour shape.
- Non-rigid, deformable objects can change their shape over time, e.g. lips, hands...

### Why Do We Want Deformable Shapes?







#### Motivations

- Some objects have similar basic form, but some variety in contour shape.
- Non-rigid, deformable objects can change their shape over time, e.g. lips, hands...
- Contour shape may be an important cue for tracking



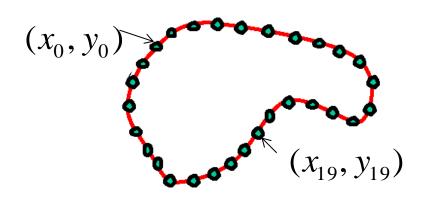
## **Topics of This Lecture**

- Deformable contours
  - Motivation
  - Contour representation
- Defining the energy function
  - External energy
  - Internal energy
- Energy minimization
  - Greedy approach
  - Dynamic Programming approach
- Extensions
  - Tracking
  - Level Sets



## **Contour Representation**

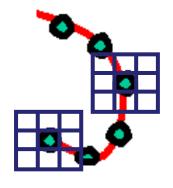
- Discrete representation
  - We'll consider a discrete representation of the contour, consisting of a list of 2D point positions ("vertices").



$$\boldsymbol{\nu}_i = (x_i, y_i),$$

for 
$$i = 0, 1, ..., n-1$$

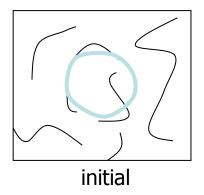
At each iteration, we'll have the option to move each vertex to another nearby location ("state").

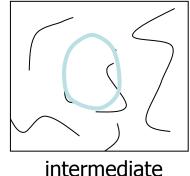


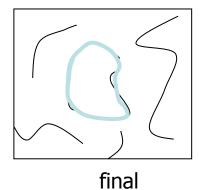


# Fitting Deformable Contours

- How to adjust the current contour to form the new contour at each iteration?
  - Define a cost function ("energy" function) that says how good a candidate configuration is.
  - Seek next configuration that minimizes that cost function.







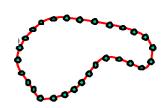
23



### **Energy Function**

#### Definition

Total energy (cost) of the current snake



$$E_{total} = E_{internal} + E_{external}$$

### Internal energy

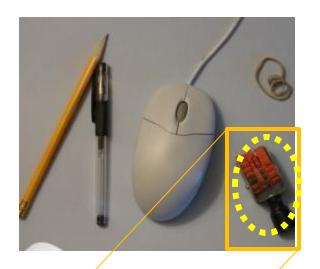
Encourage prior shape preferences: e.g., smoothness, elasticity, particular known shape.

### External energy

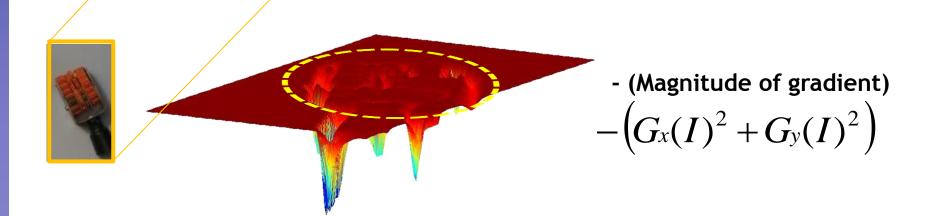
- Encourage contour to fit on places where image structures exist, e.g., edges.
- ⇒ Good fit between current deformable contour and target shape in the image will yield a low value for this cost function.



# **External Image Energy**



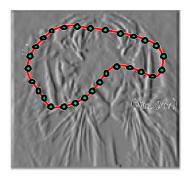
- How do edges affect snap of rubber band?
  - Think of external energy from image as gravitational pull towards areas of high contrast.

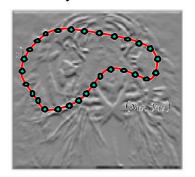




### **External Image Energy**

• Gradient images  $G_x(x, y)$  and  $G_y(x, y)$ 





External energy at a point on the curve is:

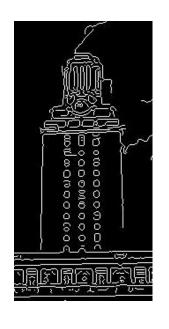
$$E_{external}(v) = -(|G_x(v)|^2 + |G_y(v)|^2)$$

External energy for the whole curve:

$$E_{external} = -\sum_{i=0}^{n-1} |G_x(x_i, y_i)|^2 + |G_y(x_i, y_i)|^2$$



### **Internal Energy: Intuition**





What are the underlying boundaries in this fragmented edge image?

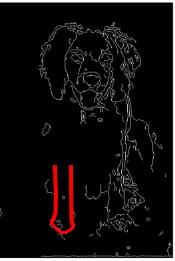
And in this one?



## **Internal Energy: Intuition**

- A priori, we want to favor
  - Smooth shapes
  - Contours with low curvature
  - Contours similar to a known shape, etc. to balance what is actually observed (i.e., in the gradient image).









### Internal Energy

#### Common formulatoin

- For a continuous curve, a common internal energy term is the "bending energy".
- At some point v(s) on the curve, this is:

$$E_{internal}(v(s)) = \alpha \left| \frac{dv}{ds} \right|^2 + \beta \left| \frac{d^2v}{d^2s} \right|^2$$

Tension, Elasticity

Stiffness, Curvature





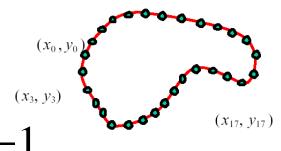
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Slide credit: Kristen Grauman



### **Internal Energy**

• For our discrete representation,



$$v_i = (x_i, y_i)$$
  $i = 0 \dots n-1$ 

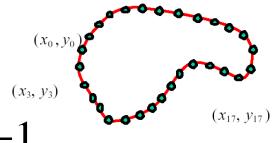
$$\frac{dv}{ds} \approx v_{i+1} - v_i \qquad \frac{d^2v}{ds^2} \approx (v_{i+1} - v_i) - (v_i - v_{i-1}) = v_{i+1} - 2v_i + v_{i-1}$$

Note these are derivatives relative to position - not spatial image gradients.



### Internal Energy

• For our discrete representation,



$$v_i = (x_i, y_i)$$
  $i = 0 \dots n-1$ 

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$$\frac{dv}{ds} \approx v_{i+1} - v_i \qquad \frac{d^2v}{ds^2} \approx (v_{i+1} - v_i) - (v_i - v_{i-1}) = v_{i+1} - 2v_i + v_{i-1}$$

Internal energy for the whole curve:

$$E_{internal} = \sum_{i=0}^{n-1} \alpha \| v_{i+1} - v_i \|^2 + \beta \| v_{i+1} - 2v_i + v_{i-1} \|^2$$

Why do these reflect tension and curvature?



# **Example: Compare Curvature**

$$E_{curvature}(v_i) = \|v_{i+1} - 2v_i + v_{i-1}\|^2$$

$$= (x_{i+1} - 2x_i + x_{i-1})^2 + (y_{i+1} - 2y_i + y_{i-1})^2$$
(2,5)

(1,1)

 $\bigcirc$ 

(3,1)

(1,1)

(2,2)

(3,1)

$$(3-2(2)+1)^2 + (1-2(5)+1)^2$$
  
=  $(-8)^2 = 64$ 

$$(3-2(2)+1)^2 + (1-2(2)+1)^2$$
  
=  $(-2)^2 = 4$ 

B. Leibe

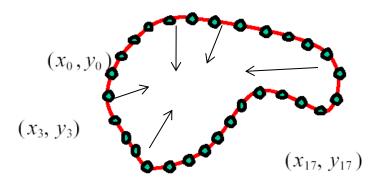


### **Penalizing Elasticity**

 Current elastic energy definition uses a discrete estimate of the derivative:

$$E_{elastic} = \sum_{i=0}^{n-1} \alpha \| v_{i+1} - v_i \|^2$$

$$= \alpha \cdot \sum_{i=0}^{n-1} (x_{i+1} - x_i)^2 + (y_{i+1} - y_i)^2$$



What is a possible problem with this definition?



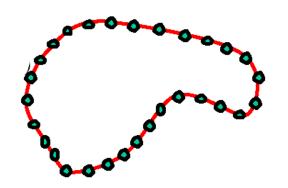
### **Penalizing Elasticity**

 Current elastic energy definition uses a discrete estimate of the derivative:

$$E_{elastic} = \sum_{i=0}^{n-1} \alpha \| v_{i+1} - v_i \|^2$$

Instead:

$$= \alpha \cdot \sum_{i=0}^{n-1} \left( (x_{i+1} - x_i)^2 + (y_{i+1} - y_i)^2 - \overline{d} \right)^2$$

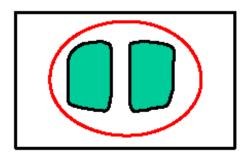


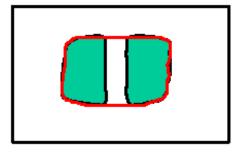
where d is the average distance between pairs of points - updated at each iteration.

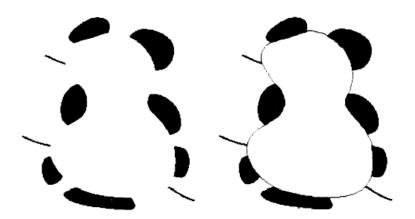


# **Dealing with Missing Data**

- Effect of Internal Energy
  - Preference for low-curvature, smoothness helps dealing with missing data







Illusory contours found!

# Extending the Internal Energy: Shape Priors

### Shape priors

If object is some smooth variation on a known shape, we can use a term that will penalize deviation from that shape:

$$E_{internal} + = \alpha \cdot \sum_{i=0}^{n-1} (\nu_i - \hat{\nu}_i)^2$$

 $\hat{\mathbf{v}}_i$ 

where  $\{\hat{v_i}\}$  are the points of the known shape.





# Putting Everything Together...

Total energy

$$E_{total} = E_{internal} + \gamma E_{external}$$

with the component terms

$$E_{external} = -\sum_{i=0}^{n-1} |G_x(x_i, y_i)|^2 + |G_y(x_i, y_i)|^2$$

$$E_{internal} = \sum_{i=0}^{n-1} \left( \alpha \left( \overline{d} - \| \nu_{i+1} - \nu_i \| \right)^2 + \beta \| \nu_{i+1} - 2\nu_i + \nu_{i-1} \|^2 \right)$$

Behavior can be controlled by adapting the weights  $\alpha$ ,  $\beta$ ,  $\gamma$ .

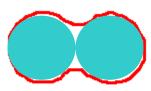


## **Total Energy**

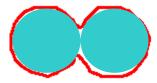
- Behavior varies as a function of the weights
  - $\triangleright$  E.g.,  $\alpha$  weight controls the penalty for internal elasticity.







 $\mathbf{medium} \ \alpha$ 

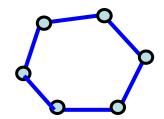


small  $\alpha$ 

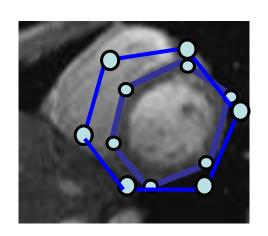


## **Summary: Deformable Contours**

- A simple elastic snake is defined by:
  - $\,\,floor\,\,$  A set of N points,
  - An internal energy term (tension, bending, plus optional shape prior)
  - An external energy term (gradient-based)



- To use to segment an object:
  - Initialize in the vicinity of the object
  - Modify the points to minimize the total energy
  - How can we do this minimization?





## **Topics of This Lecture**

- Deformable contours
  - Motivation
  - Contour representation
- Defining the energy function
  - External energy
  - > Internal energy
- Energy minimization
  - Greedy approach
  - Dynamic Programming approach
- Extensions
  - > Tracking
  - Level Sets



# **Energy Minimization**

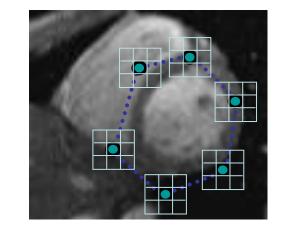
- Several algorithms have been proposed to fit deformable contours
  - Greedy search
  - Variational approaches
  - Dynamic programming (for 2D snakes)
  - **>** •••
- We'll look at two of them in the following...



## **Energy Minimization: Greedy**

#### Greedy optimization

- For each point, search window around it and move to where energy function is minimal.
- > Typical window size, e.g.,  $5 \times 5$  pixels



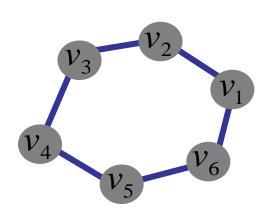
#### Stopping criterion

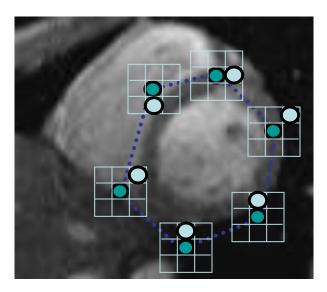
Stop when predefined number of points have not changed in last iteration, or after max number of iterations.

#### Note:

- Local optimization need decent initialization!
- Convergence not guaranteed

### **Energy Minimization: Dynamic Programming**





- Constraining the search space
  - Limit possible moves to neighboring pixels
  - With this form of the energy function, we can minimize using dynamic programming, with the Viterbi algorithm.
  - $\Rightarrow$  Optimal results in the local search space defined by the box.

A. Amini, T.E. Weymouth, R.C. Jain. <u>Using Dynamic Programming</u> for Solving Variational Problems in Vision, PAMI, Vol. 12(9), 1990.

44

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# **Energy Minimization: Dynamic Programming**

- Dynamic Programming optimization
  - Possible because snake energy can be rewritten as a sum of pairwise interaction potentials:

$$E_{total}(v_1,...,v_n) = \sum_{i=1}^{n-1} E_i(v_i,v_{i+1})$$

Or sum of triple interaction potentials

$$E_{total}(\nu_1, \dots, \nu_n) = \sum_{i=1}^{n-1} E_i(\nu_{i-1}, \nu_i, \nu_{i+1})$$

Slide credit: Kristen Grauman



## **Snake Energy: Pairwise Interactions**

Total energy

$$E_{total}(x_1, ..., x_n, y_1, ..., y_n) = -\sum_{i=1}^{n-1} |G_x(x_i, y_i)|^2 + |G_y(x_i, y_i)|^2 + |\alpha \cdot \sum_{i=1}^{n-1} (x_{i+1} - x_i)^2 + (y_{i+1} - y_i)^2$$

Rewriting the above with  $v_i=(x_i,\,y_i)$ :

$$E_{total}(v_1,...,v_n) = -\sum_{i=1}^{n-1} \|G(v_i)\|^2 + \alpha \cdot \sum_{i=1}^{n-1} \|v_{i+1} - v_i\|^2$$

Pairwise formulation

$$E_{total}(v_1,...,v_n) = E_1(v_1,v_2) + E_2(v_2,v_3) + ... + E_{n-1}(v_{n-1},v_n)$$

where  $E_i(v_i, v_{i+1}) = -\|G(v_i)\|^2 + \alpha \|v_{i+1} - v_i\|^2$ 

B. Leibe



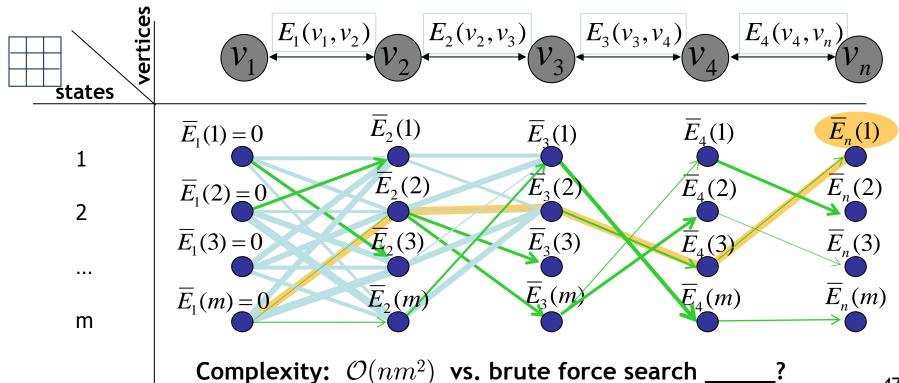
47

## Viterbi Algorithm

#### Main idea:

- Determine optimal state of predecessor, for each possible state
- Then backtrack from best state for last vertex

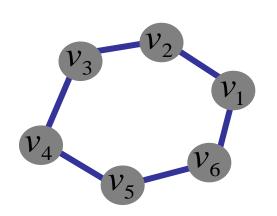
$$E_{total} = E_1(v_1, v_2) + E_2(v_2, v_3) + \dots + E_{n-1}(v_{n-1}, v_n)$$

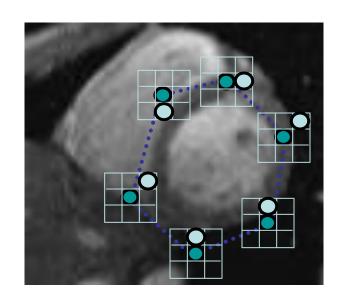


Slide credit: Kristen Grauman, adapted from Yuri Boykov



# **Summary: Dynamic Programming**





- Dynamic Programming solution
  - > Limit possible moves to neighboring pixels (discrete states).
  - Find the best joint move of all points using Viterbi algorithm.
  - Iterate until optimal position for each point is the center of the box, i.e., the snake is optimal in the local search space constrained by boxes.

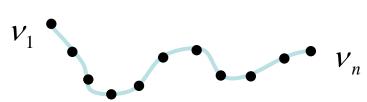
48

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## **Energy Minimization: Dynamic Programming**

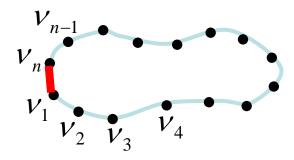
- Limitations
  - DP can be applied to optimize an open-ended snake

$$E_1(v_1, v_2) + E_2(v_2, v_3) + \dots + E_{n-1}(v_{n-1}, v_n)$$



For a closed snake, a loop is introduced into the energy

$$E_1(v_1, v_2) + E_2(v_2, v_3) + \dots + E_{n-1}(v_{n-1}, v_n) + E_n(v_n, v_1)$$



#### Workaround:

- 1) Fix  $v_1$  and solve for rest .
- 2) Fix an intermediate node at its position found in (1), solve for rest.

49



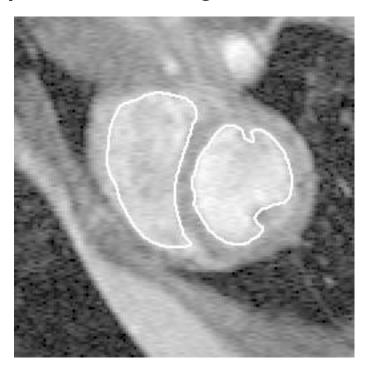
## **Topics of This Lecture**

- Deformable contours
  - Motivation
  - Contour representation
- Defining the energy function
  - External energy
  - Internal energy
- Energy minimization
  - > Greedy approach
  - Dynamic Programming approach
- Extensions
  - Tracking
  - Level Sets



# **Tracking via Deformable Contours**

- Idea
  - 1. Use final contour/model extracted at frame  $\,t\,$  as an initial solution for frame  $\,t\!+\!1\,$
  - **2.** Evolve initial contour to fit exact object boundary at frame t+1
  - 3. Repeat, initializing with most recent frame.



Tracking Heart Ventricles (multiple frames)

B. Leibe



# **Tracking via Deformable Contours**





#### Many applications

- Traffic monitoring, surveillance
- Human-computer interaction
- Animation
- Computer assisted diagnosis in medical imaging

**>** •••



#### **Limitations**

- Limitations of Dynamic Contours
  - May over-smooth the boundary



Cannot follow topological changes of objects





#### **Limitations**

#### External energy

Snake does not really "see" object boundaries in the image unless it gets very close to them.

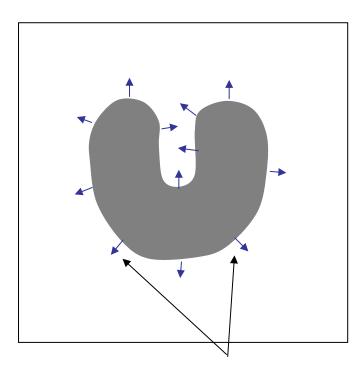
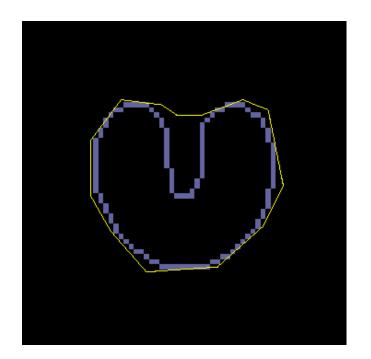


image gradients  $\nabla I$  are large only directly on the boundary





#### **Workaround: Distance Transform**

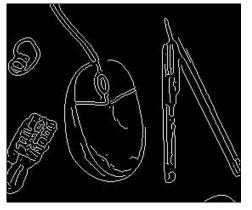
 External energy can instead be taken from the distance transform of the edge image.



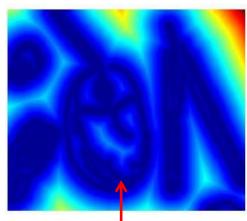
**Original** 



**Gradient** 



Edges
B. Leibe



Distance transform

Value at (x,y) tells how far that position is from the nearest edge point (or other binary image structure)

>> help bwdist



#### **Discussion**

#### Pros:

- Useful to track and fit non-rigid shapes
- Contour remains connected
- Possible to fill in "subjective" contours
- Flexibility in how energy function is defined, weighted.

#### Cons:

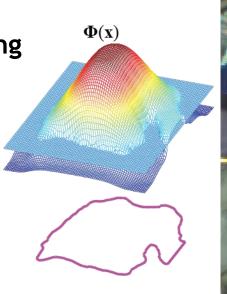
- Must have decent initialization near true boundary, may get stuck in local minimum.
- Parameters of energy function must be set well based on prior information
- Discrete optimization
- Unable to handle topological changes



#### **Extension: Level Sets**

#### Main idea

- Instead of explicitly representing the contour to track, model it implicitly as the zero-level set of a continuous embedding function  $\Phi(\mathbf{x})$ .
- Evolve the embedding function in order to better fit the image content.
- Leads to variational approaches.





#### Advantages

- Continuous optimization, easier to handle
- Can naturally cope with topological changes
- Not restricted to contour information, can also incorporate region information (color, texture, motion, disparity, etc.)



## Region-based Level Set Tracking

Using a color model to separate fg and bg regions



C. Bibby, I. Reid, <u>Robust Real-Time Visual Tracking using Pixel-Wise Posteriors</u>, *ECCV'08*.



### Summary

- Deformable shapes and active contours are useful for
  - > Segmentation: fit or "snap" to boundary in image
  - > Tracking: previous frame's estimate serves to initialize the next
- Fitting active contours:
  - Define terms to encourage certain shapes, smoothness, low curvature, push/pulls, ...
  - Use weights to control relative influence of each component cost
  - Can optimize 2d snakes with Viterbi algorithm.
- Image structure (esp. gradients) can act as attraction force for interactive segmentation methods.



## References and Further Reading

- The original Snakes paper
  - M. Kass, A. Witkin, D. Terzopoulos. <u>Snakes: Active Contour Models</u>, IJCV1988.
- The Dynamic Programming extension
  - A. Amini, T.E. Weymouth, R.C. Jain. <u>Using Dynamic</u> <u>Programming for Solving Variational Problems in Vision</u>, PAMI, Vol. 12(9), 1990.